

Steel & Wood Column Design

Design Aims

If we know the loads, we can select a section that is adequate for strength & buckling.

If we know the length, we can find the limiting load satisfying strength & buckling.

Design Code Methodologies

Allowable Stress Design (ASD): the stress in a member must be less than an allowable stress which is equal to the yield stress divided by a factor of safety.

Load and Resistance Factor Design: more efficient method that factors loads for importance and compares the summation to a nominal strength that has been adjusted by a reduction factor.

Allowable Stress Design - Steel

American Institute of Steel Construction (AISC) Manual of ASD, 9th ed:

Long and slender: [$L_c/r \geq C_c$, preferably < 200]

$$F_{allowable} = \frac{F_{cr}}{F.S.} = \frac{12\pi^2 E}{23(KL/r)^2}$$

The yield limit is idealized into a parabolic curve that blends into the Euler's Formula at C_c .

With $F_y = 36$ ksi, $C_c = 126.1$

$$C_c = \sqrt{\frac{2\pi^2 E}{F_y}}$$

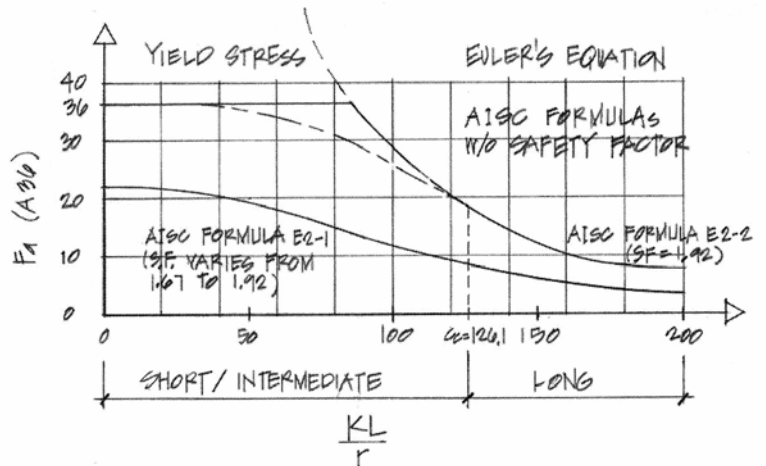
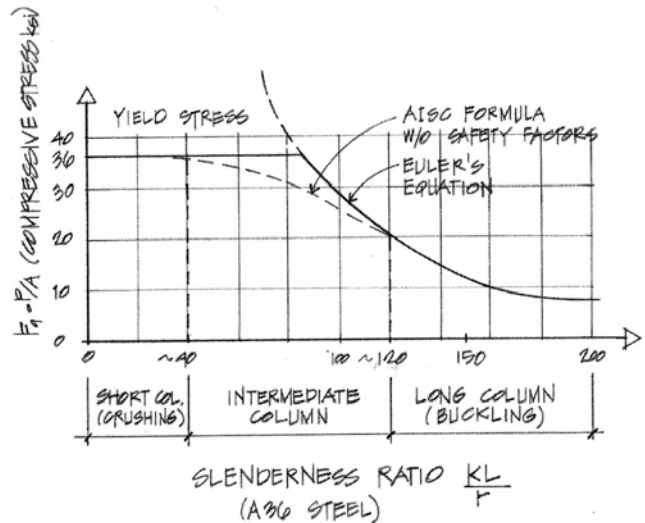
With $F_y = 50$ ksi, $C_c = 107.0$

Short and stubby: [$L_c/r < C_c$]

$$F_a = \left[1 - \frac{(KL/r)^2}{2C_c^2} \right] \frac{F_y}{F.S.}$$

with:

$$F.S. = \frac{5}{3} + \frac{3(KL/r)}{8C_c} - \frac{(KL/r)^3}{8C_c^3}$$



Procedure for Analysis

1. Calculate KL/r for each axis (if necessary). The largest will govern the buckling load.
2. Find F_a as a function of KL/r from Table 10.1 or 10.2 (pp. 361-364)
3. Compute $P_{\text{allowable}} = F_a \cdot A$ or alternatively compute $f_{\text{actual}} = P/A$
4. Is the design satisfactory?

