

Reference Formulas

$\sum F_x = 0$	$C^2 = A^2 + B^2 - 2AB\cos\gamma$	$\hat{x} = \frac{\Sigma \bar{x}A}{\Sigma A}$
$\sum F_y = 0$	$\frac{A}{\sin\alpha} = \frac{B}{\sin\beta} = \frac{C}{\sin\gamma}$	$Q_y = \bar{x}A = \sum_{i=1}^n \bar{x}_i A_i$
$\sum M = 0$	$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$	$\hat{y} = \frac{\Sigma \bar{y}A}{\Sigma A}$
$F_x = F \cos\theta$	$p = 2\pi r = \pi d$	$Q_x = \bar{y}A = \sum_{i=1}^n \bar{y}_i A_i$
$F_y = F \sin\theta$	$A = W \cdot l = t \cdot d$	$I = \bar{I} + Ad^2$
$F = \sqrt{F_x^2 + F_y^2}$	$A = \pi r^2 = \frac{\pi d^2}{4}$	$I = \Sigma I_c + \Sigma Ad^2$
$\tan\theta = \frac{F_y}{F_x}$	$M = Fd$	$r = \sqrt{\frac{I}{A}}$
$g = 9.81 \text{ m/s}^2$	$F = mg$	$S = \frac{I}{c}$
$\frac{dV}{dx} = -w$	$y = mx + b$	$J = \frac{\pi C^4}{2}$
$\frac{dM}{dx} = V$	$m = \frac{y_2 - y_1}{x_2 - x_1}$	$J = \frac{\pi(C_o^4 - C_i^4)}{2}$
$Pa = \text{N/m}^2$	$N = \text{kg} \cdot \text{m/s}^2$	$\pi(\text{radians}) = 180^\circ$
$1 \text{ kPa} = 1,000 \text{ Pa}$	$\text{psi} = \text{lb/in}^2$	$\text{ksi} = \text{kip/in}^2$
$1 \text{ kPa} = 1 \text{ kN/m}^2$	$1 \text{ kip} = 1000 \text{ lb}$	$12 \text{ in} = 1 \text{ ft}$
$1 \text{ MPa} = 10^6 \text{ Pa}$	$1 \text{ GPa} = 10^9 \text{ Pa}$	$1 \text{ m} = 1000 \text{ mm}$
$f_c = \frac{P}{A}$	$F.S = \frac{\text{ultimate}}{\text{allowable}}$	$\varepsilon = \frac{\delta}{L}$
$f_t = \frac{P}{A}$	$f_v = \frac{P}{A}$	$f_v = \frac{P}{2A}$
$f_p = \frac{P}{A}$	$\tau = \frac{T\rho}{J}$	$f_p = \frac{P}{A} = \frac{P}{td}$
$f_y = \frac{My}{I}$	$f_{v\text{-ave}} = \frac{VQ}{Ib}$	$f = E\varepsilon$
$f_{b\text{-max}} = \frac{Mc}{I} = \frac{M}{S}$	$f_{v\text{-max}} = \frac{3V}{2A}$ for a rectangle	$\delta = \frac{PL}{AE}$
$S_{req} \geq \frac{M}{F_b}$	$f_{v\text{-max}} \cong \frac{V}{A_{web}} = \frac{V}{t_w d}$ for an I beam	$\delta_T = \alpha(\Delta T)L$
$V_{longitudinal} = \frac{V_T Q}{I} \Delta x$	$\varepsilon_y = \varepsilon_z = -\frac{\mu f_x}{E}$	$\varepsilon_T = \alpha(\Delta T)$

