ARCHITECTURAL STRUCTURES I:

STATICS AND STRENGTH OF MATERIALS

DR. ANNE NICHOLS SPRING 2008



beam forces internal

Internal Beam Forces 1 Lecture 13

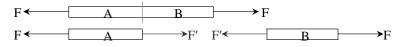
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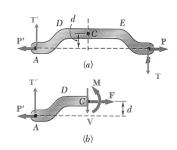
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Internal Forces

- trusses
 - axial only, (compression & tension)

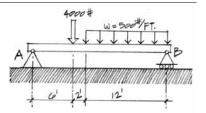


- in general
 - axial force
 - shear force, V
 - bending moment, M



Beams

- span horizontally
 - floors
 - bridges
 - roofs



- loaded transversely by gravity loads
- may have internal axial force
- will have internal shear force
- will have internal moment (bending)

Internal Ream Forces 4 Lecture 13

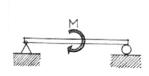
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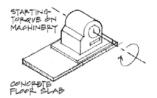
Beam Loading

- concentrated force
- concentrated moment
 - spandrel beams









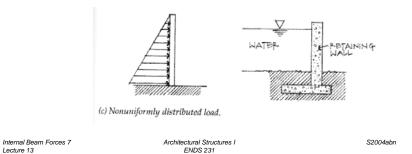
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Beam Loading

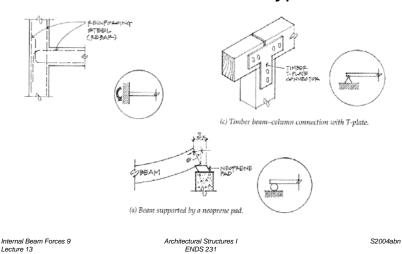
- uniformly distributed load (line load)
- non-uniformly distributed load
 - hydrostatic pressure
 - wind loads



Beam Supports

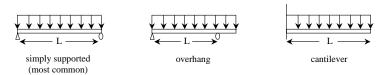
Lecture 13

• in the real world, modeled type

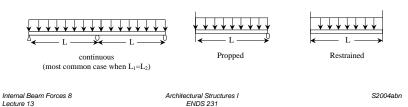


Beam Supports

statically determinate

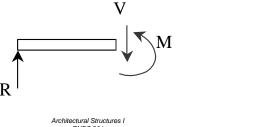


statically indeterminate



Internal Forces in Beams

- like method of sections / joints
 - no axial forces
- section must be in equilibrium
- want to know where biggest internal forces and moments are for designing

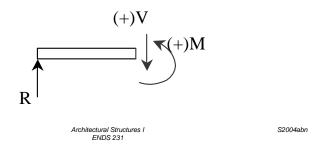


Internal Beam Forces 10

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V & M Diagrams

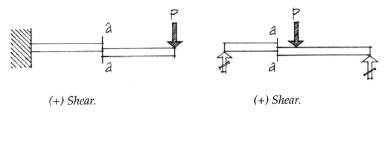
- tool to locate V_{max} and M_{max}
- <u>necessary</u> for designing
- have a <u>different sign convention</u> than external forces, moments, and reactions

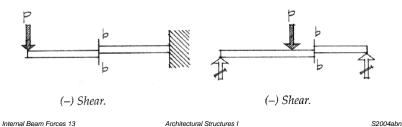


Shear Sign Convention

Internal Ream Forces 11

Lecture 13

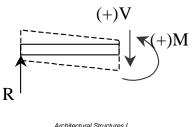




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Sign Convention

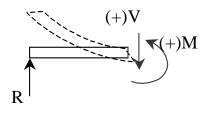
- shear force, V:
 - cut section to LEFT
 - if $\sum F_y$ is positive by statics, V acts down and is POSITIVE
 - beam has to resist shearing apart by V



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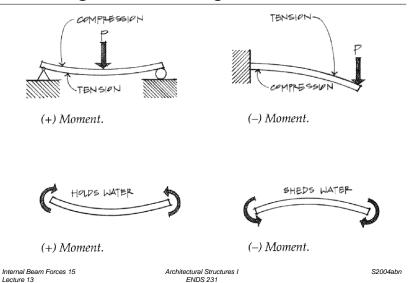
Sign Convention

- bending moment, M:
 - cut section to LEFT
 - if ∑M_{cut} is clockwise, M acts ccw and is POSITIVE – flexes into a "smiley" beam has to resist bending apart by M



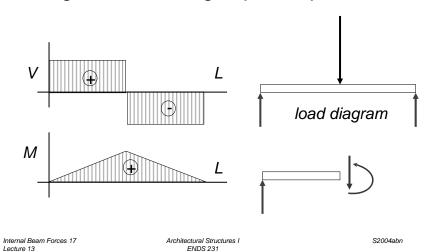
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Bending Moment Sign Convention

