ARCHITECTURAL STRUCTURES 1:

STATICS AND STRENGTH OF MATERIALS

ENDS 231

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SPRING 2007

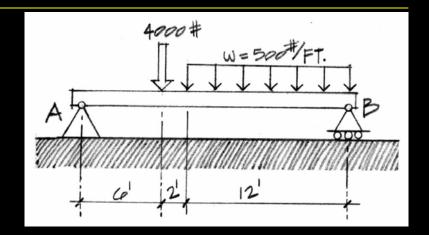
thirteen



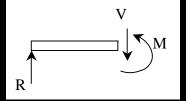
beam forces — internal

Beams

- span horizontally
 - floors
 - bridges
 - roofs



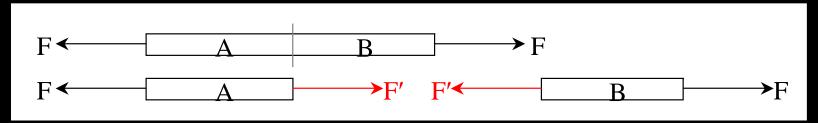
- loaded transversely by gravity loads
- may have internal axial force
- will have internal shear force



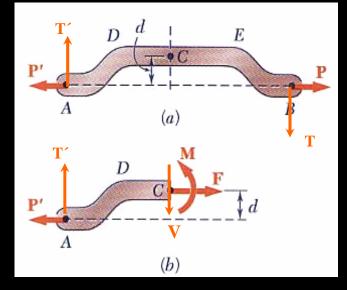
will have internal moment (bending)

Internal Forces

- trusses
 - axial only, (compression & tension)

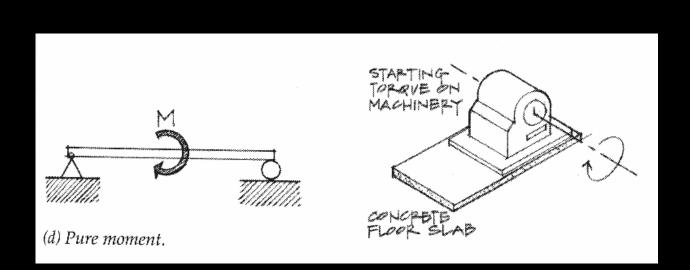


- in general
 - axial force
 - shear force, V
 - bending moment, M



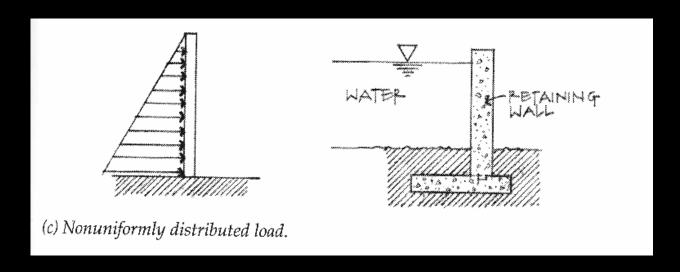
Beam Loading

- concentrated force
- concentrated <u>moment</u>
 - spandrel beams



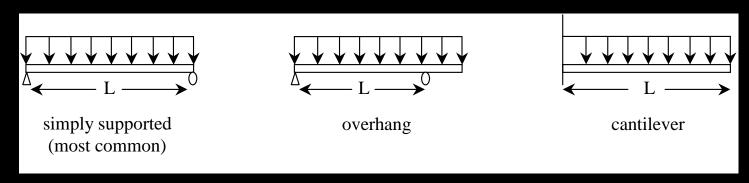
Beam Loading

- uniformly distributed load (line load)
- non-uniformly distributed load
 - hydrostatic pressure
 - wind loads