Is $P \leq P_{\text{allowable}}$? \Rightarrow yes, it is; no, it is no good

or Is $f_{\text{actual}} \leq F_a$? \Rightarrow yes, it is; no, it is no good

Procedure for Design

1. Guess a size by picking a section.
2. Calculate KL/r for each axis (if necessary). The largest will govern the buckling load.
3. Find F_a as a function of KL/r from Table 10.1 or 10.2 (pp. 361-364)
4. Compute $P_{\text{allowable}} = F_a \cdot A$ or alternatively compute $f_{\text{actual}} = P/A$
5. Is the design satisfactory?

Is $P \leq P_{\text{allowable}}$? \Rightarrow yes, it is; no, pick a bigger section and go back to step 2.

or Is $f_{\text{actual}} \leq F_a$? \Rightarrow yes, it is; no, pick a bigger section and go back to step 2.

6. Check design efficiency by calculating percentage of stress used = $\frac{P_{\text{actual}}}{P_{\text{allowable}}} \cdot 100\%$

If value is between 90-100%, it is efficient.

If values is less than 90%, pick a smaller section and go back to step 2.

The critical load with respect to the slenderness ratio is presented in chart format in ASD, 8th ed, as well as the allowable stress charts for compression members.

Allowable Stress Design - Wood

National Design Specification for Wood Construction (1992):

Any slenderness ratio, $L_c/d \leq 50$:

$$f_c = \frac{P}{A} \leq F'_c$$

$$F'_c = F_c (C_D)(C_M)(C_t)(C_F)(C_p)$$

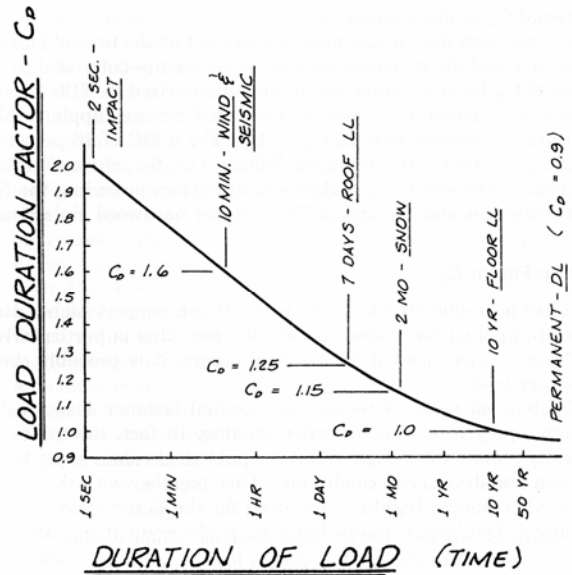
The curve uses factors to replicate the combination curve:

where:

- F'_c = allowable compressive stress parallel to the grain
- F_c = compressive strength parallel to the grain
- C_D = load duration factor
- C_M = wet service factor (1.0 for dry)
- C_t = temperature factor
- C_F = size factor
- C_p = column stability factor off chart

For preliminary column design:

$$F'_c = F_c^* C_p = (F_c C_D) C_p$$



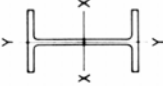
Procedure for Analysis

1. Calculate L_e/d_{min}
2. Obtain F'_c
 compute $F_{cE} = \frac{K_{cE} E}{(l_e/d)^2}$ with $K_{cE} = 0.3$ for sawn, = 0.418 for glu-lam
3. Compute $F_c^* \cong F_c C_D$ with $C_D = 1$, normal, $C_D = 1.25$ for 7 day roof...
4. Calculate F_{cE}/F_c^* and get C_p from Appendix A, Table 14 (pp. 413-414)
5. Calculate $F'_c = F_c^* C_p$
6. Compute $P_{allowable} = F'_c \cdot A$ or alternatively compute $f_{actual} = P/A$
7. Is the design satisfactory?
 Is $P \leq P_{allowable}$? \Rightarrow yes, it is; no, it is no good
 or Is $f_{actual} \leq F'_c$? \Rightarrow yes, it is; no, it is no good

