ARCHITECTURAL STRUCTURES I:
STATICS AND STRENGTH OF MATERIALS

ENDS 231

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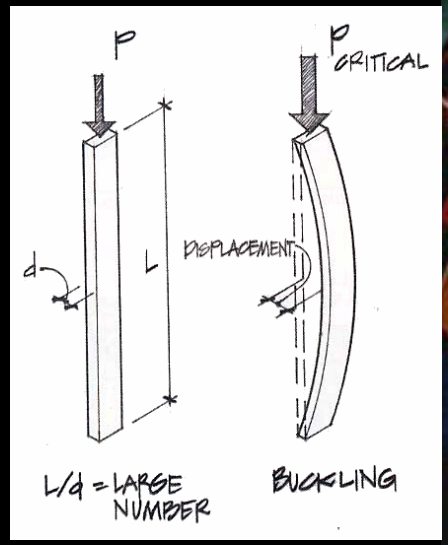
lecture
twenty

stability and columns

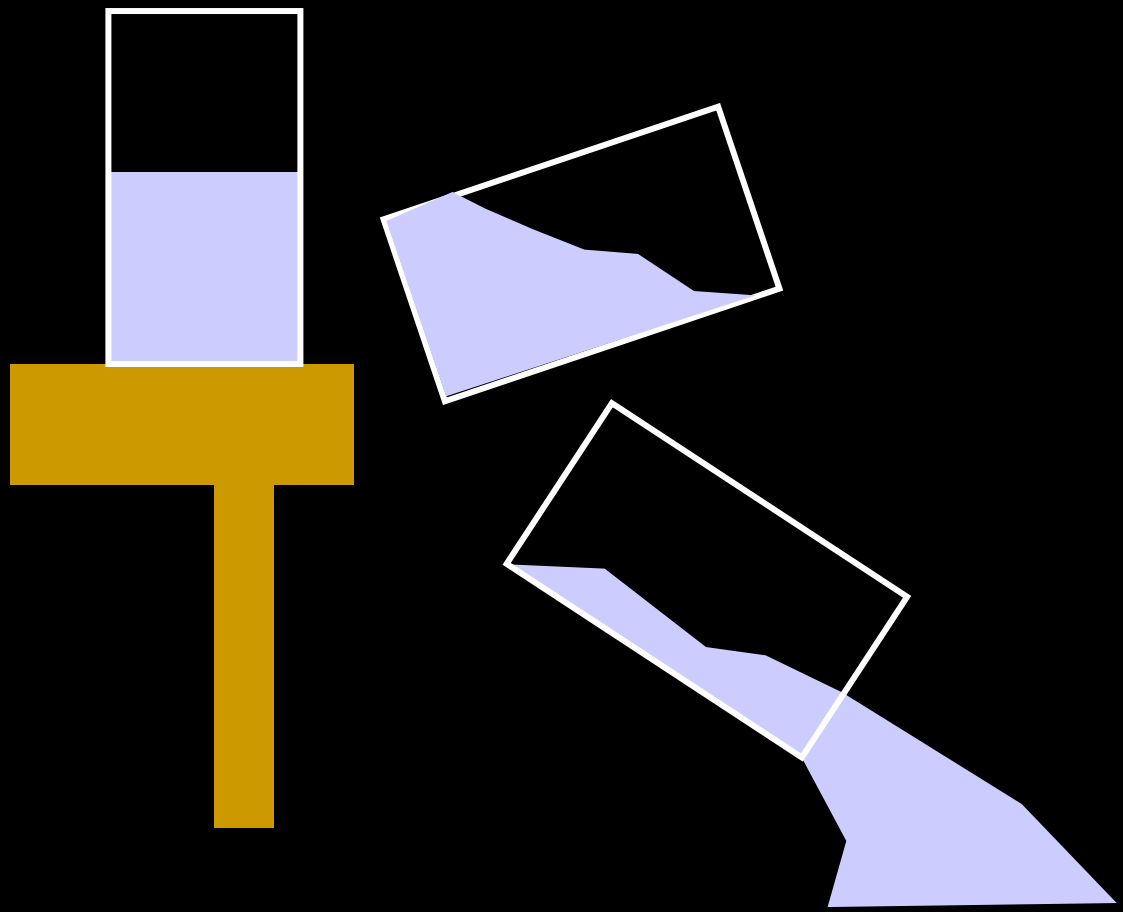
Additional Design Criteria

- *designed for strength & stresses*
- *designed for serviceability & deflection*
- *need to design for <u>stability</u>*
  - *ability to support a specified load without sudden or unacceptable deformations*