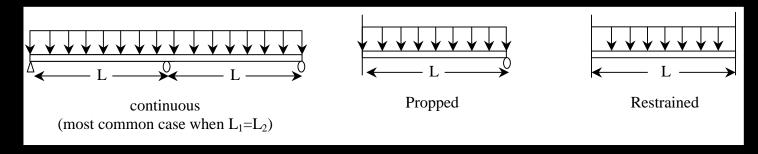


Beam Supports

• statically determinate

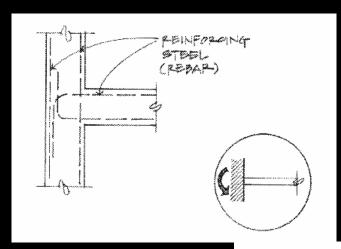


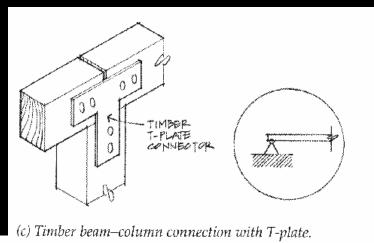
statically indeterminate

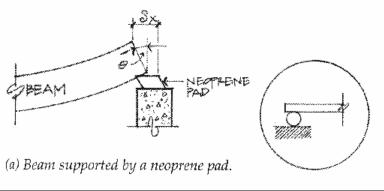


Beam Supports

• in the real world, modeled type

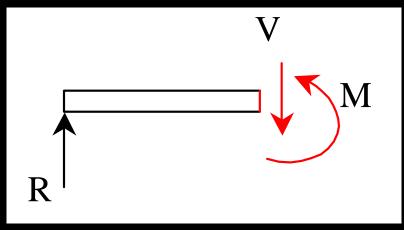






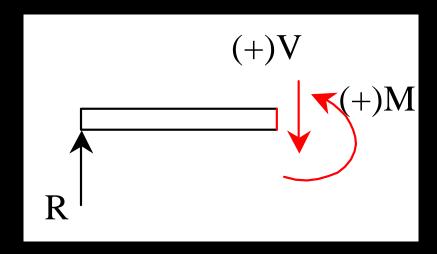
Internal Forces in Beams

- like method of sections / joints
 - no axial forces
- section <u>must</u> be in equilibrium
- want to know where biggest internal forces and moments are for designing



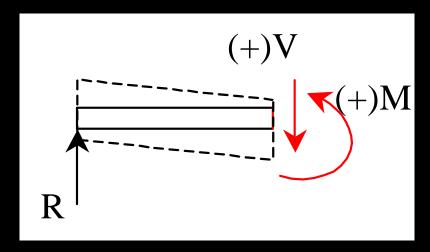
V & M Diagrams

- tool to locate V_{max} and M_{max}
- <u>necessary</u> for designing
- have a <u>different sign convention</u> than external forces, moments, and reactions

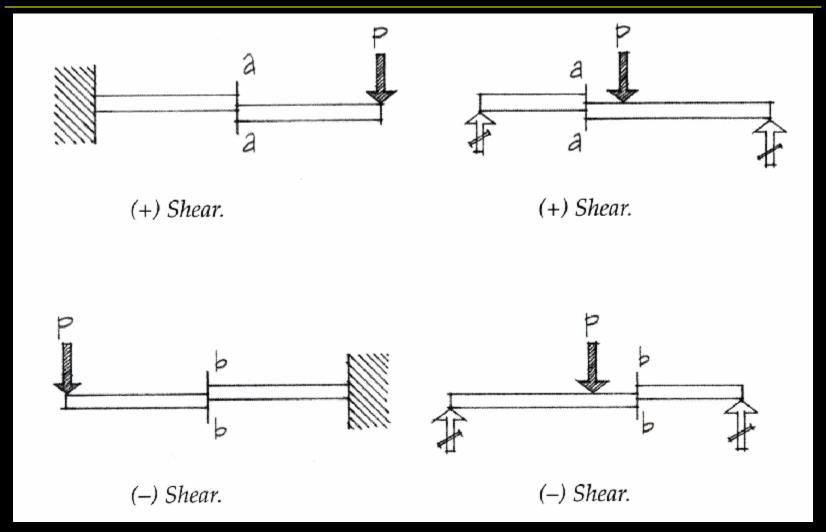


Sign Convention

- shear force, V:
 - cut section to LEFT
 - if $\sum F_y$ is positive by statics, V acts down and is POSITIVE
 - beam has to resist shearing apart by V

