Architectural Structures I: Statics and Strength of Materials

ENDS 231

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five five





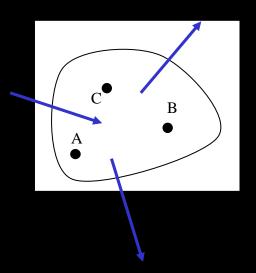
Equilibrium

- rigid body
 - doesn't deform
 - coplanar force systems
- static:

$$R_x = \sum F_x = 0$$

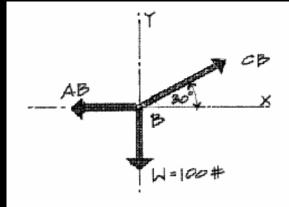
$$R_{y} = \sum F_{y} = 0$$

$$M = \sum M = 0$$



Free Body Diagram

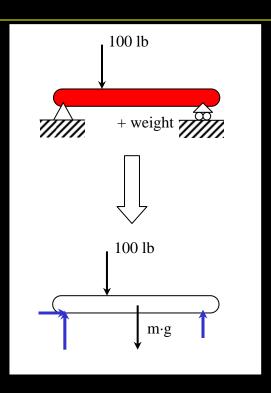
- FBD (sketch)
- tool to see all forces on a body or a point including
 - external forces
 - weights
 - force reactions
 - external moments
 - moment reactions
 - internal forces



(Example 1)

Free Body Diagram

- determine body
- FREE it from:
 - ground
 - supports & connections
- draw all external forces acting ON the body
 - reactions
 - applied forces
 - gravity

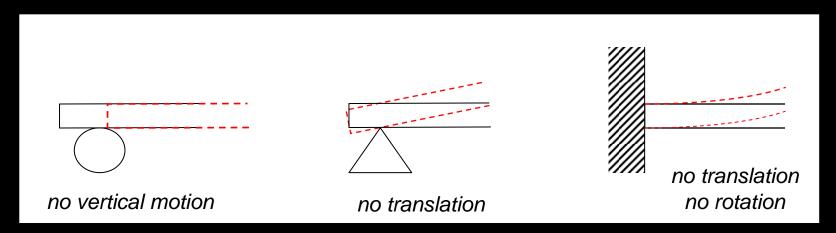


Free Body Diagram

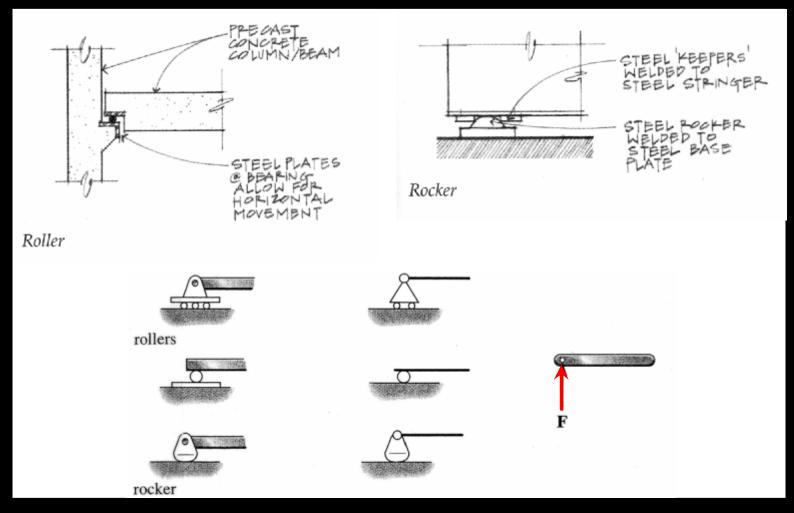
- include relevant geometry
 - guidelines helpful to see moment arms
- name and/or color the unknown
 - forces
 - moments
 - angles
- solve up to 3 equations

Reactions

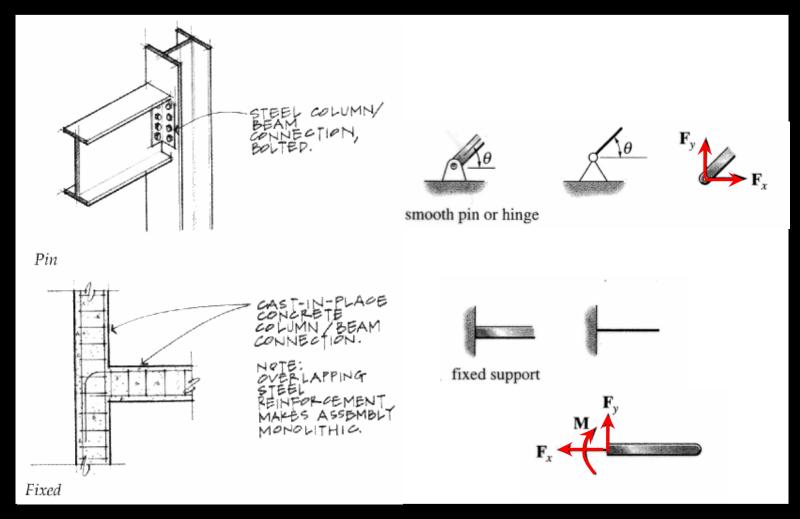
- result of applying force
- unknown size
- connection or support type
 - known direction
 - related to motion prevented



