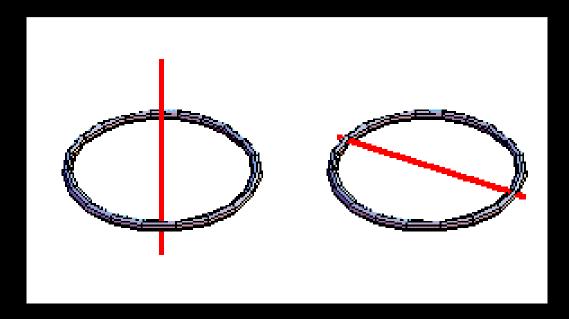
ARCHITECTURAL STRUCTURES I:

STATICS AND STRENGTH OF MATERIALS
ENDS 231

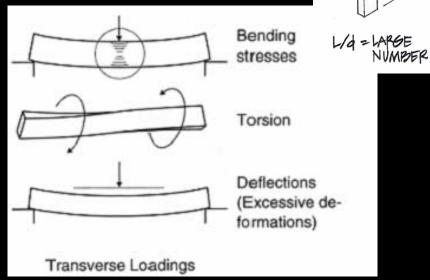
DR. ANNE NICHOLS
SPRING 2007
lecture
tWelve



moment of inertia of an area

Moments of Inertia

- 2nd moment area
 - math concept
 - area x (distance)²
- need for behavior of
 - beams
 - columns



BUDGLING

GRITICAL

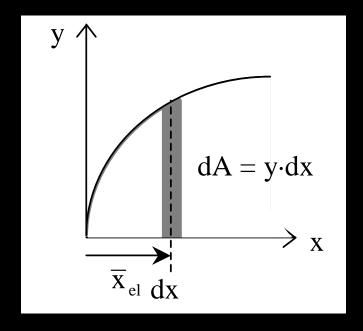
DISPLACEMEN

Moment of Inertia

- about any reference axis
- can be <u>negative</u>

$$I_{y} = \int x^{2} dA$$

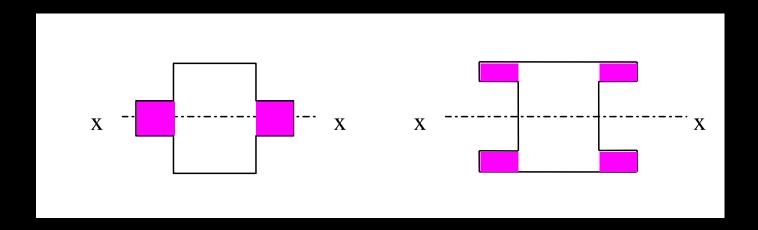
$$I_x = \int y^2 dA$$



resistance to bending and buckling

Moment of Inertia

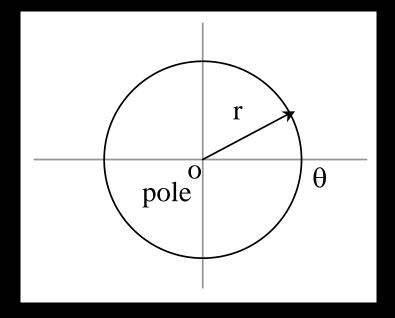
- larger area <u>away</u> for same distance
 - -larger I



Polar Moment of Inertia

- for round-ish shapes
- uses polar coordinates (r and θ)
- resistance to twisting

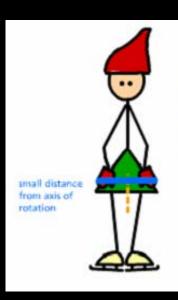
$$J_o = \int r^2 dA$$



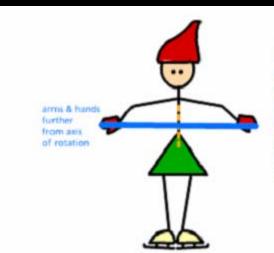
Radius of Gyration

measure of inertia with respect to area

$$r_{x} = \sqrt{\frac{I_{x}}{A}}$$



When a figure skater changes position, he or she is redistributing his or her mass. Thus, every position has it's own unique rotational inertia.



The rotational inertia of the figure skater increases when her arms are raised because more of her mass is redistributed further from her axis of rotation.

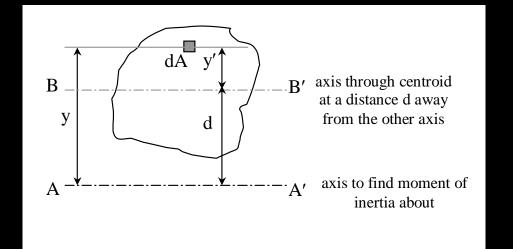
Parallel Axis Theorem

• can find composite I once composite centroid is known (basic shapes)

$$I_{x} = I_{cx} + Ad_{y}^{2}$$
$$= \underline{\overline{I}}_{x} + Ad_{y}^{2}$$

$$I = \sum \bar{I} + \sum Ad^2$$

$$|\bar{I} = I - Ad^2|$$



Basic Procedure

- 1. Draw reference origin (if not given)
- 2. Divide into basic shapes (+/-)
- 3. Label shapes
- 4. Draw table with $A, \overline{x}, \overline{x}A, \overline{y}, \overline{y}A, \overline{I}$'s, d's, and Ad^2 's
- 5. Fill in table and get \hat{x} and \hat{y} for composite
- 6. Sum necessary columns
- 7. Sum \overline{I} 's and Ad^2 's

$$(d_x = \hat{x} - \overline{x})$$

$$(d_y = \hat{y} - \overline{y})$$

Area Moments of Inertia

Table 7.2 − pg. 252: (bars refer to centroid)



$$-x', y'$$

-C