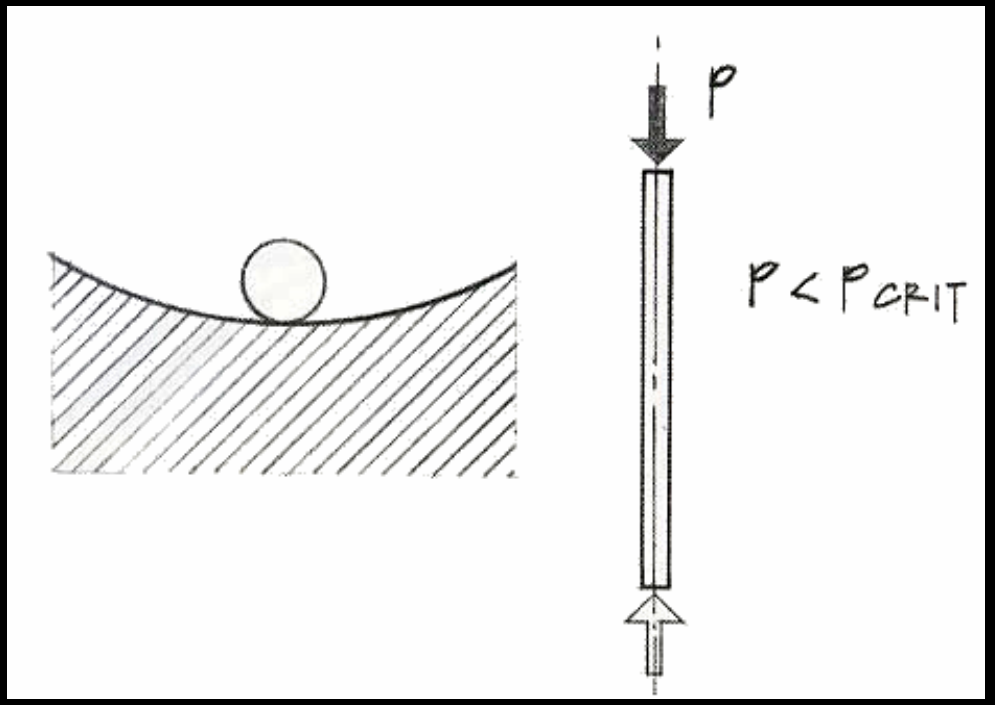
Column Behavior

- *objects like lowest energy state*



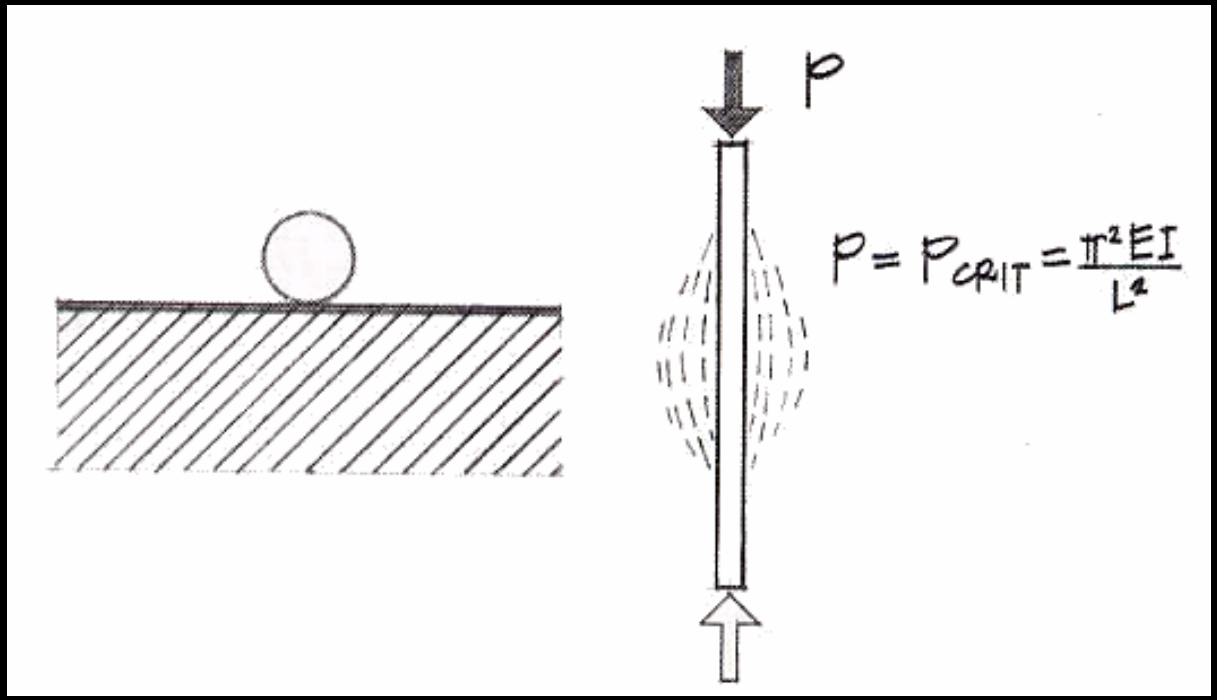
Stable Equilibrium

- *energy added*
- *things don't change*



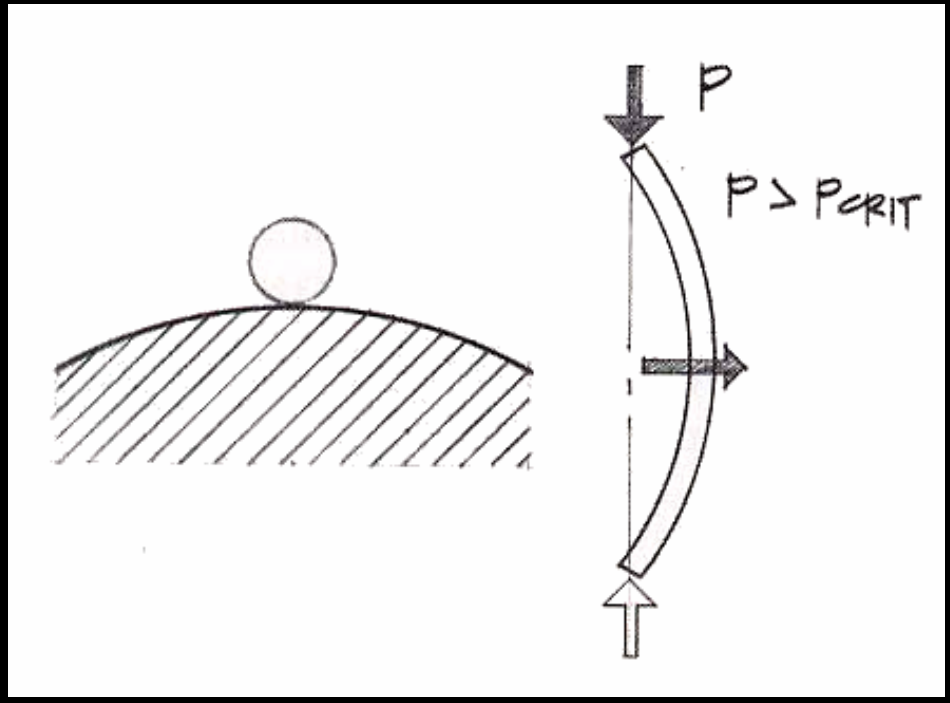
Neutral Equilibrium

- *energy added*
- *things change, but not much*



Unstable Equilibrium

- *energy added*
- *things change drastically*



Column Buckling

- *axially loaded columns*
- *long & slender*
  - *unstable equilibrium = buckling*
  - *sudden and not good*

