#### ARCHITECTURAL STRUCTURES I:

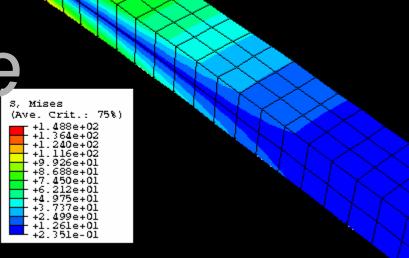
STATICS AND STRENGTH OF MATERIALS

**ENDS 231** 

DR. ANNE NICHOLS

SPRING 2008

twenty one

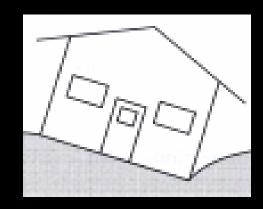


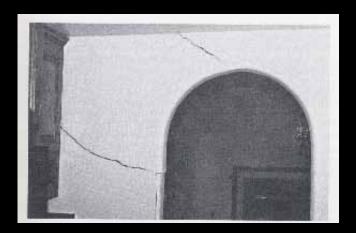
beams:

deflection & design

## Design for Strength +...

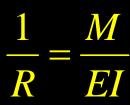
- strength design
  - forces & material
- serviceability
  - limit deflection and cracking
  - control noise & vibration
  - no excessive settlement of foundations
  - durability
  - appearance
  - component damage
  - ponding

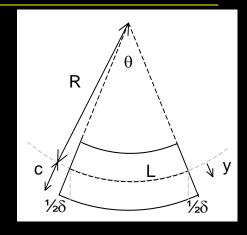




#### Beam Deformations

- curvature relates to
  - bending moment
  - modulus of elasticity
  - moment of inertia





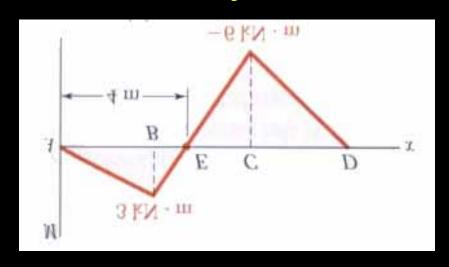
$$curvature = \frac{M(x)}{EI}$$

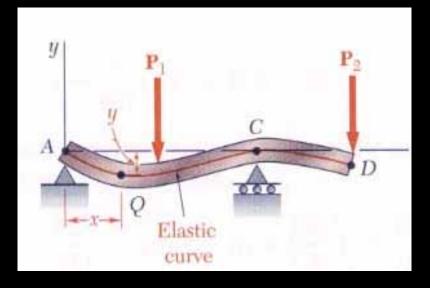
$$\theta = slope = \int \frac{M(x)}{EI} dx$$

$$\Delta = deflection = \int \int \frac{M(x)}{EI} dx$$

# Deflected Shape & M(x)

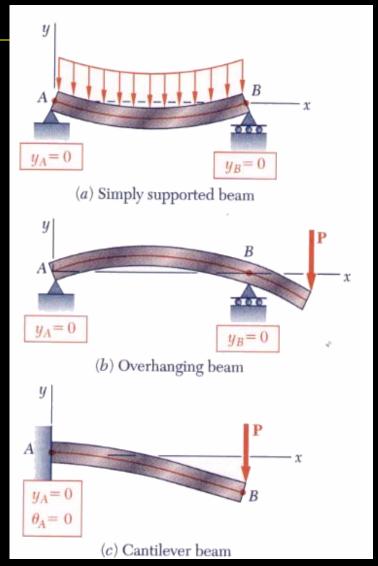
- -M(x) gives shape indication
- boundary conditions must be met





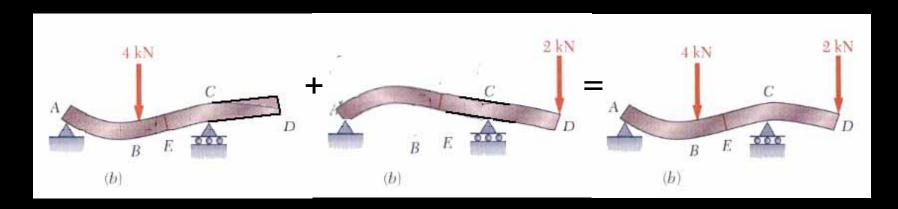
## Boundary Conditions

- at pins, rollers, fixed supports: y = 0
- at fixed supports:  $\theta = 0$
- at inflection points from symmetry:  $\theta = 0$
- $y_{max}$  at  $\frac{dy}{dx} = 0$



## Superpositioning

- if w can be <u>superpositioned</u>
  - $-\theta$  & y can
  - elastic range only!