Supports and Connections



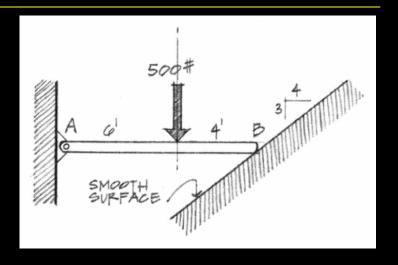
Supports and Connections

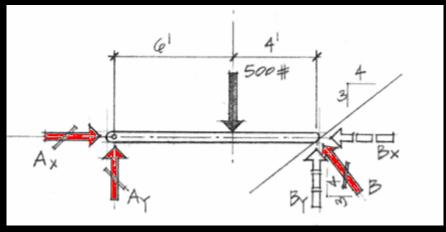


FBD Example

- 500 lb known
- $pin A_x, A_y$
- smooth surface –
 B at 4:3
- 3 equations
- sum moments at
 - -A?
 - -B?

 (B_{x})





Moment Equations

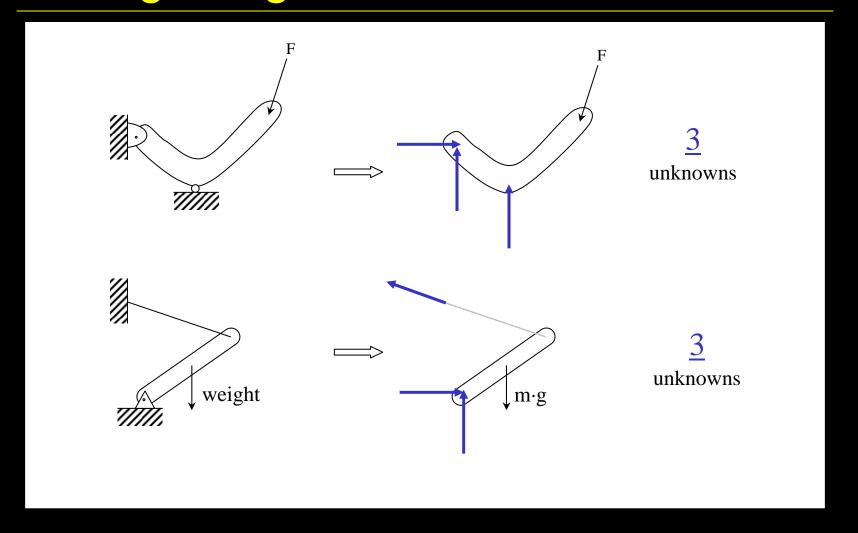
- sum moments at intersection where the most forces intersect
- multiple moment equations may not be useful
- combos:

$$\sum F_{x} = 0 \qquad \sum F = 0 \qquad \sum M_{1} = 0$$

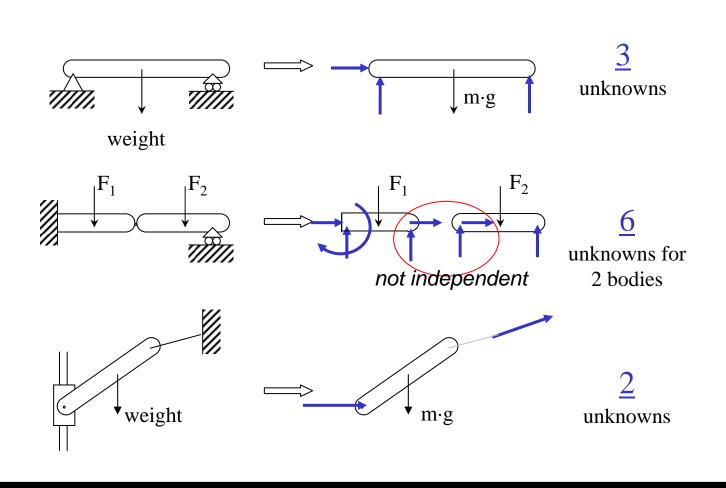
$$\sum F_{y} = 0 \qquad \sum M_{1} = 0 \qquad \sum M_{2} = 0$$

$$\sum M_{1} = 0 \qquad \sum M_{2} = 0 \qquad \sum M_{3} = 0$$

Recognizing Reactions

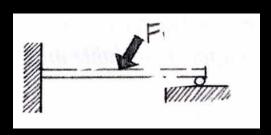


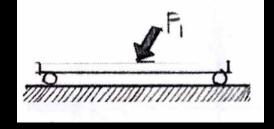
Recognizing Reactions

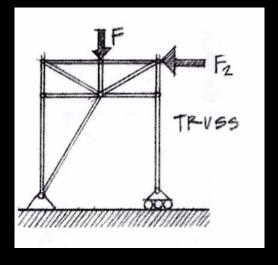


Constraints

- completely constrained
 - doesn't move
 - may not be statically determinate
- improperly or partially constrained
 - has ≤ unknowns
 - can't solve

