ARCHITECTURAL STRUCTURES I: STATICS AND STRENGTH OF MATERIALS

ENDS 231

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SPRING 2008

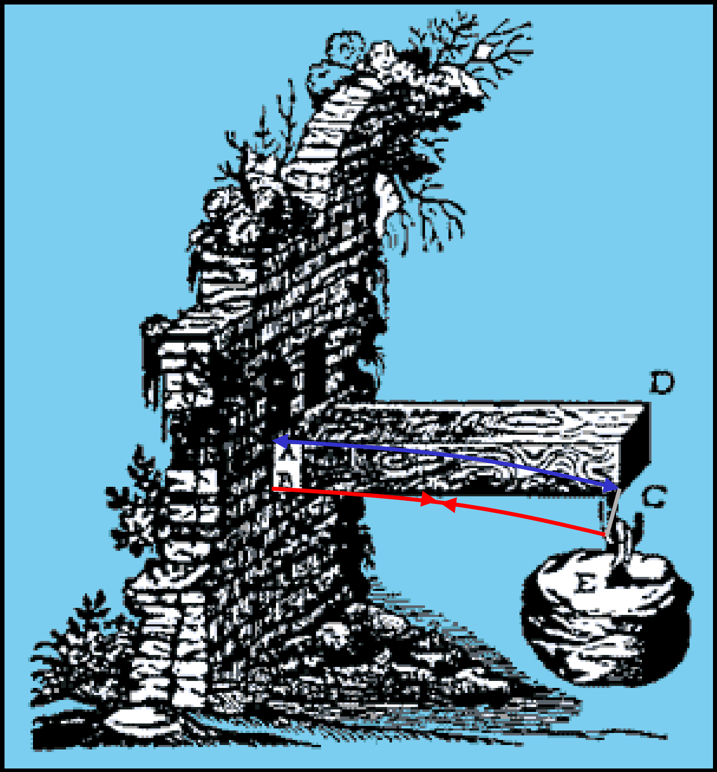
lecture

eighteen

beams: bending and shear

Beam Bending

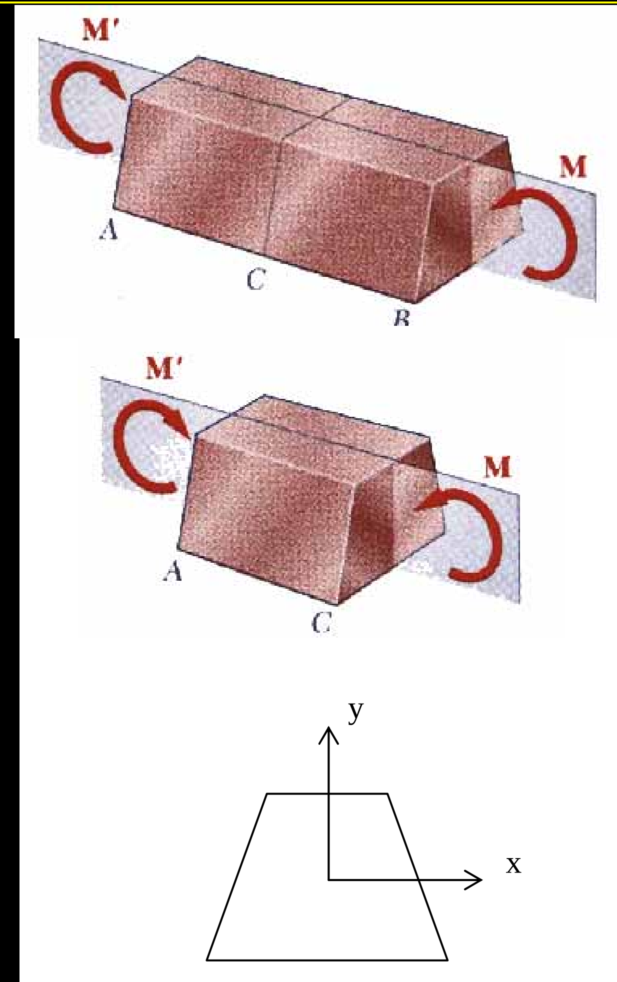
- Galileo
  - relationship between stress and depth^2
- can see
  - top squishing
  - bottom stretching



- what are the stress across the section?

