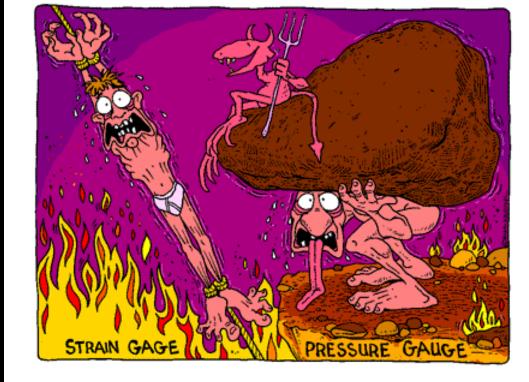
ARCHITECTURAL **S**TRUCTURES **I**: STATICS AND STRENGTH OF MATERIALS

ENDS 231 DR. ANNE NICHOLS **SUMMER 2006**





elasticity & strain

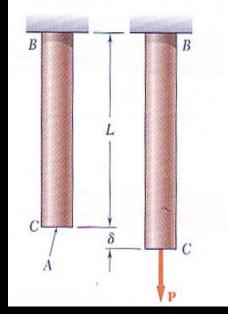
Strain 1

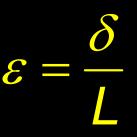
Lecture 15

Architectural Structures I **ENDS 231**

Deformations

- materials deform
- axially loaded materials change length
- normal stress is load per unit area
- STRAIN:
 - change in length over length
 - UNITLESS



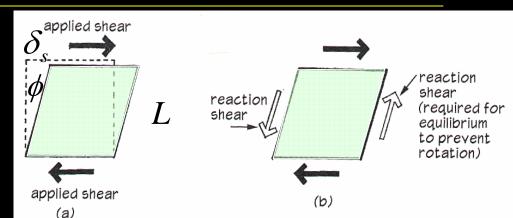


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Shearing Strain

- deformations with shear
- parallelogram
- change in angles
- stress:
- strain: γ
 unitless (radians)

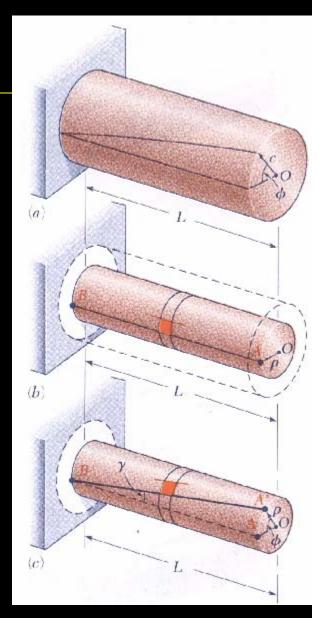
 \mathcal{T}



$$\gamma = \frac{\delta_s}{L} = \tan \phi \cong \phi$$

Shearing Strain

- deformations with torsion
- twist
- change in angle of line
- stress: au
- strain: γ
 unitless (radians)



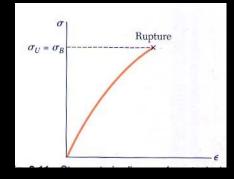
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 $ho\phi$

/

Load and Deformation

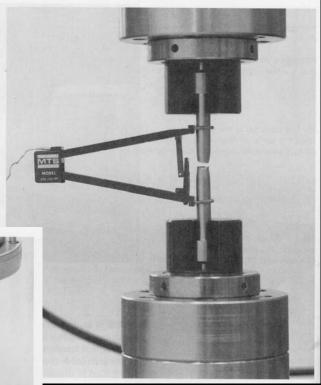
- for stress, need P & A
- for strain, need δ & L
 - how?
 - TEST with load and measure
 - plot P/A vs. ε





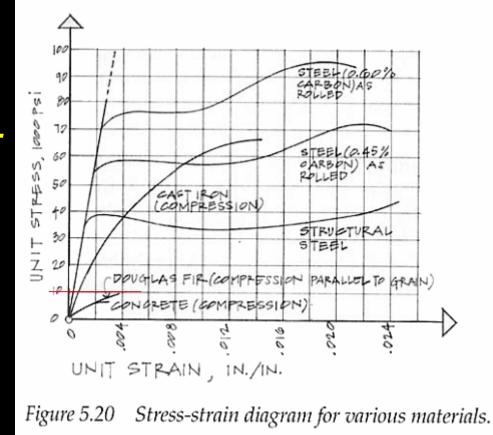


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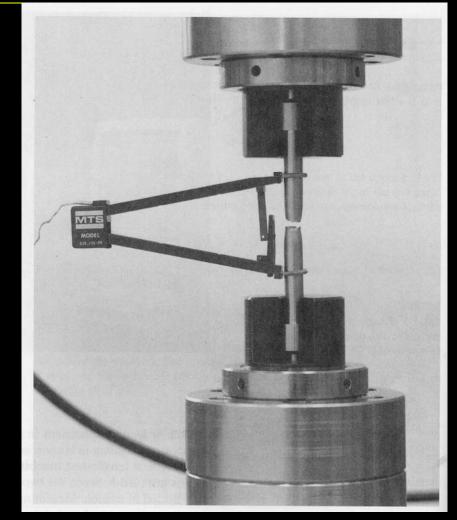
Material Behavior

- every material has its own response
 - 10,000 psi
 - -L = 10 in
 - Douglas Fir vs. steel?