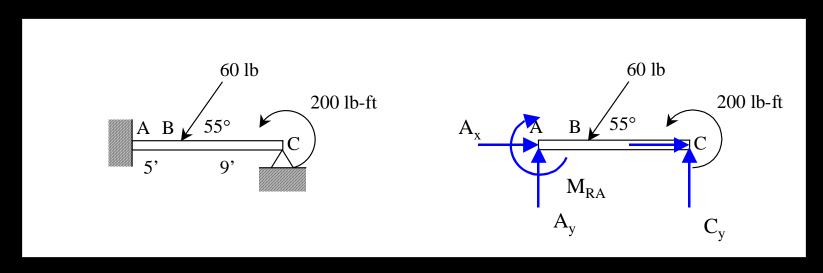




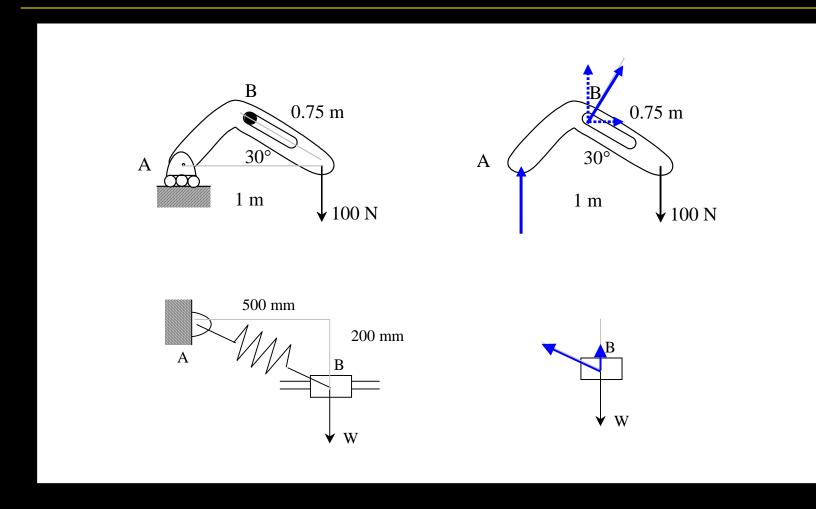


Constraints

- overconstrained
 - won't move
 - can't be solved with statics
 - statically indeterminate to nth degree

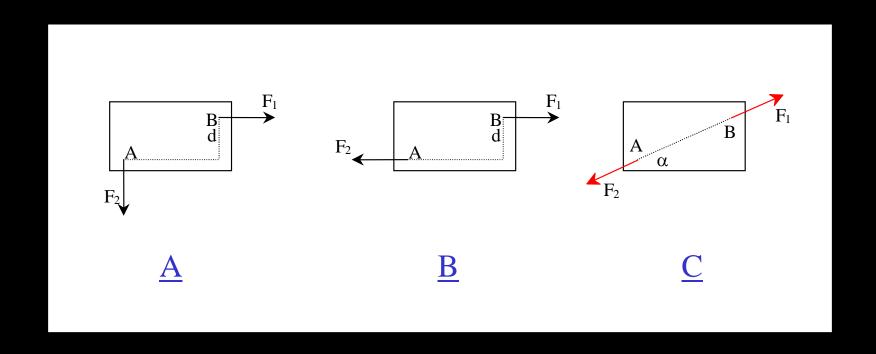


Partial Constraints



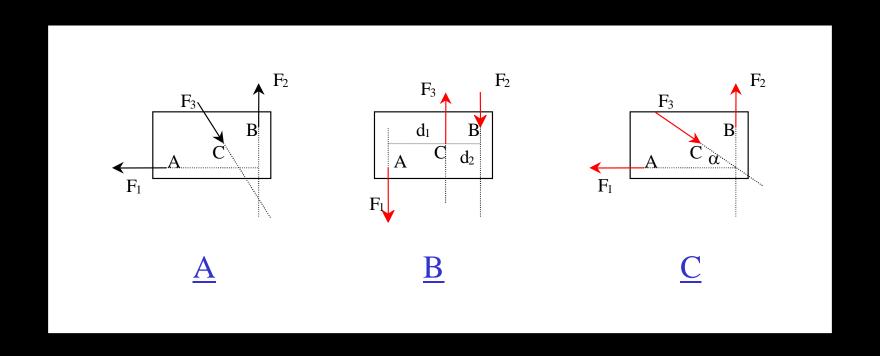
Two Force Rigid Bodies

- equilibrium:
 - forces in line, equal and opposite



Three Force Rigid Bodies

- equilibrium:
 - concurrent or parallel forces



Cable Reactions

- equilibrium:
 - more reactions (4) than equations
 - but, we have slope relationships
 - x component the same everywhere