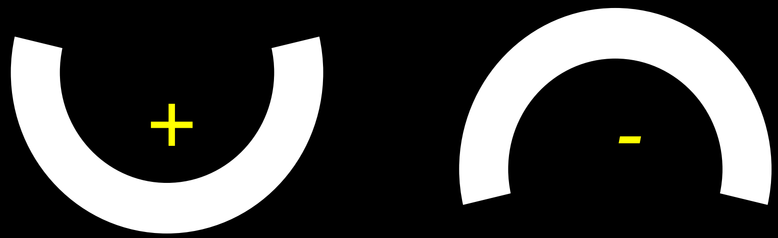
Pure Bending

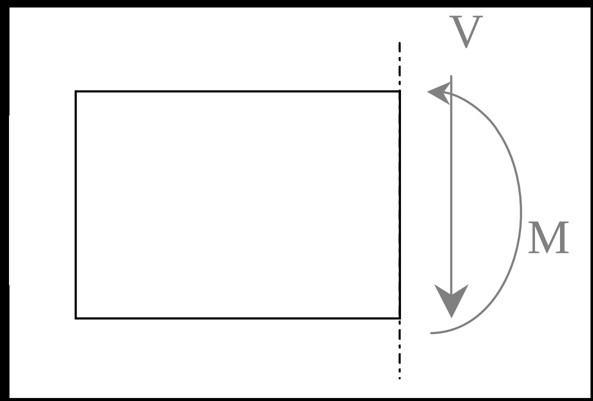
- *bending only*
- *no shear*
- *axial normal stresses from bending can be found in*
  - *homogeneous materials*
  - *plane of symmetry*
  - *follow Hooke's law*



Bending Moments

- sign convention:





- size of maximum internal moment will govern our design of the section

Normal Stresses

- *geometric fit*
  - *plane sections remain plane*
  - *stress varies linearly*

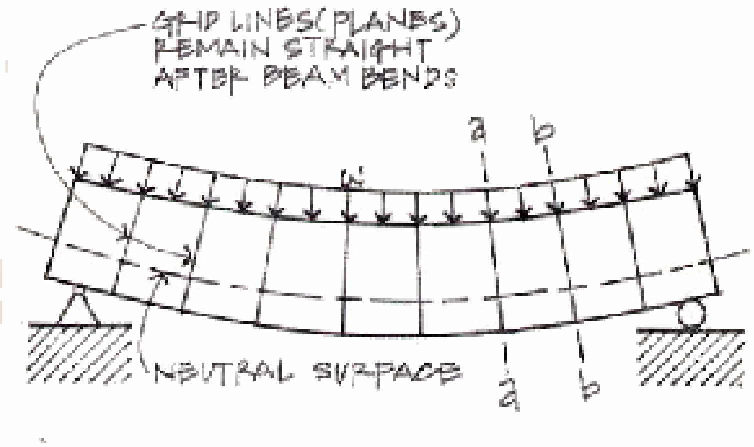


Figure 8.5(b) Beam bending under load.

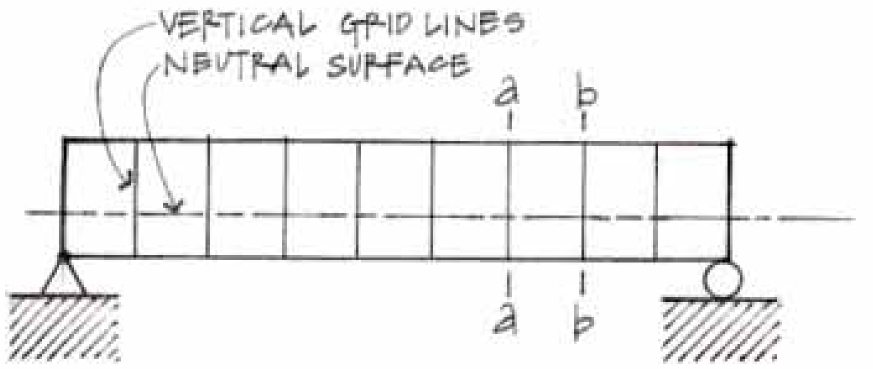
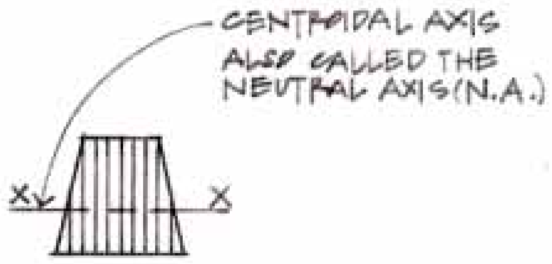