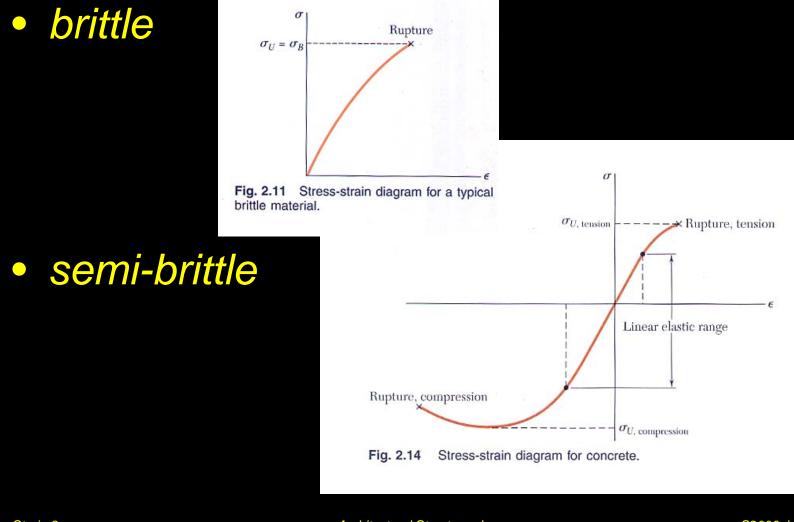
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Behavior Types • ductile - "necking" • true stress A • engineering stress - (simplified)



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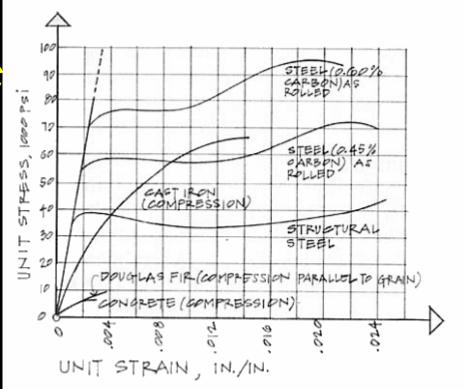


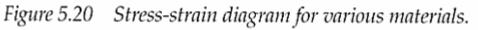
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Stress to Strain

• important to us in $f - \varepsilon$ diagrams:

- straight section
- LINEAR-ELASTIC
- recovers shape (no permanent deformation)



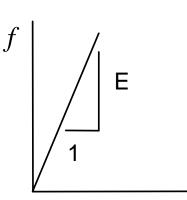


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Hooke's Law

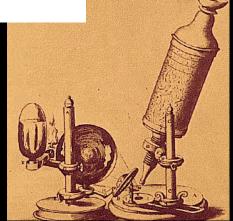
- straight line has constant slope
- Hooke's Law

