Architectural Structures I: Statics and Strength of Materials ends 231 Dr. Anne Nichols Spring 2007 lecture eleven

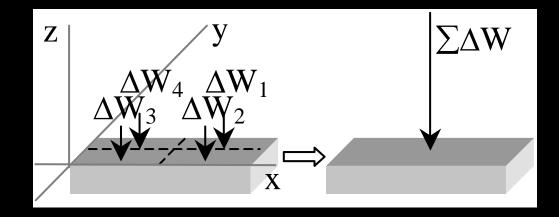


centers of gravity- centroids

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Center of Gravity

- location of equivalent weight
- determined with calculus

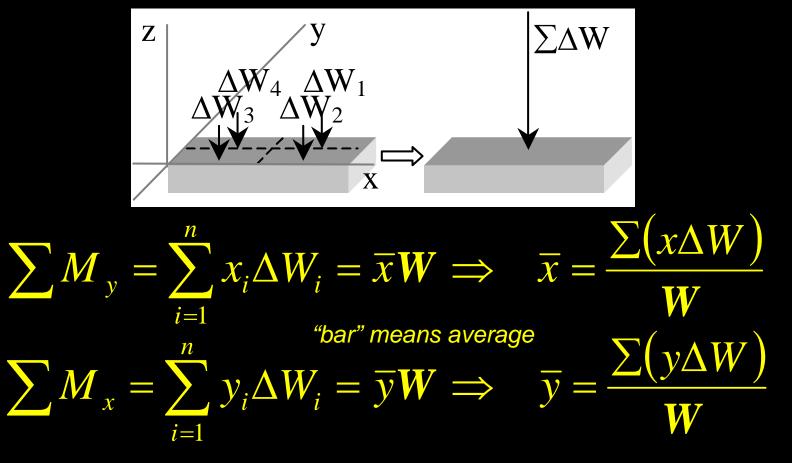


• sum element weights $W = \int dW$

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Center of Gravity

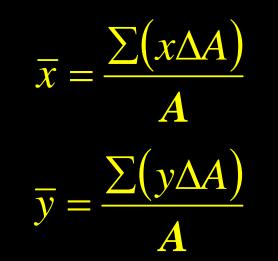
• "average" x & y from moment

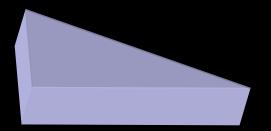


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Centroid

- "average" x & y of an area
- for a volume of constant thickness
 - $-\Delta W = \gamma t \Delta A \quad \text{where } \gamma \text{ is weight/volume} \\ \text{center of gravity} = \text{centroid of area}$

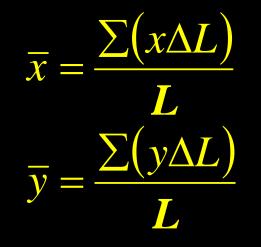




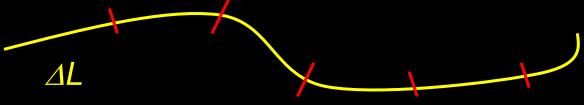
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Centroid

• for a line, sum up length



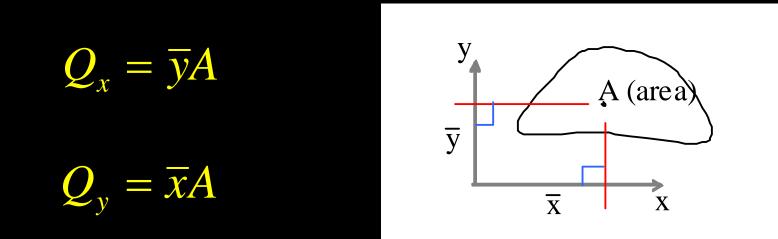




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1st Moment Area

- math concept
- the moment of an area about an axis



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Symmetric Areas

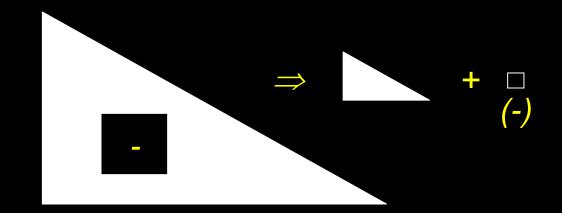
- symmetric about an axis
- symmetric about a center point

• mirrored symmetry

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Composite Areas

- made up of basic shapes
- areas can be <u>negative</u>
- (centroids can be negative for any area)



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Basic Procedure

- 1. Draw reference origin (if not given)
- 2. Divide into basic shapes (+/-)
- 3. Label shapes
- 4. Draw tableComponentArea \overline{x} \overline{xA} 5. Fill in table Σ \Box \Box
- 6. Sum necessary columns
- 7. Calculate \hat{x} and \hat{y}

 \overline{y}

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Area Centroids

• *Table 7.1 – pg. 242*

Centroids of Common Shapes of Areas and Lines			
Shape		x	y y
Triangular area	$\frac{1}{\frac{1}{\sqrt{y}}} \xrightarrow{\bullet C} \stackrel{h}{\longrightarrow} \stackrel{h}$	$\frac{b}{3}$ right triangle only	$\frac{h}{3}$
Quarter-circular area	c = c = r	$\frac{4r}{3\pi}$	$\frac{4r}{3\pi}$
Semicircular area		0	$\frac{4r}{3\pi}$
Semiparabolic area	$C \xrightarrow{a} \downarrow \overline{y}$	$\frac{3a}{8}$	$\frac{3h}{5}$
Parabolic area		0	$\frac{3h}{5}$

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