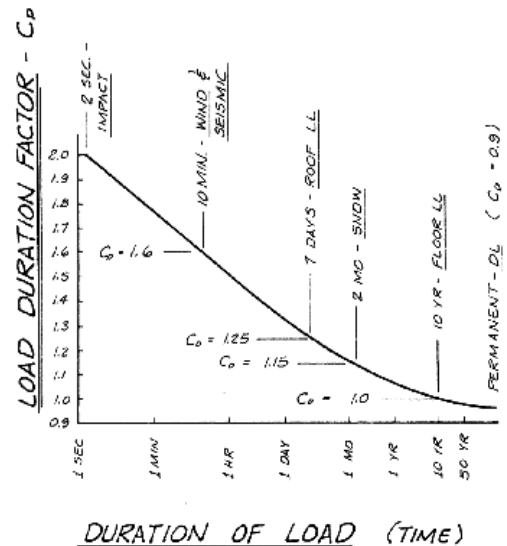
$nF_{connector} \geq \frac{VQ_{connected\ area}}{I} \cdot p$	$f_v = \tau = G \cdot \frac{\rho\phi}{L}$	$\gamma = \frac{\rho\phi}{L}$
$\tau_{max} = \frac{T}{c_1 ab^2}$	$\phi = \frac{TL}{c_2 ab^3 G}$	$\phi = \frac{TL}{JG}$
$\tau_{max} = \frac{T}{\frac{1}{3} ab^2}$	$\phi = \frac{TL}{\frac{1}{3} ab^3 G}$	$\tau_{max} = \frac{Tt_{max}}{\frac{1}{3} \Sigma b_i t_i^3}$
$\tau_{max} = \frac{T}{2t\mathcal{A}}$	$\phi = \frac{TL}{4t\mathcal{A}^2} \sum_i \frac{s_i}{t_i}$	$\phi = \frac{TL}{\frac{1}{3} G \Sigma b_i t_i^3}$
$\frac{1}{\rho} = \frac{M}{EI} = \frac{1}{R}$	$\Delta = \iint \frac{M(x)}{EI} dx$	$2n = b + 3$
$P_U = P_L \gamma_L + P_D \gamma_D \leq \phi P_n$	AISC-LRFD: $P_U : 1.4D$	$M_u \leq \phi_b M_n = 0.9 F_y Z$
$L_e = Kl$	$P_U : 1.2D + 1.6L + 0.5(Lr\ or\ S\ or\ R)$	$M_{ult} = M_p = f_y \Sigma A_i y_i = f_y Z$
$P_{cr} = \frac{\pi^2 EI}{(L_e)^2} = \frac{\pi^2 EA}{\left(L_e/r\right)^2}$	$P_U : 1.2D + 1.6(Lr\ or\ S\ or\ R) + (0.5L\ or\ 0.8W)$	$k = Z/S$ $Z = \frac{M_p}{f_y}$
$f_{cr} = \frac{\pi^2 E}{\left(L_e/r\right)^2}$	$P_U : 1.2D + 1.3W + 0.5L + 0.5(Lr\ or\ S\ or\ R)$	$P_u \leq \phi_c F_{cr} A_g$ $\phi_c = 0.85$
	$V_u \leq \phi_v (0.6 F_{yw} A_w)$ $\phi_v = 0.9$	$\lambda_c = \frac{Kl}{r\pi} \sqrt{\frac{F_y}{E}}$
Wood: $F' = C_D C_M C_F \dots \times F_{tabulated}$	$\lambda_c \leq 1.5$	$F_{cr} = (0.658^{\lambda_c^2}) F_y$
$F'_c = F_c^* C_p = (F_c C_D) C_p$	$\lambda_c > 1.5$	$F_{cr} = \left[\frac{0.877}{\lambda_c^2} \right] F_y$
$F_{cE} = \frac{K_{cE} E}{\left(l_e/d\right)^2}$ $K_{cE} = 0.3\ \text{sawn}, 0.418\ \text{glulam}$	$\frac{P_u}{\phi_c P_n} \geq 0.2 :$	$\frac{P_u}{\phi_c P_n} + \frac{8}{9} \left(\frac{M_{ux}}{\phi_b M_{nx}} + \frac{M_{uy}}{\phi_b M_{ny}} \right) \leq 1.0$
$\left[\frac{f_c}{F'_c} \right]^2 + \frac{f_{bx}}{F'_{bx} \left[1 - \frac{f_c}{F_{cEx}} \right]} \leq 1.0$	$\frac{P_u}{\phi_c P_n} < 0.2 :$	$\frac{P_u}{2\phi_c P_n} + \left(\frac{M_{ux}}{\phi_b M_{nx}} + \frac{M_{uy}}{\phi_b M_{ny}} \right) \leq 1.0$
$f_{max} = \frac{P}{A} + \frac{Mc}{I}$	$P_u \leq \phi_t F_y A_g$ $\phi_t = 0.9$	$P_u \leq \phi_t F_u A_e$ $\phi_t = 0.75$
$\frac{f_a}{F_a} + \frac{f_b}{F_b} \leq 1.0$	$f_{max} = \frac{P}{A} + \frac{M_1 y}{I} + \frac{M_2 z}{I}$	$\frac{f_a}{F_a} + \frac{f_{bx}}{F_{bx}} + \frac{f_{by}}{F_{by}} \leq 1.0$

