Architectural Structures I: Statics and Strength of Materials

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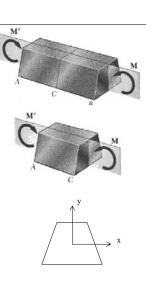


## beams: **2** bending and shear

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## Pure Bending

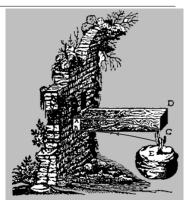
- bending only
- no shear
- axial normal stresses from bending can be found in
  - homogeneous materials
  - plane of symmetry
  - follow Hooke's law



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## Beam Bending

- Galileo
  - relationship between stress and depth<sup>2</sup>
- can see
  - top squishing
  - bottom stretching



• what are the stress across the section?

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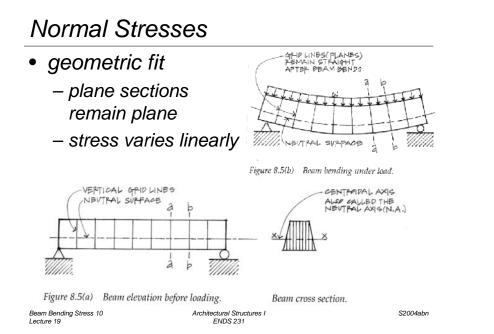
### **Bending Moments**

- sign convention:
  +
- size of maximum internal moment will govern our design of the section

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#### Neutral Axis

- stresses vary linearly
- zero stress occurs at the centroid
- <u>neutral axis</u> is line of centroids (n.a.)

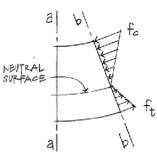


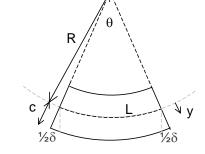
Figure 8.8 Bending stresses on section b-b.

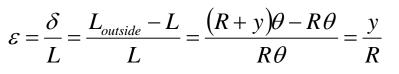
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# Derivation of Stress from Strain

• pure bending = arc shape  $L = R\theta$  $L_{outside} = (R + y)\theta$ °





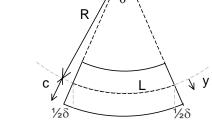
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#### Derivation of Stress

• zero stress at n.a.

$$f = E\varepsilon = \frac{Ey}{R}$$

$$f_{\rm max} = \frac{Ec}{R}$$



 $f = rac{y}{c} f_{\max}$ 

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#### **Bending Moment**

 resultant moment from stresses = bending moment!

 $M = \Sigma f y \Delta A$ 

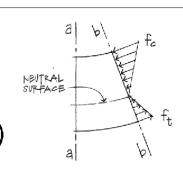


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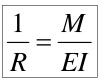
 $= \Sigma \frac{yf_{max}}{y} y \Delta A = \frac{f_{max}}{z} \Sigma y^2 \Delta A = \frac{f_{max}}{I} I = f_{max} S$ С С

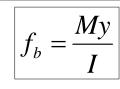
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#### **Bending Stress Relations**





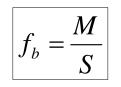


curvature

general bending stress

section modulus

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maximum bending stress

 $S_{required}$ 

required section modulus for design

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