#### **Deflection Limits**

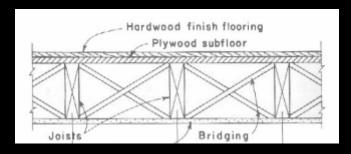
## • based on service condition, severity

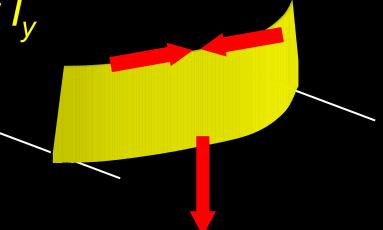
Use	LL only	DL+LL
Roof beams:		
Industrial	L/180	L/120
Commercial		
plaster ceiling	L/240	L/180
no plaster	L/360	L/240
Floor beams:		
Ordinary Usage	L/360	L/240
Roof or floor (damageable elements)		L/480

#### Lateral Buckling

- lateral buckling caused by compressive forces at top coupled with insufficient rigidity
- can occur at low stress levels

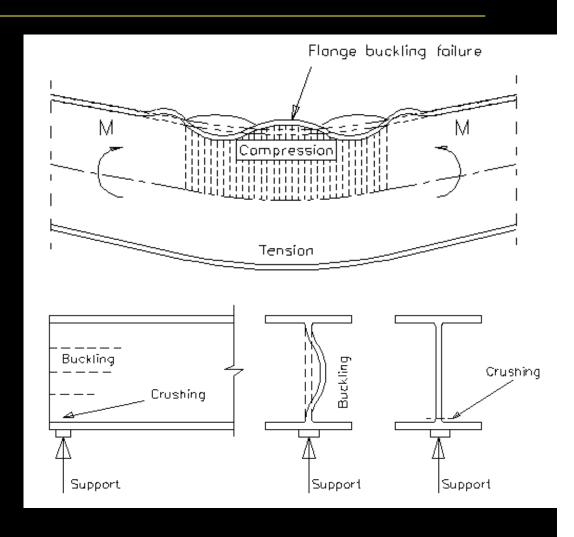
stiffen, brace or bigger I<sub>v</sub>





## Local Buckling

- steel I beams
- flange
  - buckle in direction of smaller radius of gyration
- web
  - force
  - "crippling"



# Local Buckling

## • flange

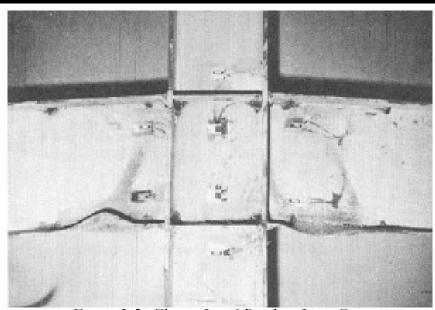


Figure 2-5. Flange Local Bending Limit State (Beedle, L.S., Christopher, R., 1964)

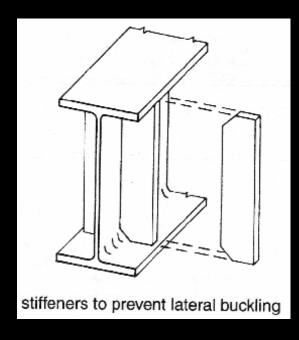
#### web

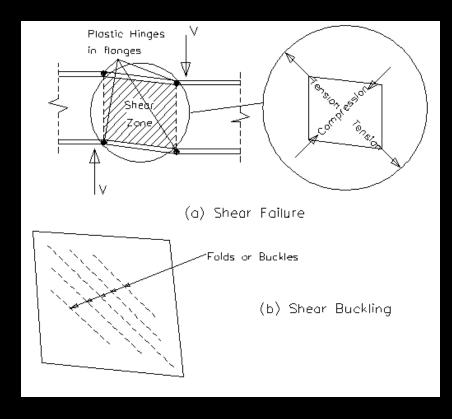


Figure 2-7. Web Local Buckling Limit State (SAC Project)

#### Shear in Web

- panels in plate girders or webs with large shear
- buckling in compression direction
- add stiffeners



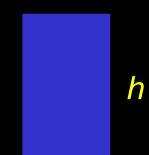


## Shear in Web

• plate girders and stiffeners



- 1. Know  $F_{all}$  for the material or  $F_{U}$  for LRFD
- 2. Draw V & M, finding M<sub>max</sub>



3. Calculate 
$$S_{req'd}$$
  $(f_b \leq F_b)$ 

b

$$S = \frac{bh^2}{6}$$

- $4^*$ . Include self weight for  $M_{max}$ 
  - and repeat 3 & 4 if necessary

#### 5. Consider lateral stability

Unbraced roof trusses were blown down in 1999 at this project in Moscow, Idaho.