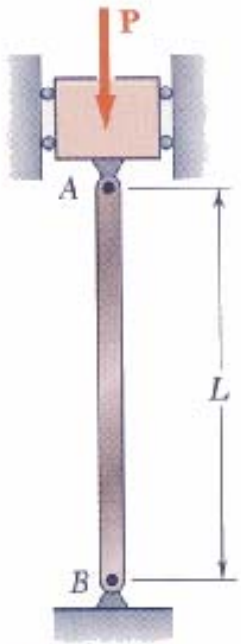
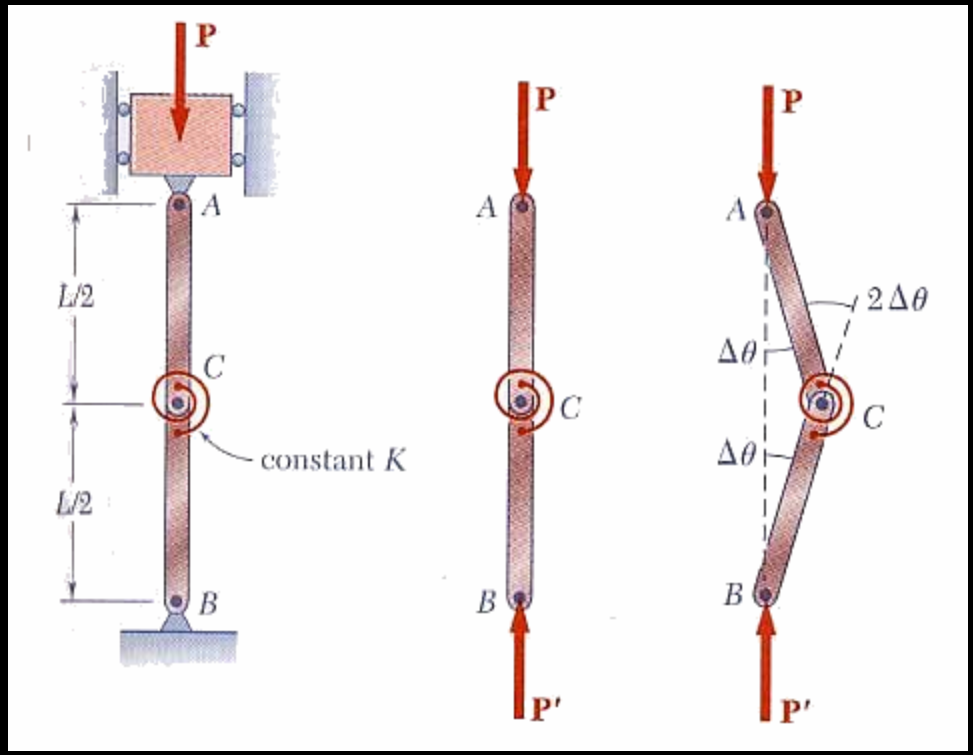