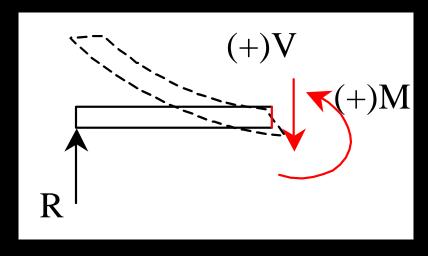


Shear Sign Convention

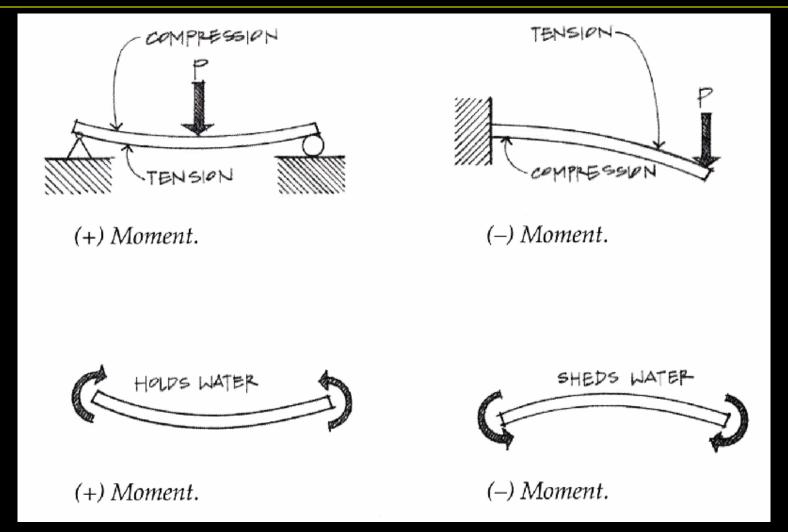


Sign Convention

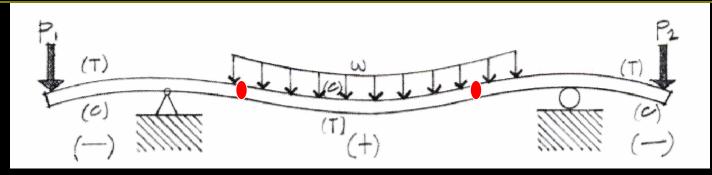
- bending moment, M:
 - cut section to LEFT
 - if ∑M_{cut} is clockwise, M acts ccw and is POSITIVE – flexes into a "smiley" beam has to resist bending apart by M



Bending Moment Sign Convention



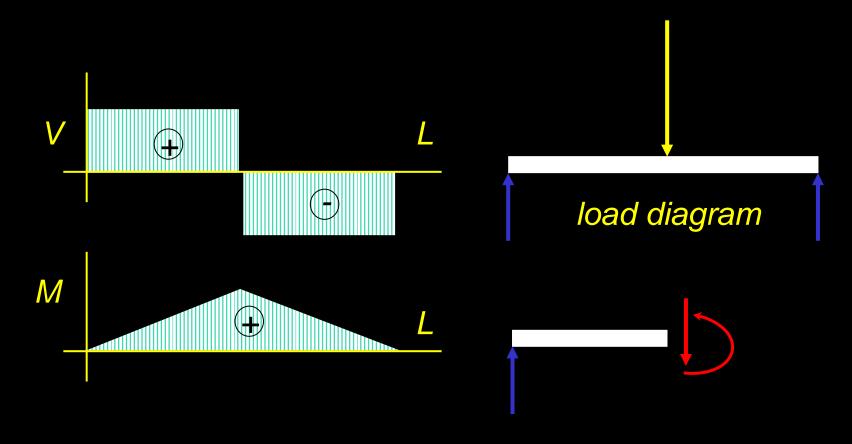
Deflected Shape



- positive bending moment
 - tension in bottom, compression in top
- negative bending moment
 - tension in top, compression in bottom
- zero bending moment
 - inflection point

Constructing V & M Diagrams

• along the beam length, plot V, plot M



Mathematical Method

cut sections with x as width

• write functions of V(x) and M(x)