Procedure for Design

1. Guess a size by picking a section
2. Calculate L_e/d_{min}
3. Obtain F'_c
 compute $F_{cE} = \frac{K_{cE} E}{(l_e/d)^2}$ with $K_{cE} = 0.3$ for sawn, = 0.418 for glu-lam
4. Compute $F_c^* \cong F_c C_D$ with $C_D = 1$, normal, $C_D = 1.25$ for 7 day roof...
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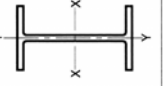
COLUMNS
W shapes
Allowable axial loads in kips



Designation	W12											
	106		96		87		79		72		65	
Wt. ft.	36	50	36	50	36	50	36	50	36	50	36	50
F_y	674	936	609	846	553	768	501	696	456	633	413	573
0	637	872	575	788	522	715	473	647	430	589	389	533
6	629	858	568	775	515	703	467	637	424	579	384	524
7	620	844	560	762	508	691	460	626	418	569	378	514
8	611	828	552	748	501	678	453	614	412	558	373	504
9	602	812	544	733	493	665	446	601	406	547	367	494
10	593	795	535	718	485	650	439	588	399	535	361	483
11	583	777	526	701	477	636	431	575	392	522	354	472
12	572	759	516	685	468	620	423	561	385	509	348	460
13	561	740	506	667	459	604	415	546	377	496	341	448
14	550	720	496	649	450	588	407	531	369	482	334	435
15	539	699	486	630	440	570	398	515	361	468	326	422
16	527	678	475	611	430	553	389	499	353	453	319	408
17	514	656	464	591	420	534	379	482	344	434	311	394
18	502	634	452	570	409	515	370	465	336	422	303	380
19	489	611	440	549	398	496	360	447	326	406	294	365
20	476	589	428	528	386	475	349	428	315	386	285	346
21	463	567	416	507	375	454	338	409	304	365	274	327
22	450	545	404	486	364	433	327	390	293	344	263	308
23	437	523	392	465	353	412	316	371	282	323	252	289
24	424	501	380	444	342	391	305	352	271	302	241	270
25	411	479	368	423	331	370	298	331	260	281	230	251
26	400	457	356	402	320	349	287	310	249	260	220	230
27	387	435	344	381	309	328	276	290	238	240	210	210
28	375	413	332	360	298	307	265	270	227	220	200	200
29	363	391	320	339	287	286	254	250	216	200	190	190
30	351	369	308	318	276	265	243	230	205	180	180	180
31	339	347	296	297	265	244	230	219	197	170	170	170
32	327	325	284	276	254	223	219	194	175	156	156	156
33	315	303	272	257	243	202	193	173	156	139	139	139
34	303	281	260	239	232	191	173	155	140	125	125	125
35	291	259	248	218	221	180	173	155	140	125	125	125
36	279	237	236	206	209	169	173	155	140	125	125	125
37	267	215	224	185	202	158	173	155	140	125	125	125
38	255	193	212	163	199	147	173	155	140	125	125	125
39	243	171	200	141	196	136	173	155	140	125	125	125
40	231	149	188	119	196	125	173	155	140	125	125	125

Sample AISC Table for LRFD Design Strength in Compression

Table 4-2 (cont.).
W-Shapes
Design Strength in Axial Compression, $\phi_c P_n$, kips



