ARCHITECTURAL STRUCTURES I:

STATICS AND STRENGTH OF MATERIALS

ENDS 231

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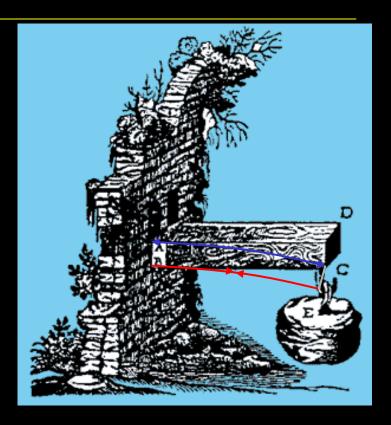
eighteen

beams: bending and shear



Beam Bending

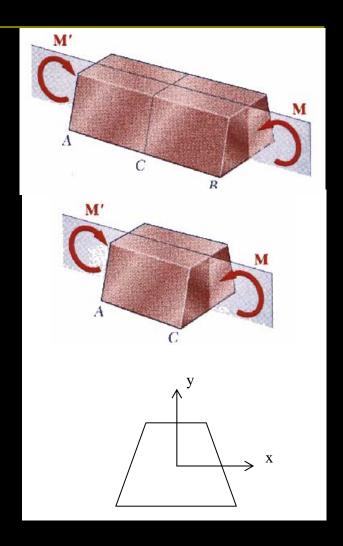
- Galileo
 - relationship between
 stress and depth²
- can see
 - top squishing
 - bottom stretching



what are the stress across the section?

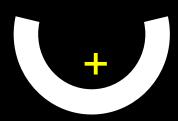
Pure Bending

- bending only
- no shear
- axial normal stresses from bending can be found in
 - homogeneous materials
 - plane of symmetry
 - follow Hooke's law

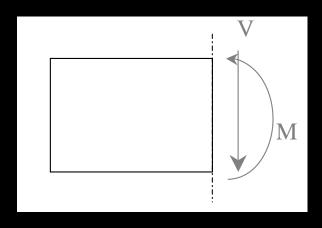


Bending Moments

• sign convention:







• size of maximum internal moment will govern our design of the section

Normal Stresses

- geometric fit
 - plane sectionsremain plane
 - stress varies linearly

Figure 8.5(a) Beam elevation before loading.

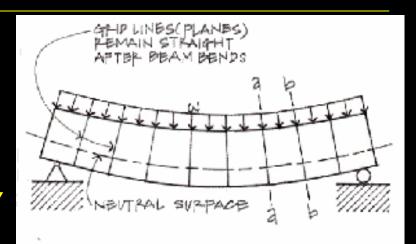
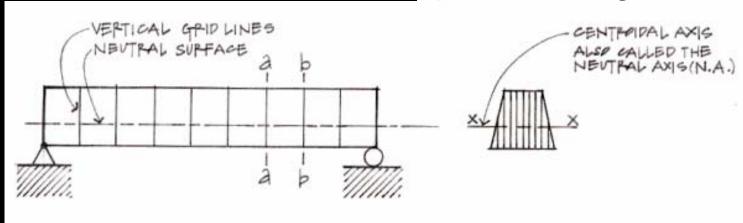


Figure 8.5(b) Beam bending under load.

Beam cross section.



Neutral Axis

stresses vary linearly

 zero stress occurs at the centroid

• <u>neutral axis</u> is line of centroids (n.a.)

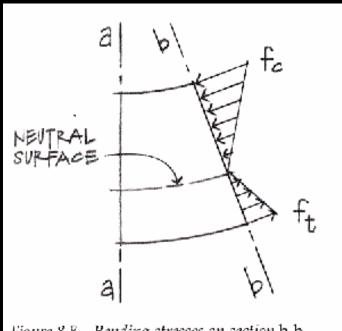


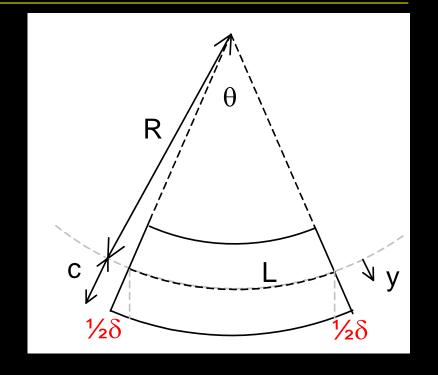
Figure 8.8 Bending stresses on section b-b.

Derivation of Stress from Strain

pure bending = arc shape

$$L = R\theta$$

$$L_{outside} = (R + y)\theta$$



$$\varepsilon = \frac{\delta}{L} = \frac{L_{outside} - L}{L} = \frac{(R + y)\theta - R\theta}{R\theta} = \frac{y}{R}$$

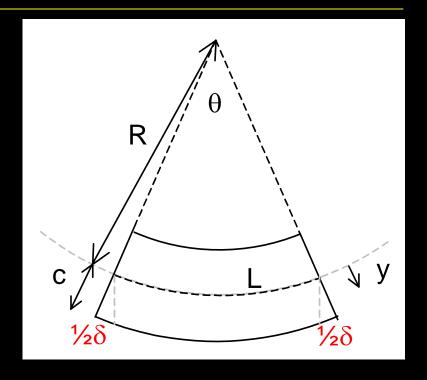
Derivation of Stress

• zero stress at n.a.

$$f = E\varepsilon = \frac{Ey}{R}$$

$$f_{\text{max}} = \frac{Ec}{R}$$

$$f = \frac{y}{c} f_{\text{max}}$$



Bending Moment

resultant moment from stresses = bending moment!

$$M = \sum f y \Delta A$$

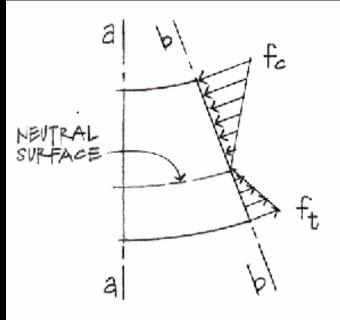


Figure 8.8 Bending stresses on section b-b.

$$= \sum \frac{yf_{max}}{c} y \Delta A = \frac{f_{max}}{c} \sum y^2 \Delta A = \frac{f_{max}}{c} I = f_{max} S$$

Bending Stress Relations

$$\frac{1}{R} = \frac{M}{EI}$$

$$f_b = \frac{My}{I}$$

$$S = \frac{I}{c}$$

curvature

general bending stress

section modulus

$$f_b = \frac{M}{S}$$

$$S_{required} \ge \frac{M}{F_b}$$

required section modulus for design