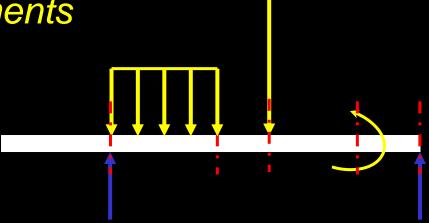
Method 1: Equilibrium

• cut sections at important places

 plot V & M L/2

Method 1: Equilibrium

- important places
 - supports
 - concentrated loads
 - start and end of distributed loads
 - concentrated moments
- free ends
 - zero forces



Method 2: Semigraphical

by knowing

- area under loading curve = change in V
- area under shear curve = change in M
- concentrated forces cause "jump" in V
- concentrated moments cause "jump" in M

$$V_{D} - V_{C} = -\int_{C}^{X_{D}} w dx \qquad M_{D} - M_{C} = \int_{C}^{X_{D}} V dx$$

$$x_{C}$$

Method 2

relationships

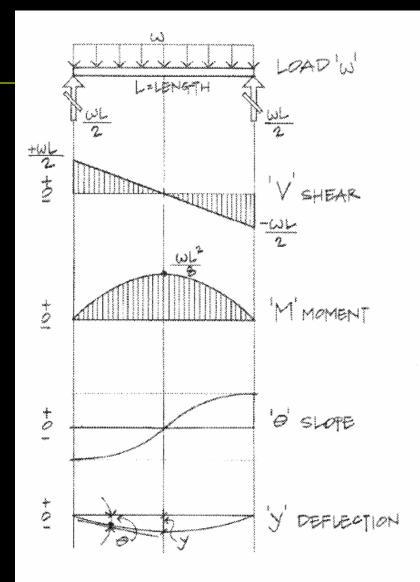
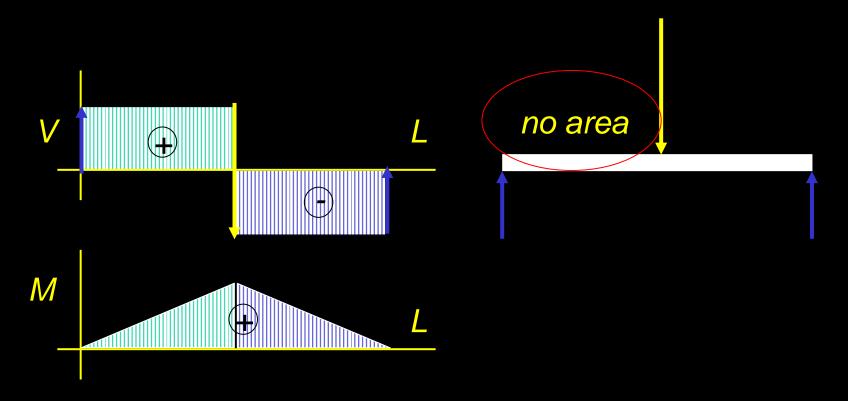


Figure 7.11 Relationship of load, shear, moment, slope, and deflection diagrams.

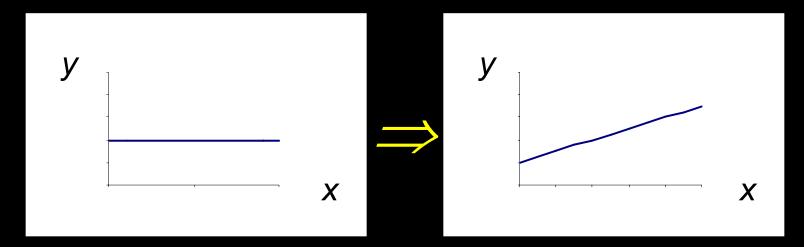
Method 2: Semigraphical

• M_{max} occurs where V = 0 (calculus)