Shape	W12x											
	105	96	87	79	72	65T	58	53	50	45	40	
0	1330	1200	1090	986	897	812	723	663	621	557	497	
6	1280	1150	1050	947	861	779	680	623	562	504	450	
7	1260	1140	1030	933	848	767	666	610	543	486	434	
8	1240	1120	1010	917	834	754	649	594	521	466	416	
9	1210	1100	994	900	818	739	631	577	497	445	396	
10	1190	1070	973	880	800	723	611	559	472	422	376	
11	1160	1050	950	860	781	706	590	539	445	398	354	
12	1130	1020	926	838	761	687	568	518	418	374	332	
13	1100	995	901	814	740	668	545	496	390	349	310	
14	1070	966	874	790	717	647	521	474	363	324	287	
15	1040	935	846	764	694	626	496	451	335	299	265	
16	1000	904	817	738	670	604	471	428	308	274	243	
17	968	871	788	711	645	581	446	404	281	250	222	
18	932	838	758	683	620	558	420	381	255	227	201	
19	895	805	727	655	594	535	395	357	230	204	181	
20	858	771	696	627	566	512	370	334	208	185	163	
22	783	703	634	570	517	464	322	290	172	152	135	
24	708	635	572	514	465	417	276	247	144	128	113	
26	635	569	511	459	415	372	235	210	123	109	96.5	
28	565	505	453	406	367	328	202	181	106	94.1	83.2	
30	497	443	397	355	321	287	176	158	92.3	82.0	72.5	
32	437	390	349	312	282	252	155	139	81.2	72.1	63.7	
34	387	345	309	277	250	223	137	123	110	98.4	88.9	
36	345	308	276	247	223	199	122	110	98.4	88.9	80.9	
38	310	276	248	221	200	179	110	98.4	88.9	80.9	73.5	
40	279	249	223	200	181	161	99.2	88.9	80.9	73.5	66.7	

Properties

P_n , kips	242	206	182	156	137	117	112	101	105	90.5	75.2
P_n , kips/in.	30.5	27.5	25.8	23.5	21.5	19.5	18.0	17.3	18.5	16.8	14.8
P_n , kips	609	445	365	278	213	159	125	110	133	98.6	67.4
P_n , kips	276	228	185	152	126	103	115	93.0	115	93.0	74.6
L_p , ft	11.0	10.9	10.8	10.8	10.7	11.9	8.87	8.76	6.92	6.89	6.85
L_r , ft	44.9	41.4	38.4	35.7	33.6	31.7	27.0	25.6	21.5	20.3	19.2
A_g , in ²	31.2	26.2	25.6	23.2	21.1	19.1	17.0	15.6	14.6	13.1	11.7
r_x , in.	9.33	8.33	7.40	6.62	5.97	5.33	4.75	4.25	3.91	3.48	3.07
r_y , in.	3.01	2.70	2.41	2.16	1.95	1.74	1.57	1.40	1.26	1.13	1.00
r_x/r_y	3.11	3.09	3.07	3.05	3.04	3.02	2.51	2.48	1.96	1.95	1.94
Ratio r_x/r_y	1.76	1.76	1.75	1.75	1.75	1.75	2.10	2.11	2.64	2.64	2.64
$P_n/(K L)^2/10^4$	26700	23600	21200	18900	17100	15300	13600	12200	11200	9960	8790
$P_n/(K L)^2/10^4$	8620	7730	6900	6180	5580	4980	3060	2740	1610	1430	1260

Flange is non-compact. K/r equal to or greater than 200.

Example 1 (pg 367)

Example Problem 10.10 (Figure 10.41)

A 24-ft.-tall, A572 grade 50, steel column (W14×82) with an $F_y = 50$ ksi has pins at both ends. Its weak axis is braced at midheight, but the column is free to buckle the full 24 ft. in the strong direction. Determine the safe load capacity for this column.

