Architectural Structures I: Statics and Strength of Materials ends 231 Dr. Anne Nichols Spring 2007 lecture eleven

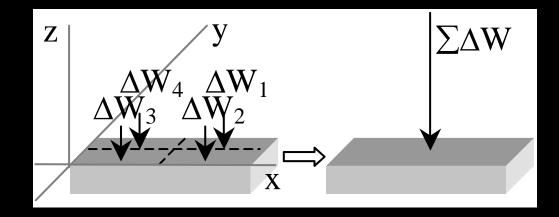


centers of gravity- centroids

Centroids 1 Lecture 11 Architectural Structures I ENDS 231

Center of Gravity

- location of equivalent weight
- determined with calculus

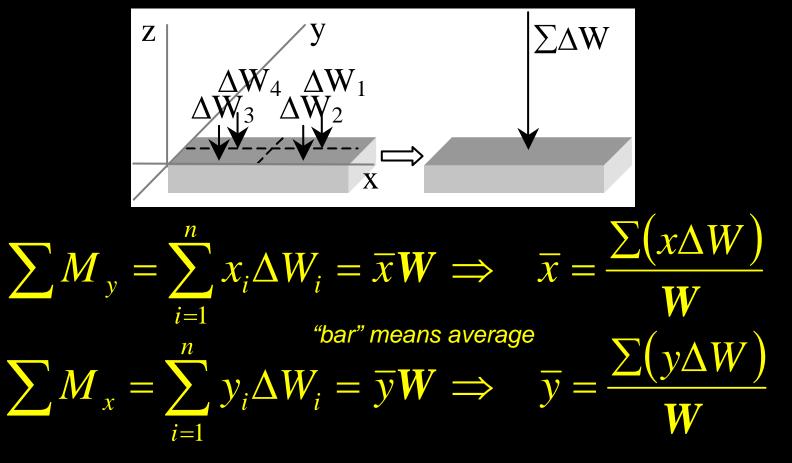


• sum element weights $W = \int dW$

Centroids 2 Lecture 11 Architectural Structures I ENDS 231

Center of Gravity

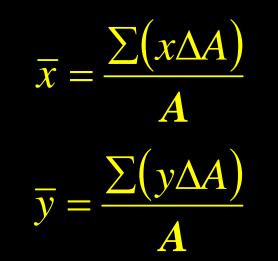
• "average" x & y from moment

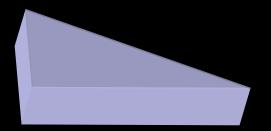


Centroids 3 Lecture 11 Architectural Structures I ENDS 231

Centroid

- "average" x & y of an area
- for a volume of constant thickness
 - $-\Delta W = \gamma t \Delta A \quad \text{where } \gamma \text{ is weight/volume} \\ \text{center of gravity} = \text{centroid of area}$

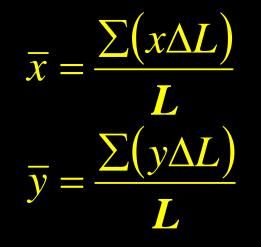




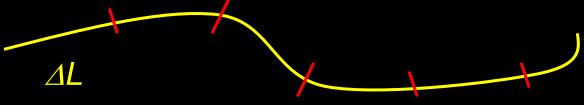
Centroids 4 Lecture 11 Architectural Structures I ENDS 231

Centroid

• for a line, sum up length



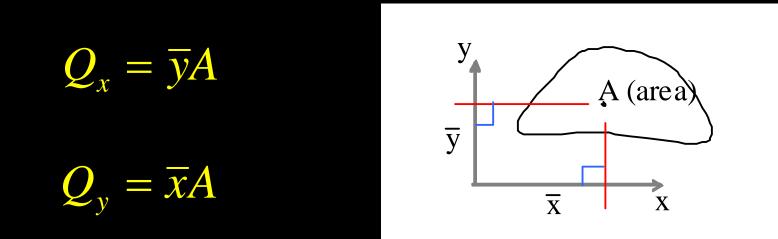




Architectural Structures I ENDS 231

1st Moment Area

- math concept
- the moment of an area about an axis



Centroids 6 Lecture 11 Architectural Structures I ENDS 231

Symmetric Areas

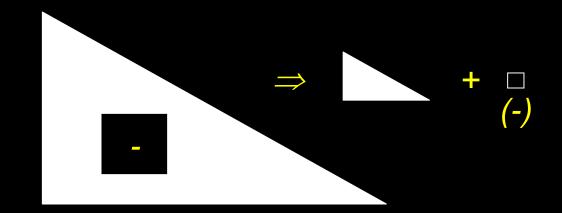
- symmetric about an axis
- symmetric about a center point

• mirrored symmetry

Centroids 7 Lecture 11 Architectural Structures I ENDS 231

Composite Areas

- made up of basic shapes
- areas can be <u>negative</u>
- (centroids can be negative for any area)



Centroids 8 Lecture 11 Architectural Structures I ENDS 231

Basic Procedure

- 1. Draw reference origin (if not given)
- 2. Divide into basic shapes (+/-)
- 3. Label shapes
- 4. Draw tableComponentArea \overline{x} \overline{xA} 5. Fill in table Σ \Box \Box
- 6. Sum necessary columns
- 7. Calculate \hat{x} and \hat{y}

 \overline{y}

ÿΑ

Area Centroids

• *Table 7.1 – pg. 242*

| Centroids of Common Shapes of Areas and Lines | | | |
|-----------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----------------------------------|-------------------|
| Shape | | x | y y |
| Triangular area | $\frac{1}{\frac{1}{\sqrt{y}}} \xrightarrow{\bullet C} \stackrel{h}{\longrightarrow} \stackrel{h}$ | $\frac{b}{3}$ right triangle only | $\frac{h}{3}$ |
| Quarter-circular area | c = c = r | $\frac{4r}{3\pi}$ | $\frac{4r}{3\pi}$ |
| Semicircular area | | 0 | $\frac{4r}{3\pi}$ |
| Semiparabolic area | $C \xrightarrow{a} \downarrow \overline{y}$ | $\frac{3a}{8}$ | $\frac{3h}{5}$ |
| Parabolic area | | 0 | $\frac{3h}{5}$ |

Centroids 10 Lecture 11 Architectural Structures I ENDS 231