AISC – ASD:		$\frac{l_e}{r} \geq C_c$	$F_a = \frac{f_{critical}}{F.S.} = \frac{12\pi^2 E}{23(Kl/r)^2}$
$C_m = 0.6 - 0.4\left(\frac{M_1}{M_2}\right)$		$\frac{l_e}{r} < C_c$	$F_a = \left[1 - \frac{(Kl/r)^2}{2C_c^2}\right] \frac{F_y}{F.S.}$
$F_b = 0.66F_y$ (braced)	$F.S. = \frac{5}{3} + \frac{3}{8} \cdot \frac{L_e/r}{C_c} - \frac{1}{8} \cdot \left(\frac{L_e/r}{C_c}\right)^3$		
$F_b = 0.60F_y$ (unbraced)			
$F_v = 0.40F_y$			
$F_v = 0.30F_{weld}$			
$F_t = 0.60F_y$ (gross)	$\frac{f_a}{F_a} + \frac{C_{mx}f_{bx}}{\left(1 - \frac{f_a}{F'_{ex}}\right)F_{bx}} + \frac{C_{my}f_{by}}{\left(1 - \frac{f_a}{F'_{ey}}\right)F_{by}} \leq 1.0$		
$F_t = 0.5F_u$ (net)			
$F_t = 0.45F_y$ (pinned)			
$F_t = 0.33F_u$ (threaded)			

Reference Diagrams

Buckled shape of column shown by dashed line	(a)	(b)	(c)	(d)	(e)	(f)
Theoretical K value	0.5	0.7	1.0	1.0	2.0	2.0
Recommended design values when ideal conditions are approximated	0.65	0.80	1.0	1.2	2.10	2.0
End conditions code	<ul style="list-style-type: none"> Rotation fixed, Translation fixed Rotation free, Translation fixed Rotation fixed, Translation free Rotation free, Translation free 					

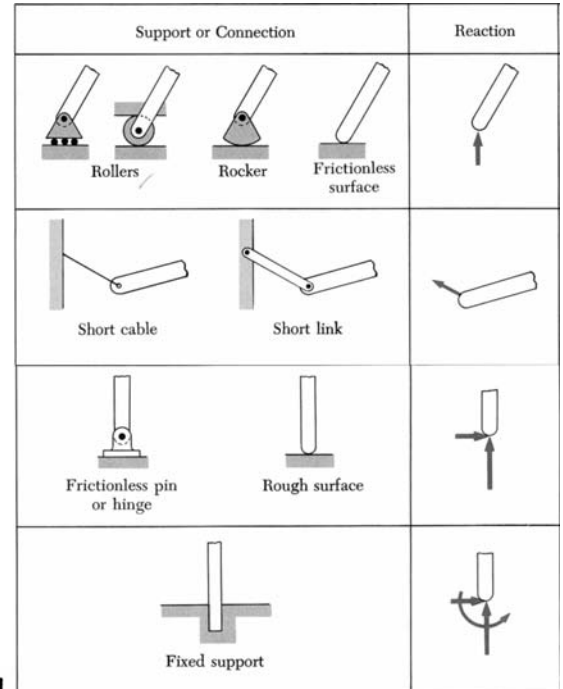
Allowable Strength of Fillet Welds per inch of weld		
Weld Size (in.)	E60XX (k/in.)	E70XX (k/in.)
3/16	2.39	2.78
1/4	3.18	3.71
5/16	3.98	4.64
3/8	4.77	5.57
7/16	5.57	6.94
1/2	6.36	7.42
5/8	7.95	9.27
3/4	9.55	11.13