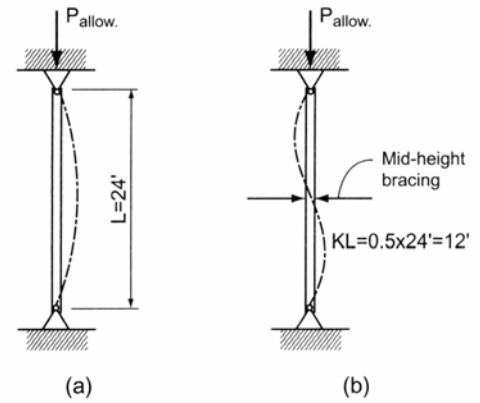


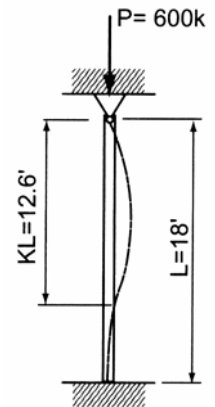
Figure 10.41 (a) Strong axis buckling.
(b) Weak axis buckling.

Example 2 (pg 371) + chart method

Example Problem 10.14: Design of Steel Columns (Figure 10.48)

Select the most economical W12 × column 18' in height to support an axial load of 600 kips using A572 grade 50 steel. Assume that the column is hinged at the top but fixed at the base.

ALSO: Select the column using the ASD design charts, and the LRFD charts assuming that the load is a dead load (factor of 1.4)



Example 3 (pg 379)

Example Problem 10.18 (Figures 10.60 and 10.61)

An 18' tall 6x8 Southern pine column supports a roof load (dead load plus a 7-day live load) equal to 16 kips. The weak axis of buckling is braced at a point 9'6" from the bottom support. Determine the adequacy of the column.

$$F_c = 975 \text{ psi}, E = 1.6 \times 10^6 \text{ psi}$$

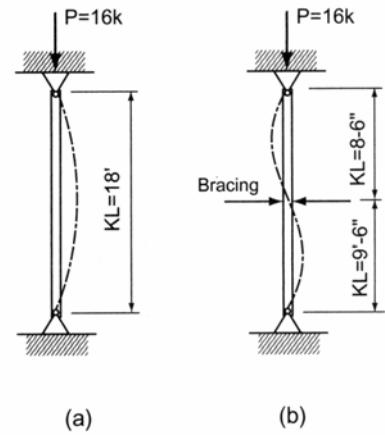
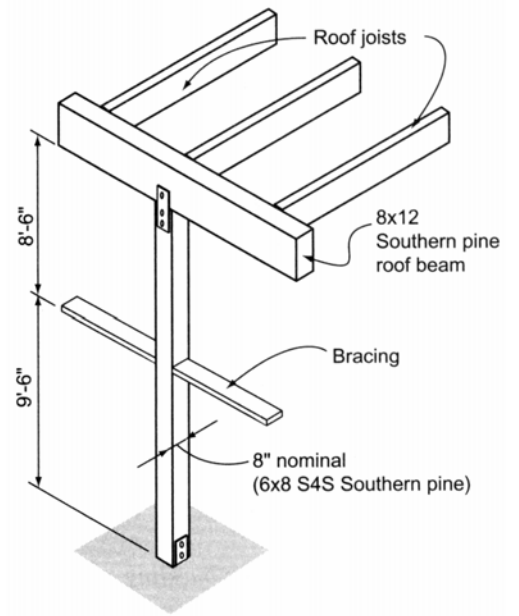


Figure 10.61 (a) Strong axis. (b) Weak axis.

Example 4 (pg 381)**Example Problem 10.20:
Design of Wood Columns(Figure 10.66)**

A 22'-tall glu-lam column is required to support a roof load (including snow) of 40 kips. Assuming $8\frac{3}{4}$ " in one dimension (to match the beam width above), determine the minimum column size if the top and bottom are pin supported.

Select from the following sizes:

$$8\frac{3}{4}" \times 9" (A = 78.75 \text{ in.}^2)$$

$$8\frac{3}{4}" \times 10\frac{1}{2}" (A = 91.88 \text{ in.}^2)$$

$$8\frac{3}{4}" \times 12" (A = 105.00 \text{ in.}^2)$$