Fig. 10.1

Fig. 10.2

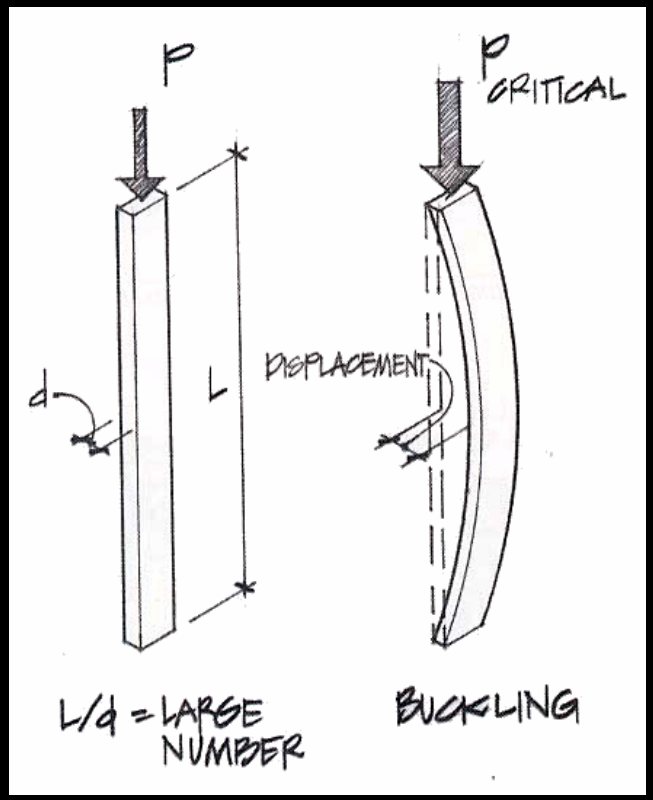
Modeling

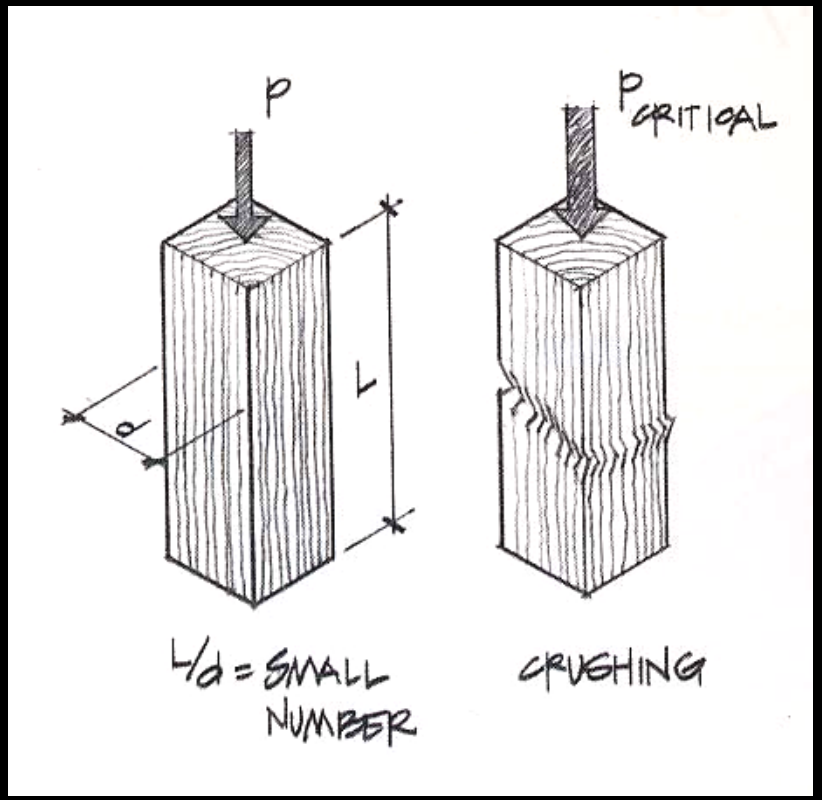
- *can be modeled with a spring at mid-height*
- *when moment from deflection exceeds the spring capacity … "boing"*
- *critical load P*



Effect of Length

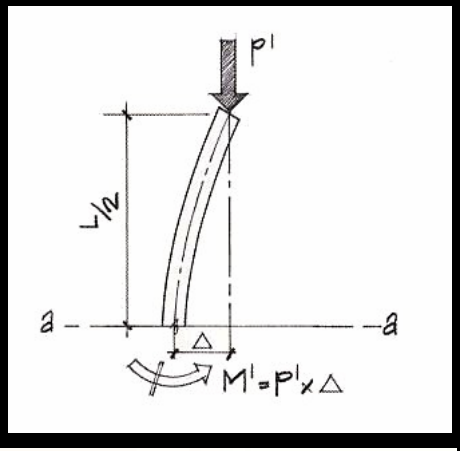
- *long & slender*
- *short & stubby*





Buckling Load

- *related to deflected shape (PΔ)*
- *shape of sine wave*
- *Euler's Formula*
- *I minimum*



$$P_{critical} = \frac{\pi^2 E I_{\min}}{(L)^2}$$

Figure 9.3 Leonhard Euler (1707–1783).

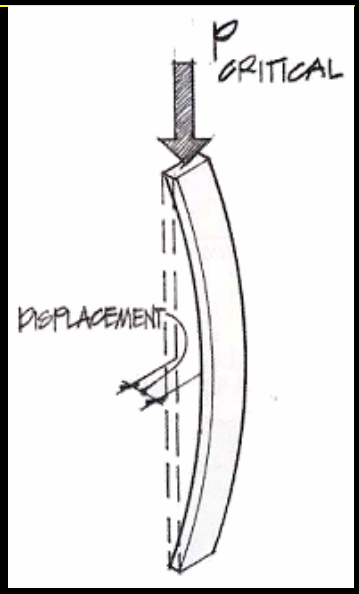
Critical Stress

- short columns

$$f_{critical} = \frac{P_{actual}}{A} < F_a$$

- slenderness ratio = L_e/r (L/d)

- radius of gyration = $r = \sqrt{\frac{I}{A}}$



weak axis

$$f_{critical} = \frac{P_{critical}}{A} = \frac{\pi^2 EAr^2}{A(L_e)^2} = \frac{\pi^2 E}{\left(L_e/r\right)^2}$$

$$P_{critical} = \frac{\pi^2 EA}{\left(L_e/r\right)^2}$$

Critical Stresses

- *when a column gets stubby, F_y will limit the load*
- *real world has loads with eccentricity*
- *C_c for steel and allowable stress*

