Architectural Structures I: Statics and Strength of Materials

ends 231 Dr. Anne Nichols Summer 2006

lecture ten

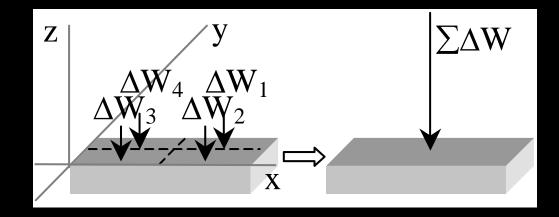


centers of gravity- centroids

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Center of Gravity

- location of equivalent weight
- determined with calculus

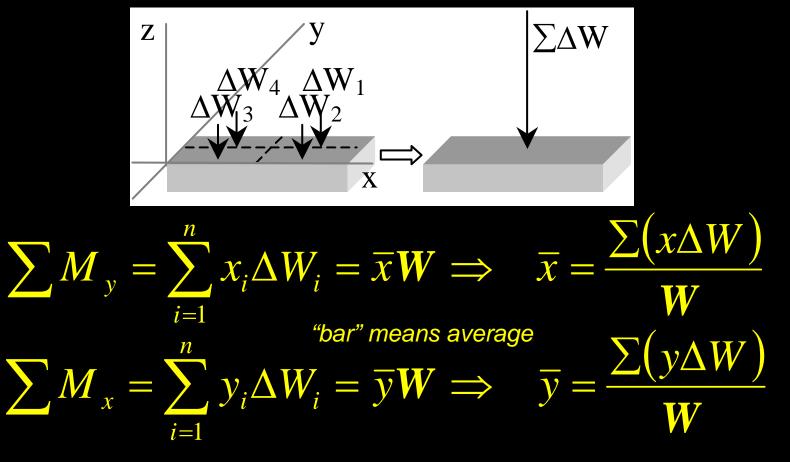


• sum element weights $W = \int dW$

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Center of Gravity

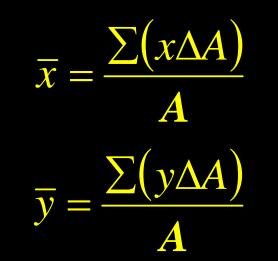
• "average" x & y from moment

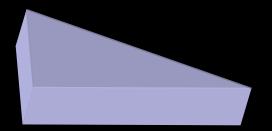


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Centroid

- "average" x & y of an area
- for a volume of constant thickness
 - $-\Delta W = \gamma t \Delta A \quad \text{where } \gamma \text{ is weight/volume} \\ \text{center of gravity} = \text{centroid of area}$

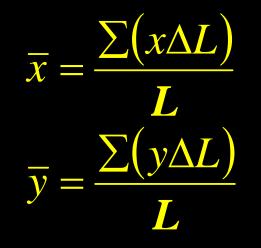




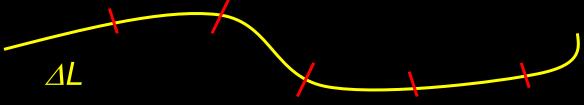
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Centroid

• for a line, sum up length



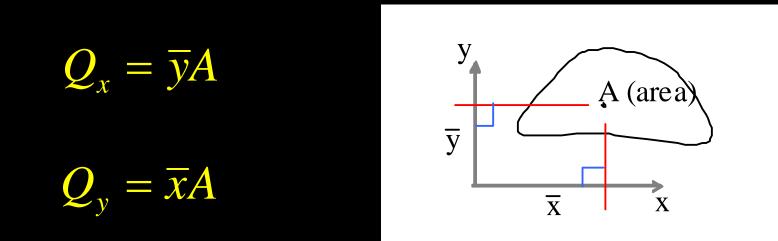




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1st Moment Area

- math concept
- the moment of an area about an axis



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Symmetric Areas

- symmetric about an axis
- symmetric about a center point

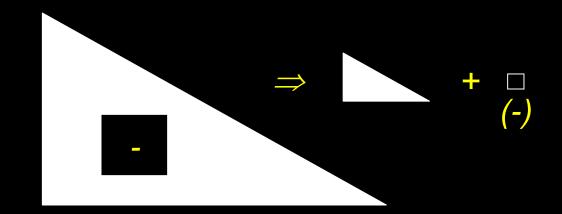
• mirrored symmetry

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Composite Areas

- made up of basic shapes
- areas can be <u>negative</u>
- (centroids can be negative for any area)



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Basic Procedure

- 1. Draw reference origin (if not given)
- 2. Divide into basic shapes (+/-)
- 3. Label shapes
- 4. Draw tableComponentArea \bar{x} $\bar{x}A$ \bar{y} $\bar{y}A$ 5. Fill in table Σ III
- 6. Sum necessary columns
- 7. Calculate \hat{x} and \hat{y}

Area Centroids

• *Table 7.1 – pg. 242*

| Centroids of Common Shapes of Areas and Lines | | | |
|---|---|-----------------------------------|-------------------|
| Shape | | x | y y |
| Triangular area | $\frac{1}{\sqrt{y}}$ | $\frac{b}{3}$ right triangle only | $\frac{h}{3}$ |
| Quarter-circular area | $c = \frac{c}{ \overline{y} } = c = r$ | $\frac{4r}{3\pi}$ | $\frac{4r}{3\pi}$ |
| Semicircular area | | 0 | $\frac{4r}{3\pi}$ |
| Semiparabolic area | $C \xrightarrow{a} \downarrow \overline{y}$ | $\frac{3a}{8}$ | $\frac{3h}{5}$ |
| Parabolic area | | 0 | $\frac{3h}{5}$ |

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