 $f = E \cdot \varepsilon$



- Modulus of elasticity

Young's modulusunits just like stress

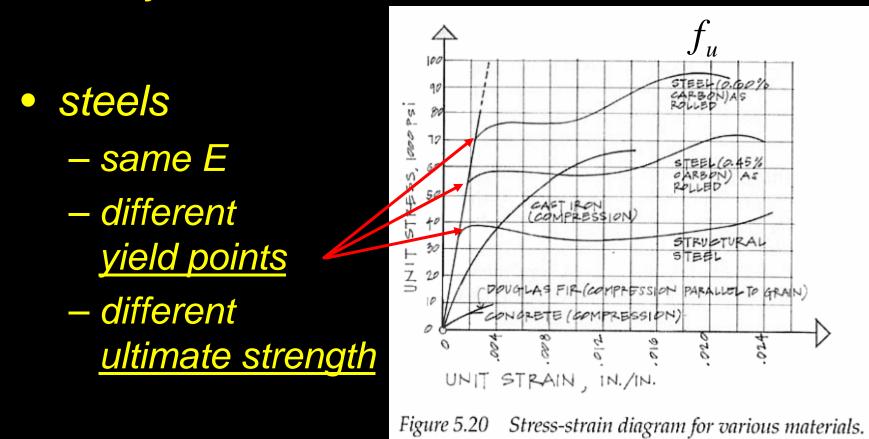


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Stiffness

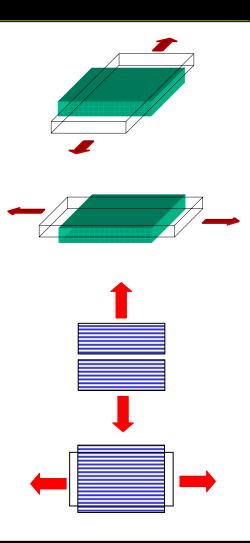
• ability to resist strain



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Isotropy & Anisotropy

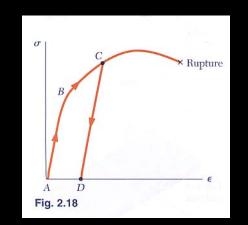
- ISOTROPIC
 - materials with E <u>same</u> at any direction of loading
 - ex. steel
- ANISOTROPIC
 - materials with <u>different</u> E at any direction of loading
 - ex. wood

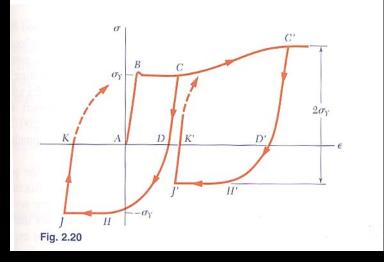


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Elastic, Plastic, Fatigue

- elastic springs back
- plastic has permanent deformation
- fatigue caused by reversed loading cycles

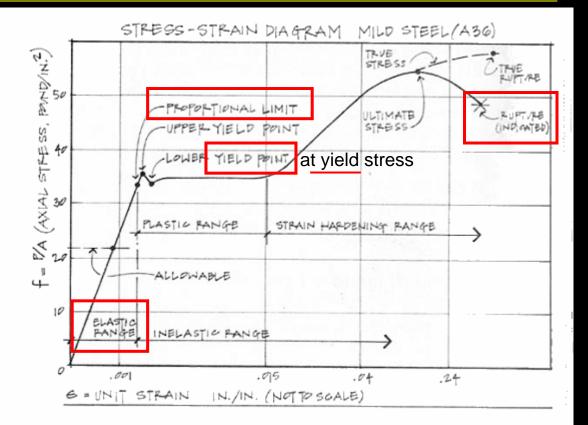


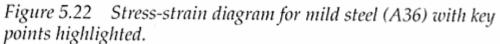


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Plastic Behavior

• ductile

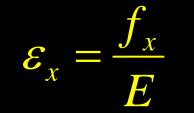




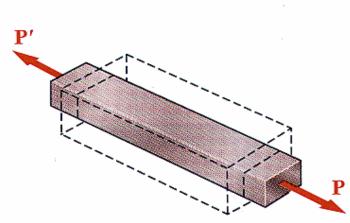
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Lateral Strain

 or "what happens to the cross section with axial stress"



 $f_{v} = f_{z} = 0$



E

- strain in lateral direction
 - negative
 - equal for isometric materials

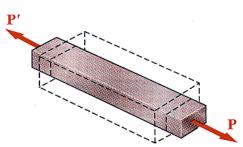


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Poisson's Ratio

• constant relationship between longitudinal strain and lateral strain

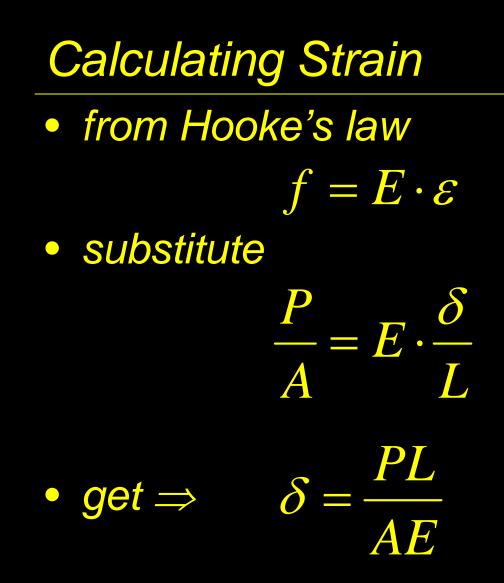
 $\mu = -\frac{\text{lateral strain}}{\text{axial strain}} = -\frac{\varepsilon_y}{\varepsilon_x} = -\frac{\varepsilon_z}{\varepsilon_x}$ $\varepsilon_y = \varepsilon_z = -\frac{\mu f_x}{E}$