Reference Diagrams

BOLTS, THREADED PARTS AND RIVETS
Allowable Shear in kips

TABLE SHEAR												
ASTM Designation	Connection Type ^a	Hole Type ^b	F _v ksi	Loading ^c	Nominal Diameter d, in.							
					5/8	3/4	7/8	1	1 1/8	1 1/4	1 3/8	1 1/2
					Area (Based on Nominal Diameter) in. ²							
					.3068	.4418	.6013	.7854	.9940	1.227	1.485	1.767
A307	—	STD	10.0	S	3.1	4.4	6.0	7.9	9.9	12.3	14.8	17.7
		NSL	10.0	D	6.1	8.8	12.0	15.7	19.9	24.5	29.7	35.3
A325	SC ^a Class A	STD	17.0	S	5.22	7.51	10.2	13.4	16.9	20.9	25.2	30.0
		D	17.0	D	10.4	15.0	20.4	26.7	33.8	41.7	50.5	60.1
		OVS, SSL	15.0	S	4.60	6.63	9.02	11.8	14.9	18.4	22.3	26.5
		D	15.0	D	9.20	13.3	18.0	23.6	29.8	36.8	44.6	53.0
	LSL	12.0	S	3.68	5.30	7.22	9.42	11.9	14.7	17.8	21.2	
	D	12.0	D	7.36	10.6	14.4	18.8	23.9	29.4	35.6	42.4	
N	STD, NSL	21.0	S	6.4	9.3	12.6	16.5	20.9	25.8	31.2	37.1	
		D	21.0	D	12.9	18.6	25.3	33.0	41.7	51.5	62.4	
X	STD, NSL	30.0	S	9.2	13.3	18.0	23.6	29.8	36.8	44.5	53.0	
		D	30.0	D	18.4	26.5	36.1	47.1	59.6	73.6	89.1	



BOLTS, AND THREADED PARTS
Allowable Bearing load in kips

TABLE BEARING Slip-critical and Bearing-type Connections												
Material Thickness	F _v = 58 ksi Bolt dia.			F _v = 65 ksi Bolt dia.			F _v = 70 ksi Bolt dia.			F _v = 100 ksi Bolt dia.		
	3/4	7/8	1	3/4	7/8	1	3/4	7/8	1	3/4	7/8	1
	1/8	6.5	7.6	8.7	7.3	8.5	9.8	7.9	9.2	10.5	11.3	13.1
3/16	9.8	11.4	13.1	11.0	12.8	14.6	11.8	13.8	15.8	16.9	19.7	22.5
1/4	13.1	15.2	17.4	14.6	17.1	19.5	15.8	18.4	21.0	22.5	26.3	30.0
5/16	16.3	19.0	21.8	18.3	21.3	24.4	19.7	23.0	26.3	28.1	32.8	37.5
3/8	19.6	22.8	26.1	21.9	25.6	29.3	23.6	27.6	31.5	33.8	39.4	45.0
7/16	22.8	26.6	30.5	25.6	29.9	34.1	27.6	32.2	36.8	45.9	52.5	60.0
1/2	26.1	30.5	34.8	29.3	34.1	39.0	31.5	36.8	42.0	60.0		
9/16	29.4	34.3	39.2	32.9	38.4	43.9		41.3	47.3			
5/8	32.6	38.1	43.5		42.7	48.8		45.9	52.5			
1 1/16		41.9	47.9		46.9	53.6			57.8			
3/4		45.7	52.2			58.5						
1 3/16			56.6									
7/8			60.9									
1 5/16												
1	52.2	60.9	69.6	58.5	68.3	78.0	63.0	73.5	84.0	90.0	105.0	120.0