Figure 8.5(a) Beam elevation before loading.



Beam cross section.

Neutral Axis

- *stresses vary linearly*
- *zero stress occurs at the centroid*
- *neutral axis is line of centroids (n.a.)*

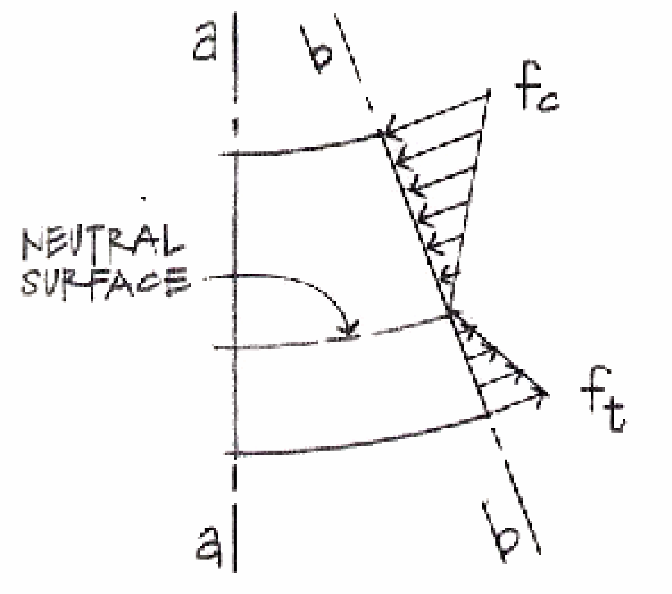
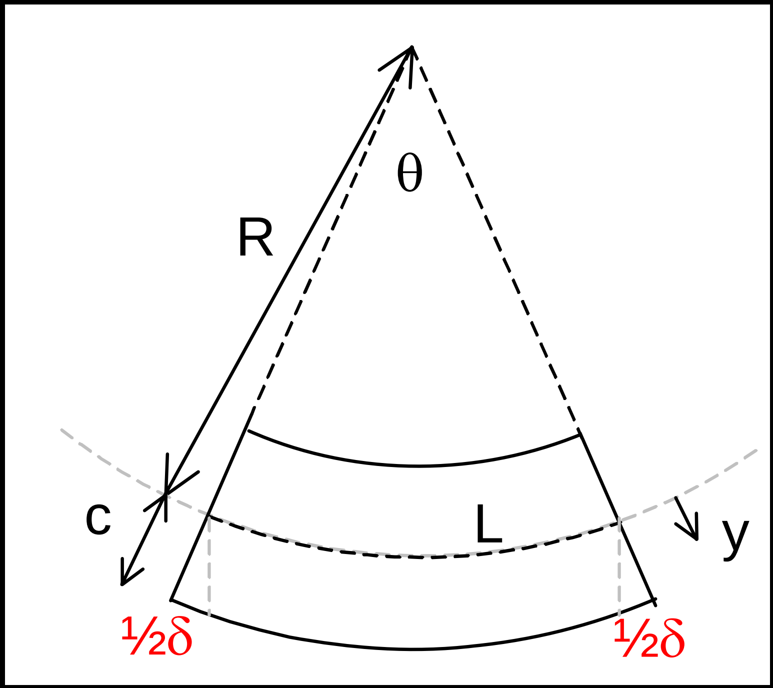


Figure 8.8 Bending stresses on section b-b.

