#### Architectural Structures I: Statics and Strength of Materials

ends 231 Dr. Anne Nichols Summer 2006

lecture ten

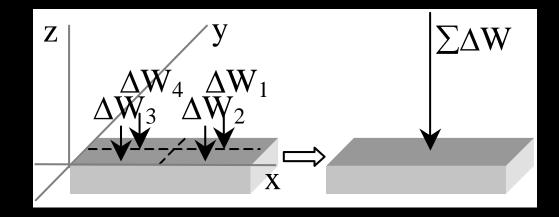


# centers of gravity- centroids

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# **Center of Gravity**

- location of equivalent weight
- determined with calculus

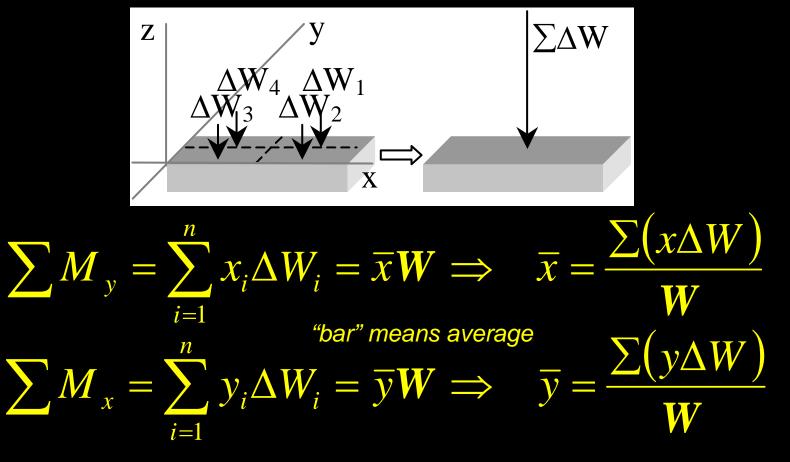


• sum element weights  $W = \int dW$ 

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# Center of Gravity

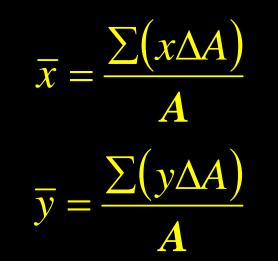
#### • "average" x & y from moment

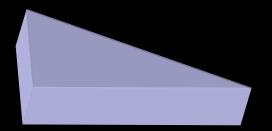


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### Centroid

- "average" x & y of an area
- for a volume of constant thickness
  - $-\Delta W = \gamma t \Delta A \quad \text{where } \gamma \text{ is weight/volume} \\ \text{center of gravity} = \text{centroid of area}$

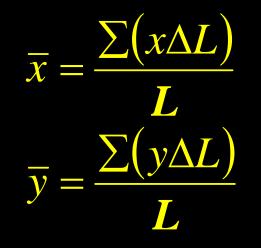




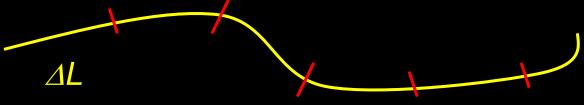
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# Centroid

• for a line, sum up length



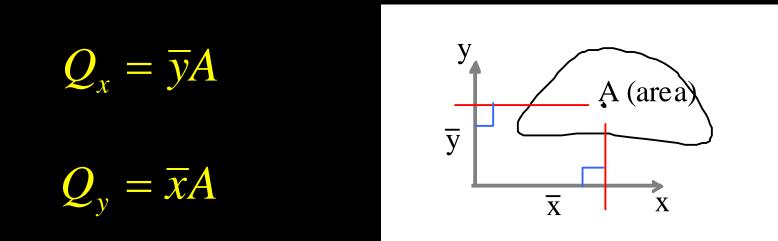




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#### 1<sup>st</sup> Moment Area

- math concept
- the moment of an area about an axis



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# Symmetric Areas

- symmetric about an axis
- symmetric about a center point

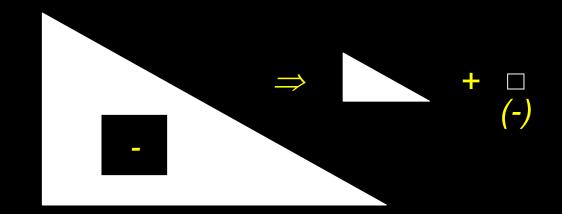
• mirrored symmetry

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# **Composite Areas**

- made up of basic shapes
- areas can be <u>negative</u>
- (centroids can be negative for any area)



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#### **Basic Procedure**

- 1. Draw reference origin (if not given)
- 2. Divide into basic shapes (+/-)
- 3. Label shapes
- 4. Draw tableComponentArea $\bar{x}$  $\bar{x}A$  $\bar{y}$  $\bar{y}A$ 5. Fill in table $\Sigma$ III
- 6. Sum necessary columns
- 7. Calculate  $\hat{x}$  and  $\hat{y}$

# Area Centroids

# • *Table 7.1 – pg. 242*

Centroids of Common Shapes of Areas and Lines			
Shape		x	y y
Triangular area	$\frac{1}{\sqrt{y}}$	$\frac{b}{3}$ right triangle only	$\frac{h}{3}$
Quarter-circular area	$c = \frac{c}{ \overline{y} } = c = r$	$\frac{4r}{3\pi}$	$\frac{4r}{3\pi}$
Semicircular area		0	$\frac{4r}{3\pi}$
Semiparabolic area	$C \xrightarrow{a} \downarrow \overline{y}$	$\frac{3a}{8}$	$\frac{3h}{5}$
Parabolic area		0	$\frac{3h}{5}$

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