$$\frac{L_e}{r} > C_c = \sqrt{\frac{2\pi^2 E}{F_y}}$$

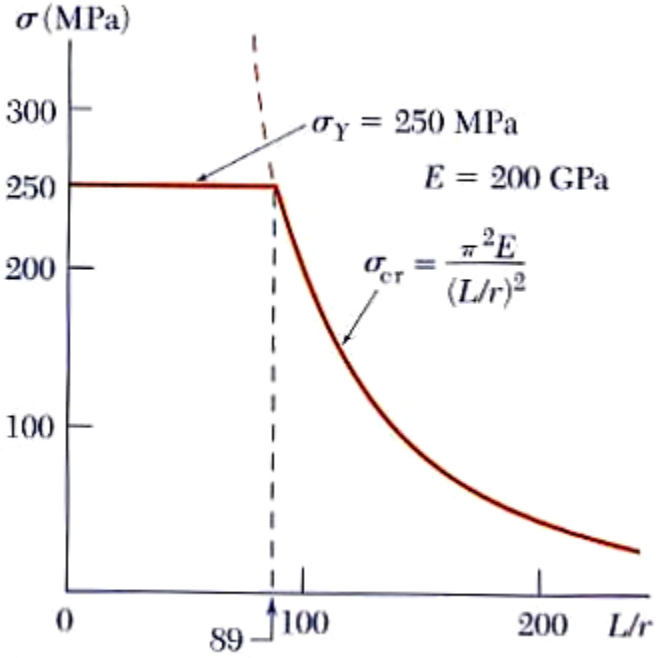
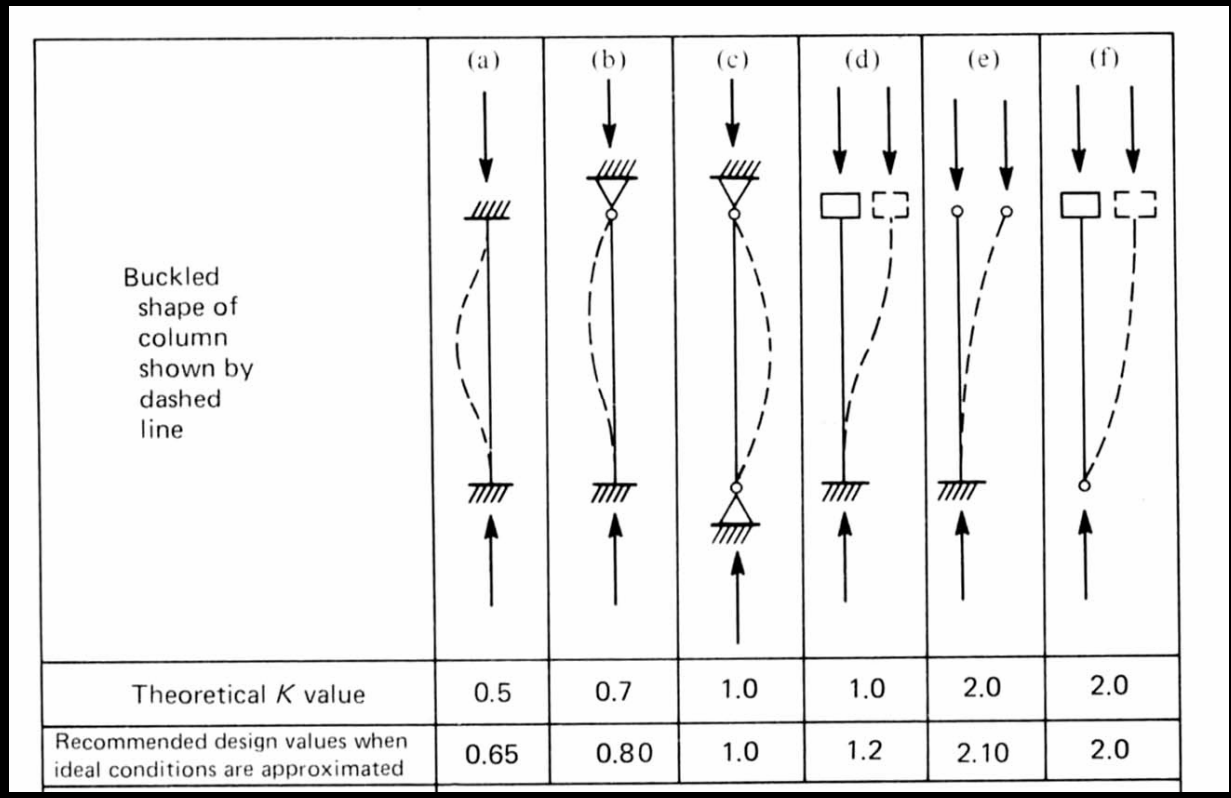


Fig. 10.9

Effective Length

- *end conditions affect shape*
- *effective length factor, K* $L_e = K \cdot L$



Bracing

- *bracing affects shape of buckle in one direction*
- *both should be checked!*