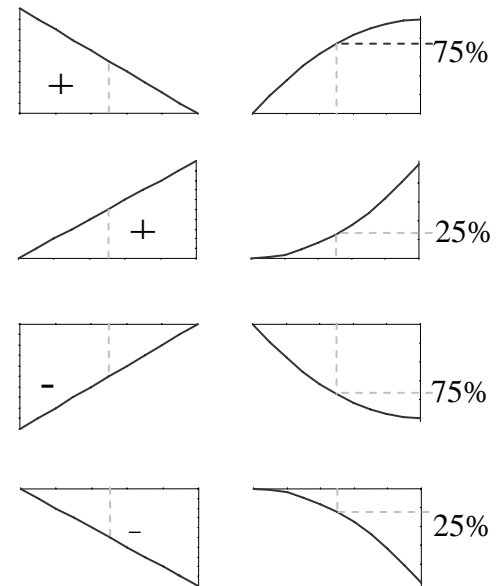


TABLE 3.1. Coefficients for Rectangular Bars in Torsion

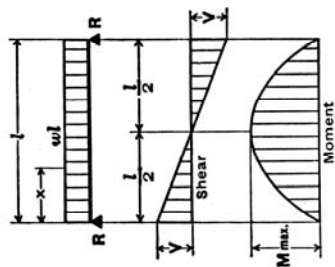
a/b	c ₁	c ₂
1.0	0.208	0.1406
1.2	0.219	0.1661
1.5	0.231	0.1958
2.0	0.246	0.229
2.5	0.258	0.249
3.0	0.267	0.263
4.0	0.282	0.281
5.0	0.291	0.291
10.0	0.312	0.312
∞	0.333	0.333

Reference Geometry

Shape	Drawing	\bar{x}	\bar{y}	Area	Moment of Inertia (I_x)
Rectangle		$b/2$	$h/2$	bh	$I_x = \frac{bh^3}{12}$
Triangle		$b/3$	$h/3$	$bh/2$	$I_x = \frac{bh^3}{36}$
Circle		0	0	πr^2	$I_x = \frac{\pi r^4}{4} = \frac{\pi d^4}{64}$
Hollow Circle		0	0	$\frac{\pi(D^2 - d^2)}{4}$	$I_x = \frac{\pi(D^4 - d^4)}{64}$
Semicircle		0	$4r/3\pi$	$\pi r^2/2$	$I_x = I_y = \frac{\pi r^4}{8}$
Quarter Circle		$4r/3\pi$	$4r/3\pi$	$\pi r^2/4$	$I_x = I_y = \frac{\pi r^4}{16}$
Parabolic Segment		$5b/8$	$2h/5$	$2bh/3$	$I_x = \frac{8h^3b}{175}$
Complement of a Parabolic Segment		$3b/4$	$3h/10$	$bh/3$	$I_x = \frac{37h^3b}{2100}$

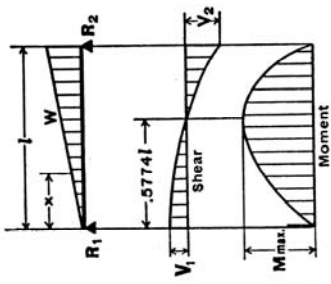
Reference Beam Diagrams

1. SIMPLE BEAM—UNIFORMLY DISTRIBUTED LOAD



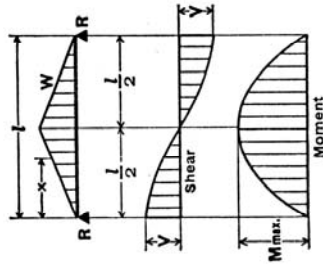
Total Equiv. Uniform Load = wl
 $R = V$ = $\frac{wl}{2}$
 V_x = $w\left(\frac{l}{2} - x\right)$
 M max. (at center) = $\frac{wl^2}{8}$
 M_x = $\frac{wx}{2}(l-x)$
 Δ max. (at center) = $\frac{5wl^4}{384EI}$
 Δ_x = $\frac{wx}{24EI}(l^3 - 2lx^2 + x^3)$

2. SIMPLE BEAM—LOAD INCREASING UNIFORMLY TO ONE END



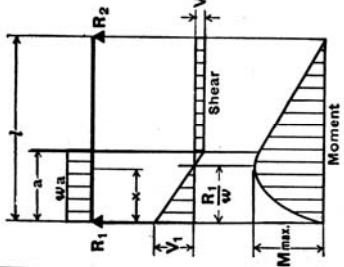
Total Equiv. Uniform Load = $\frac{16W}{9\sqrt{3}} = 1.0264W$
 $R_1 = V_1$ = $\frac{W}{3}$
 $R_2 = V_2$ max. = $\frac{2W}{3}$
 V_x = $\frac{W}{3} - \frac{Wx^2}{l^2}$
 M max. (at $x = \frac{l}{\sqrt{3}} = .5774l$) = $\frac{2Wl}{9\sqrt{3}} = .1283Wl$
 M_x = $\frac{Wx}{3l^2}(l^2 - x^2)$
 Δ max. (at $x = l\sqrt{\frac{8}{15}} = .5193l$) = $\frac{Wl^3}{.01304EI}$
 Δ_x = $\frac{Wx}{180EI^2}(3x^4 - 10l^2x^2 + 7l^4)$