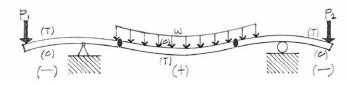


Constructing V & M Diagrams

along the beam length, plot V, plot M



Deflected Shape

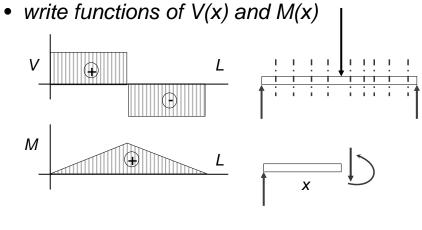


- positive bending moment
 - tension in bottom, compression in top
- negative bending moment
 - tension in top, compression in bottom
- zero bending moment
 - inflection point

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Mathematical Method

cut sections with x as width

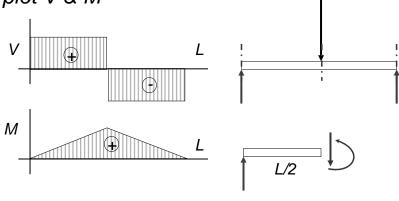


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Method 1: Equilibrium

cut sections at important places





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Method 2: Semigraphical

- by knowing
 - area under loading curve = change in V
 - area under shear curve = change in M
 - concentrated forces cause "jump" in V
 - concentrated moments cause "jump" in M

$$V_D - V_C = -\int_C^{X_D} w dx \qquad M_D - M_C = \int_C^{X_D} V dx$$

$$X_C$$

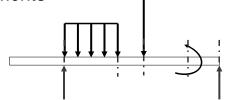
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Method 1: Equilibrium

- important places
 - supports
 - concentrated loads
 - start and end of distributed loads

- concentrated moments

- free ends
 - zero forces



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Method 2

relationships

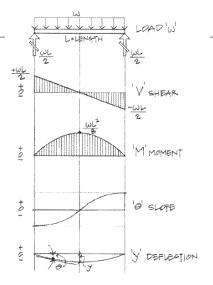
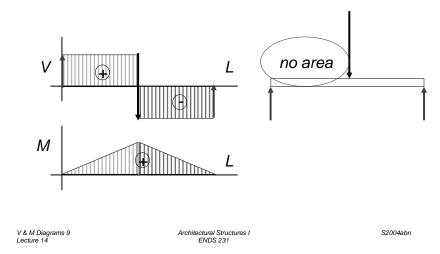


Figure 7.11 Relationship of load, shear, A moment, slope, and deflection diagrams.

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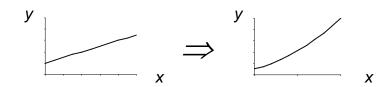
Method 2: Semigraphical

• M_{max} occurs where V = 0 (calculus)



Curve Relationships

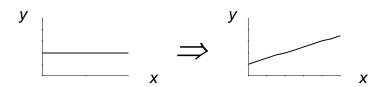
• line with slope, integrates to parabola



• ex: load to shear, shear to moment

Curve Relationships

- integration of functions
- line with 0 slope, integrates to sloped

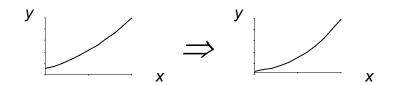


ex: load to shear, shear to moment

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Curve Relationships

• parabola, integrates to 3rd order curve



• ex: load to shear, shear to moment

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V & M Diagrams 12

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Basic Procedure

Find reaction forces & moments
 Plot axes, underneath beam load diagram

V.

- 2. Starting at left
- 3. Shear is 0 at free ends
- 4. Shear jumps with concentrated load
- 5. Shear changes with area under load

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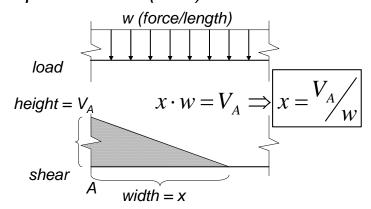
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M:

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Triangle Geometry

• slope of V is w (-w:1)



Parabolic Shapes

Basic Procedure

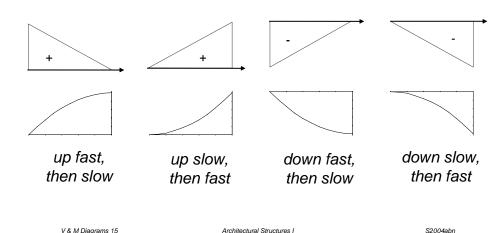
Starting at left

Moment is 0 at free ends

Moment jumps with moment

9. Moment changes with area under V

cases



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