Curve Relationships

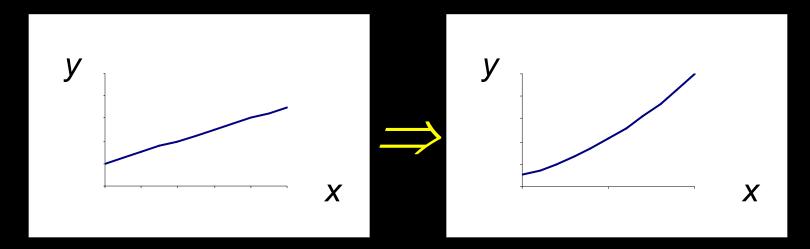
- integration of functions
- line with 0 slope, integrates to sloped



ex: load to shear, shear to moment

Curve Relationships

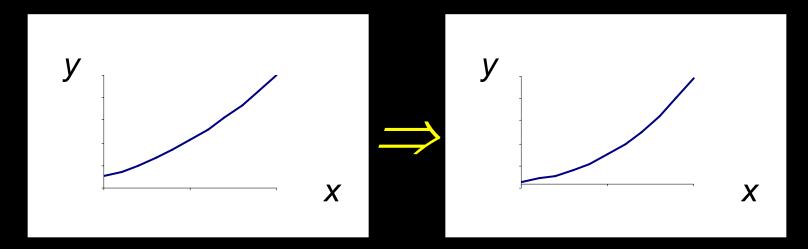
• line with slope, integrates to parabola



• ex: load to shear, shear to moment

Curve Relationships

• parabola, integrates to 3rd order curve



• ex: load to shear, shear to moment

Basic Procedure

1. Find reaction forces & moments

Plot axes, underneath beam load
diagram

V:

- 2. Starting at left
- 3. Shear is 0 at free ends
- 4. Shear jumps with concentrated load
- 5. Shear changes with area under load

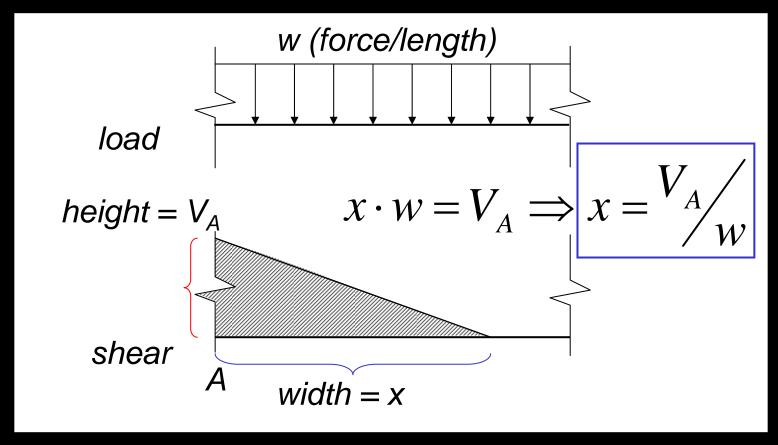
Basic Procedure

M:

- 6. Starting at left
- 7. Moment is 0 at free ends
- 8. Moment jumps with moment
- 9. Moment changes with area under V

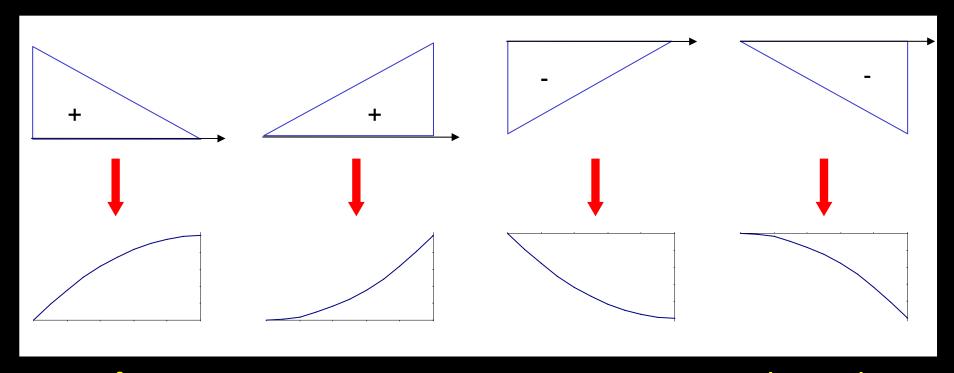
Triangle Geometry

slope of V is w (-w:1)



Parabolic Shapes

cases



up fast, then slow

up slow, then fast down fast, then slow down slow, then fast