3. SIMPLE BEAM—LOAD INCREASING UNIFORMLY TO CENTER



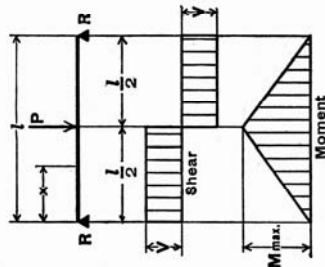
Total Equiv. Uniform Load = $\frac{4W}{3}$
 $R = V$ = $\frac{W}{2}$
 V_x (when $x < \frac{l}{2}$) = $\frac{W}{2l^2}(l^2 - 4x^2)$
 M max. (at center) = $\frac{Wl}{6}$
 M_x (when $x < \frac{l}{2}$) = $Wx\left(\frac{l}{2} - \frac{2x^2}{3l}\right)$
 Δ max. (at center) = $\frac{Wl^3}{60EI}$
 Δ_x (when $x < \frac{l}{2}$) = $\frac{Wx}{480EI^2}(5l^3 - 4x^3)^2$

5. SIMPLE BEAM—UNIFORM LOAD PARTIALLY DISTRIBUTED AT ONE END



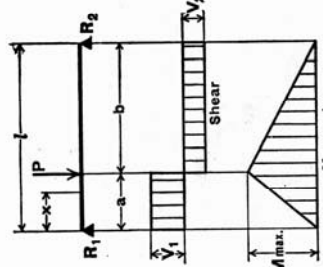
$R_1 = V_1$ max. = $\frac{wa}{2l}(2l-a)$
 $R_2 = V_2$ = $\frac{wa^2}{2l}$
 V_x (when $x < a$) = $R_1 - wx$
 M max. (at $x = \frac{R_1}{w}$) = $\frac{R_1^2}{2w}$
 M_x (when $x < a$) = $R_1x - \frac{wx^2}{2}$
 M_x (when $x > a$) = $R_2(l-x)$
 Δ_x (when $x < a$) = $\frac{wx}{24EI}(a^2(2l-a)^2 - 2ax^2(2l-a) + lx^3)$
 Δ_x (when $x > a$) = $\frac{wa^2(l-x)}{24EI}(4xl - 2x^2 - a^2)$

7. SIMPLE BEAM—CONCENTRATED LOAD AT CENTER



Total Equiv. Uniform Load = $2P$
 $R = V$ = $\frac{P}{2}$
 M max. (at point of load) = $\frac{Pl}{4}$
 M_x (when $x < \frac{l}{2}$) = $\frac{Px}{2}$
 Δ max. (at point of load) = $\frac{Pl^3}{48EI}$
 Δ_x (when $x < \frac{l}{2}$) = $\frac{Px}{48EI}(3l^2 - 4x^2)$

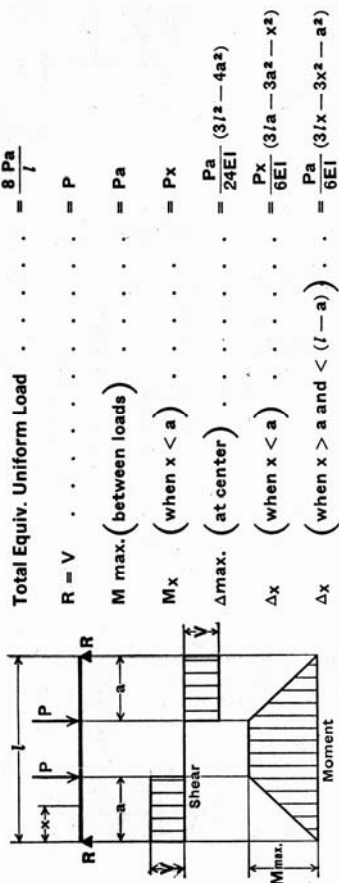
8. SIMPLE BEAM—CONCENTRATED LOAD AT ANY POINT