Photo: Ken Carper



#### 6. Evaluate shear stresses - horizontal

- $(f_v \leq F_v)$
- W and rectangles

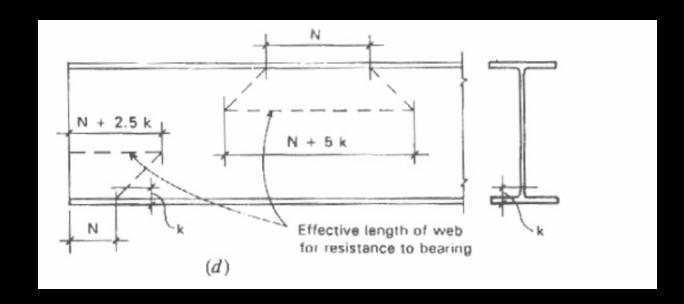
$$f_{v-\text{max}} = \frac{3V}{2A} \approx \frac{V}{A_{web}}$$

thin walled sections

$$f_{v-\text{max}} = \frac{VQ}{Ib}$$

# 7. Provide adequate bearing area at supports

$$f_p = \frac{P}{A} \le F_p$$



#### 8. Evaluate torsion

$$(f_v \leq F_v)$$

circular cross section

$$f_v = \frac{T\rho}{J}$$

rectangular

$$f_{v} = \frac{1}{c_{1}ab^{2}}$$

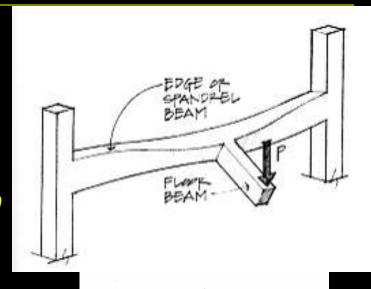
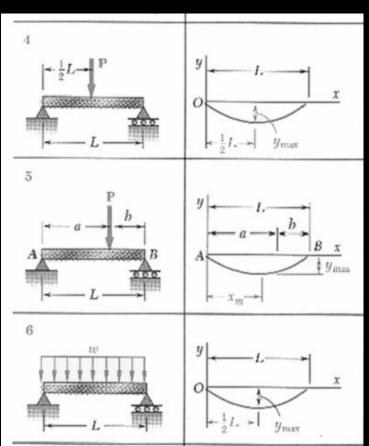
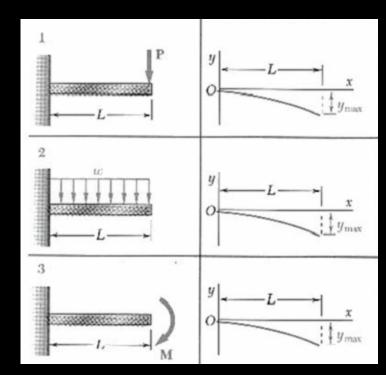


TABLE 3.1. Coefficients for Rectangular Bars in Torsion

a/b	<b>c</b> <sub>1</sub>	C <sub>2</sub>
1.0	° 0.208	0.1406
1.2	0.219	0.1661
1.5	0.231	0.1958
2.0	0.246	0.229
2.5	0.258	0.249
3.0	0.267	0.263
4.0	0.282	0.281
5.0	0.291	0.291
10.0	0.312	0.312
$\infty$	0.333	0.333

#### 9. Evaluate deflections

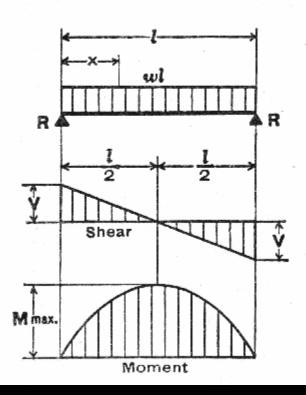




$$y_{\text{max}}(x) = \Delta_{actual} \le \Delta_{allowable}$$

#### 9. – how to read charts

#### SIMPLE BEAM—UNIFORMLY DISTRIBUTED LOAD



Total Equiv. Uniform Load . . . = 
$$wl$$

R = V . . . . . . =  $\frac{wl}{2}$ 

Vx . . . . . . =  $w\left(\frac{l}{2} - x\right)$ 

M max. (at center) . . . =  $\frac{wl^2}{8}$ 

Mx . . . . . . . =  $\frac{wx}{2}(l - x)$ 
 $\Delta max$ . (at center) . . . =  $\frac{5}{384}\frac{wl^4}{El}$ 
 $\Delta x$  . . . . . . . =  $\frac{wx}{24El}(l^3 - 2lx^2 + x^3)$