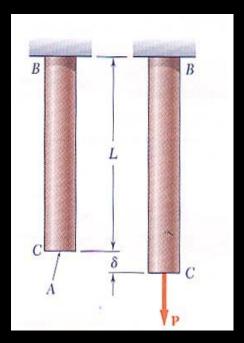




 $0 < \mu < 0.5$

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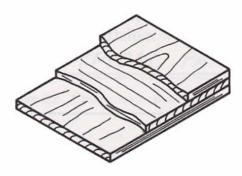




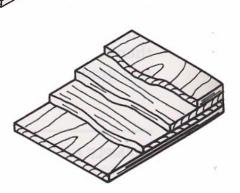
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Orthotropic Materials

- non-isometric
- directional values of E and μ
- ex:
 - plywood
 - laminates
 - polymercomposites





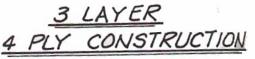


BACK

FACE

CROSS BAND

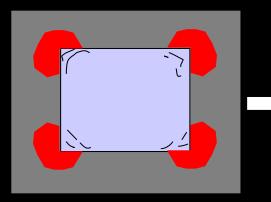
FACE

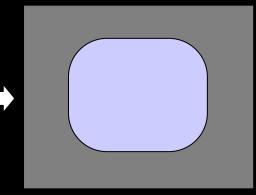


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Stress Concentrations

- why we use f_{ave}
- increase in stress at changes in geometry
 - sharp notches
 - holes
 - corners





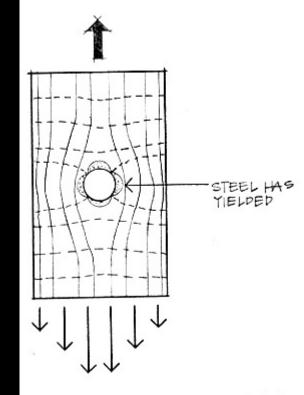
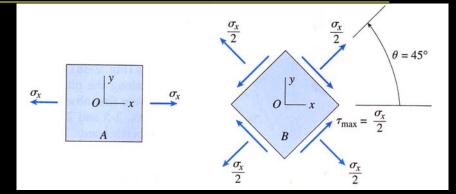


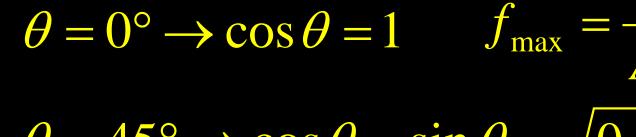
Figure 5.35 Stress trajectories around a hole.

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Maximum Stresses

 if we need to know where max f and f_v happen:





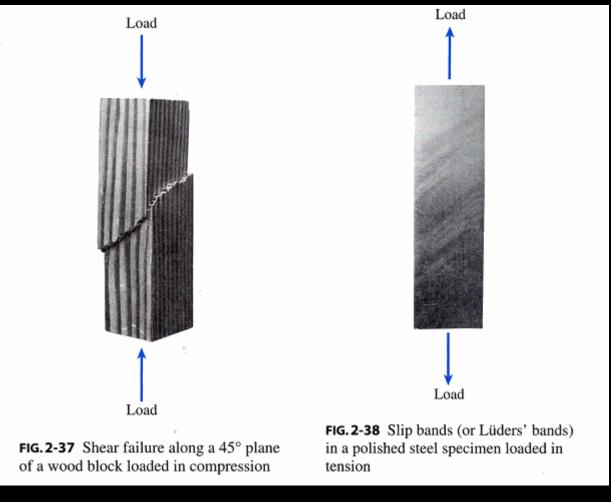


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S2006abr

max

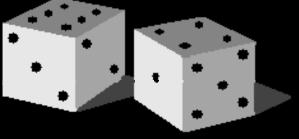
Maximum Stresses

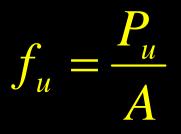


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Design of Members

- beyond allowable stress...
- materials aren't uniform 100% of the time
 - ultimate strength or capacity to failure may be different and some strengths hard to test for
- RISK & UNCERTAINTY





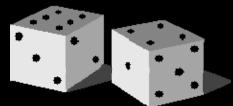
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Factor of Safety

- accommodate uncertainty with a safety factor: allowable load = $\frac{\text{ultimate load}}{F.S}$
- with linear relation between load and stress: $F.S = \frac{ultimate load}{allowable load} = \frac{ultimate stress}{allowable stress}$

Load and Resistance Factor Design

- loads on structures are
 - not constant



- can be more influential on failure
- happen more or less often
- UNCERTAINTY

 $R_{u} = \gamma_{D}R_{D} + \gamma_{L}R_{L} \leq \phi R_{n}$

 ϕ - resistance factor γ - load factor for (D)ead & (L)ive load

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