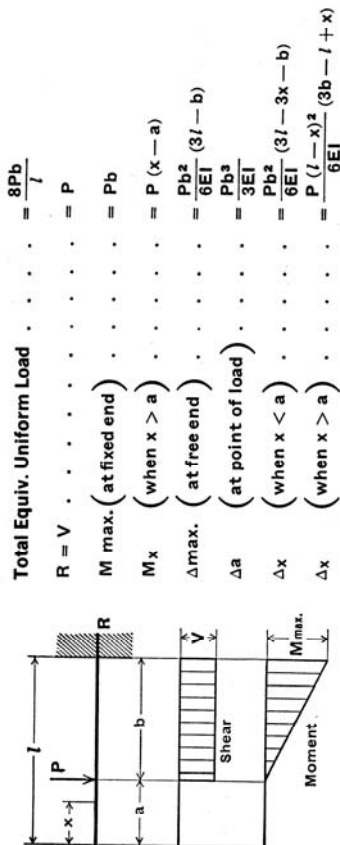
Total Equiv. Uniform Load = $\frac{8Pab}{l^2}$
 $R_1 = V_1$ (max. when $a < b$) = $\frac{Pb}{l}$
 $R_2 = V_2$ (max. when $a > b$) = $\frac{Pa}{l}$
 M max. (at point of load) = $\frac{Pab}{l}$
 M_x (when $x < a$) = $\frac{Pbx}{l}$
 Δ max. (at $x = \sqrt{\frac{a(a+2b)}{3}}$ when $a > b$) = $\frac{Pab(a+2b)\sqrt{3a(a+2b)}}{27EI l}$
 Δ_a (at point of load) = $\frac{Pab^2}{3EI l}$
 Δ_x (when $x < a$) = $\frac{Pbx}{6EI l}(l^2 - bx^2 - x^2)$

Reference Beam Diagrams

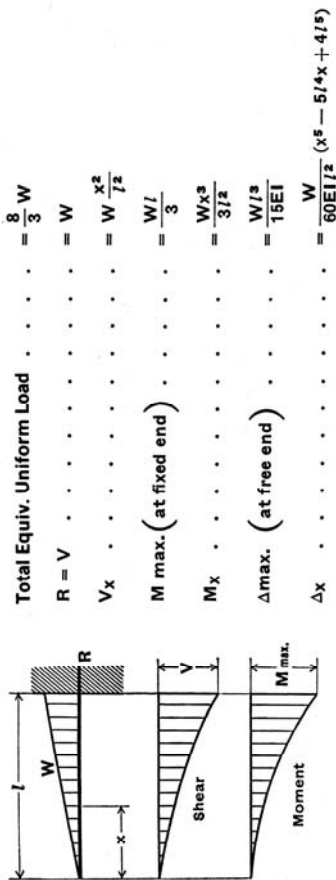
9. SIMPLE BEAM—TWO EQUAL CONCENTRATED LOADS SYMMETRICALLY PLACED



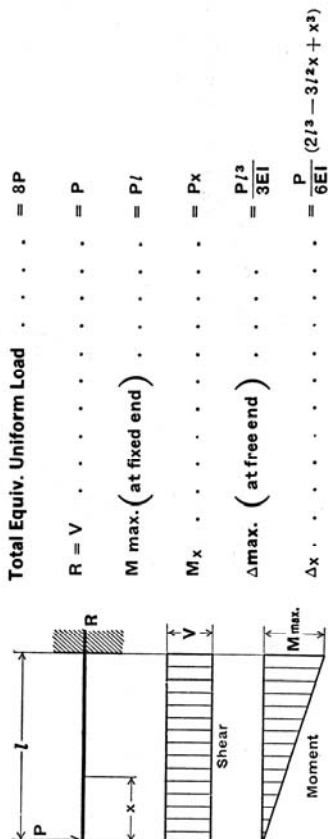
21. CANTILEVER BEAM—CONCENTRATED LOAD AT ANY POINT