Derivation of Stress from Strain

- pure bending = arc shape



$$L = R\theta$$

$$L_{outside} = (R + y)\theta$$

$$\varepsilon = \frac{\delta}{L} = \frac{L_{outside} - L}{L} = \frac{(R + y)\theta - R\theta}{R\theta} = \frac{y}{R}$$

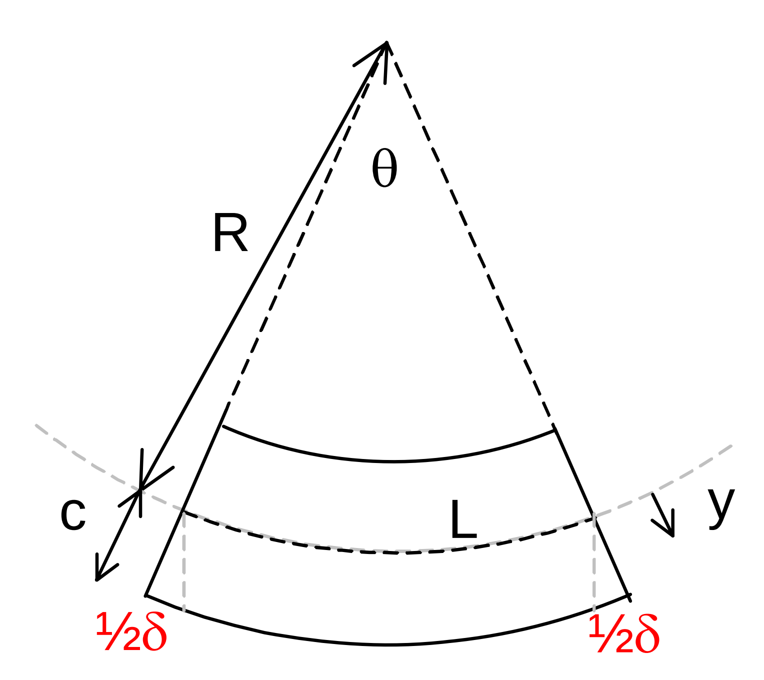
Derivation of Stress

- *zero stress at n.a.*

$$f = E\varepsilon = \frac{Ey}{R}$$

$$f_{\max} = \frac{Ec}{R}$$

$$f = \frac{y}{c} f_{\max}$$



Bending Moment

- *resultant moment from stresses = bending moment!*

$$M = \Sigma f y \Delta A$$

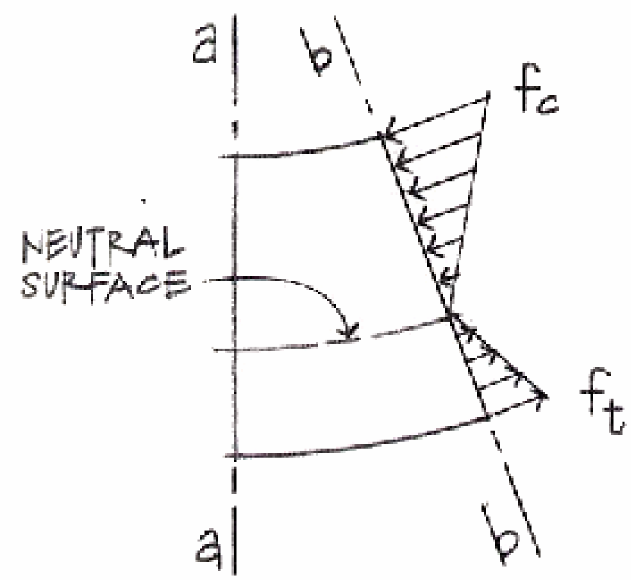


Figure 8.8 Bending stresses on section b-b.

$$= \Sigma \frac{y f_{max}}{c} y \Delta A = \frac{f_{max}}{c} \underline{\Sigma y^2 \Delta A} = \frac{f_{max}}{c} I = f_{max} S$$

Bending Stress Relations

$$\frac{1}{R} = \frac{M}{EI}$$

curvature

$$f_b = \frac{My}{I}$$

general bending stress

$$S = \frac{I}{c}$$

section modulus

$$f_b = \frac{M}{S}$$

maximum bending stress

$$S_{required} \geq \frac{M}{F_b}$$

required section modulus for design