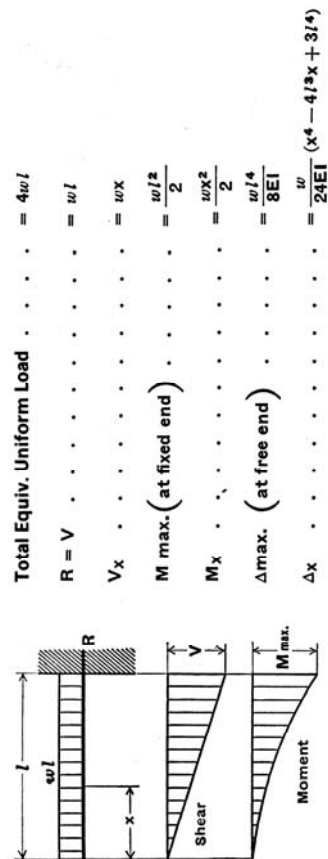
18. CANTILEVER BEAM—LOAD INCREASING UNIFORMLY TO FIXED END



22. CANTILEVER BEAM—CONCENTRATED LOAD AT FREE END



19. CANTILEVER BEAM—UNIFORMLY DISTRIBUTED LOAD



26. BEAM OVERHANGING ONE SUPPORT—CONCENTRATED LOAD AT END OF OVERHANG

$R_1 = V_1 = \frac{Pa}{l}$
 $R_2 = V_1 + V_2 = \frac{P}{l}(l+a)$
 $V_2 = P$
 $M \text{ max. (at } R_2) = Pa$
 $M_x \text{ (between supports) = } \frac{Pa^2x}{l}$
 $M_{x_1} \text{ (for overhang) = } P(a-x_1)$
 $\Delta \text{ max. (between supports at } x = \frac{l}{\sqrt{3}}) = \frac{Pa^2l^2}{9\sqrt{3}EI} = .06415 \frac{Pa^2l^2}{EI}$
 $\Delta \text{ max. (for overhang at } x_1 = a) = \frac{Pa^2}{3EI}(l+a)$
 $\Delta x \text{ (between supports) = } \frac{Pa^2x}{6EI}(l^2-x^2)$
 $\Delta x_1 \text{ (for overhang) = } \frac{Px_1}{6EI}(2al+3ax_1-x_1^2)$

27. BEAM OVERHANGING ONE SUPPORT—UNIFORMLY DISTRIBUTED LOAD BETWEEN SUPPORTS

$\text{Total Equiv. Uniform Load} = wl$
 $R = V = \frac{wl}{2}$
 $V_x = w\left(\frac{l}{2}-x\right)$
 $M \text{ max. (at center) = } \frac{wl^2}{8}$
 $M_x = \frac{wx}{2}(l-x)$
 $\Delta \text{ max. (at center) = } \frac{5wl^4}{384EI}$
 $\Delta x = \frac{wx}{24EI}(l^3-2lx^2+x^3)$
 $\Delta x_1 = \frac{wl^2x_1}{24EI}$

28. BEAM OVERHANGING ONE SUPPORT—CONCENTRATED LOAD AT ANY POINT BETWEEN SUPPORTS

$\text{Total Equiv. Uniform Load} = \frac{8Pab}{l^2}$
 $R_1 = V_1 \text{ (max. when } a < b) = \frac{Pb}{l}$
 $R_2 = V_2 \text{ (max. when } a > b) = \frac{Pa}{l}$
 $M \text{ max. (at point of load) = } \frac{Pab}{l}$
 $M_x \text{ (when } x < a) = \frac{Pbx}{l}$
 $\Delta \text{ max. (at } x = \sqrt{\frac{a(a+2b)}{3}} \text{ when } a > b) = \frac{Pab(a+2b)\sqrt{3a(a+2b)}}{27EI}$
 $\Delta a \text{ (at point of load) = } \frac{Pa^2b^2}{3EI}$
 $\Delta x \text{ (when } x < a) = \frac{Pbx}{6EI}(l^2-b^2-x^2)$
 $\Delta x \text{ (when } x > a) = \frac{Pa}{6EI}(l-x)(2lx-x^2-a^2)$
 $\Delta x_1 = \frac{Pabx_1}{6EI}(l+a)$