

APPLIED ARCHITECTURAL STRUCTURES:  
STRUCTURAL ANALYSIS AND SYSTEMS

ARCH 631

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FALL 2013

lecture  
twenty one



<http://nisee.berkeley.edu/godden>

steel construction  
and design

Steel Construction 1  
Lecture 21

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Steel

- cast iron – wrought iron - steel
- cables
- columns
- beams
- trusses
- frames



Steel Construction 2  
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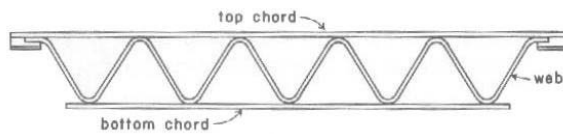
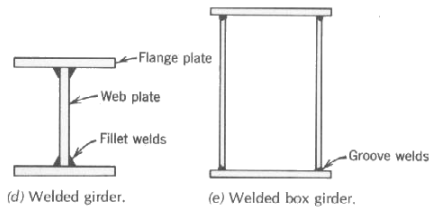
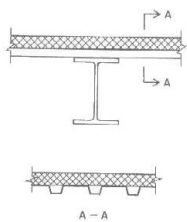
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Steel Construction

- standard rolled shapes
- open web joists
- plate girders
- decking



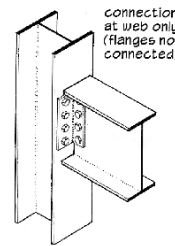
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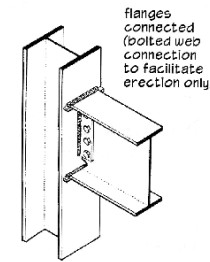
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Steel Construction

- welding
- bolts



SHEAR CONNECTION



MOMENT CONNECTION

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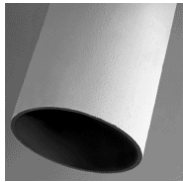


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# Steel Construction

- fire proofing
  - cementitious spray
  - encasement in gypsum
  - intumescent – expands with heat
  - sprinkler system



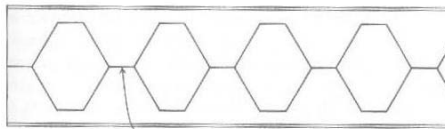
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# Steel Beams

- types
  - manufactured shapes

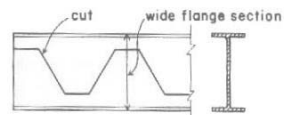


(b)

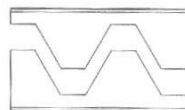


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castellated



(c)



(d)

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# Steel Materials

- high strength to weight ratio
- ductile
- beam size often limited by deflection
- column size limited by slenderness

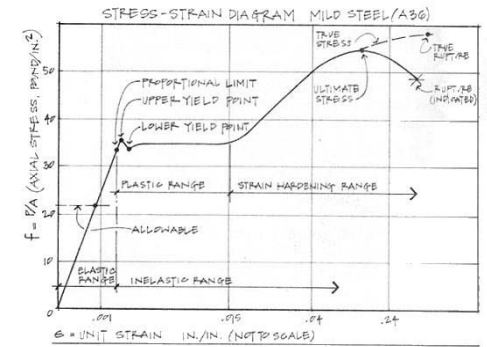


Figure 5.22 Stress-strain diagram for mild steel (A36) with key points highlighted.

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# Steel Beams

- types
  - wide flange



Rollled beam (W section).



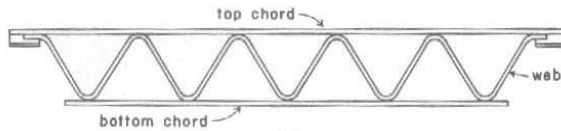
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# Steel Beams

- types
  - open web joists (manufactured trusses)



(2) SECTION THRU JOISTS SHOWING FLANGE TYPES



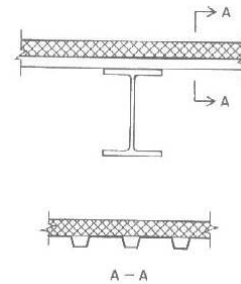
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# Steel Beams

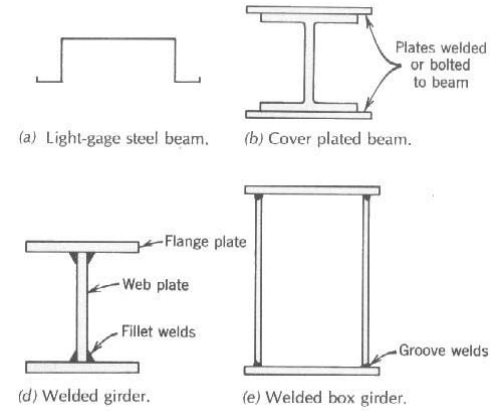
- types (more)
  - plate girder
  - decking



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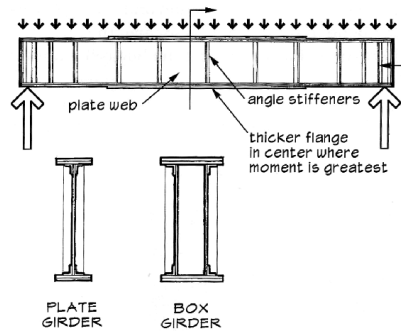
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# Steel Beams



<http://nisee.berkeley.edu/golden>

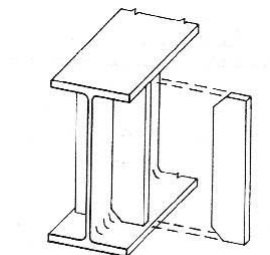


stiffeners at end where shear is greatest and at support

thicker flange in center where moment is greatest

PLATE GIRDER

BOX GIRDER



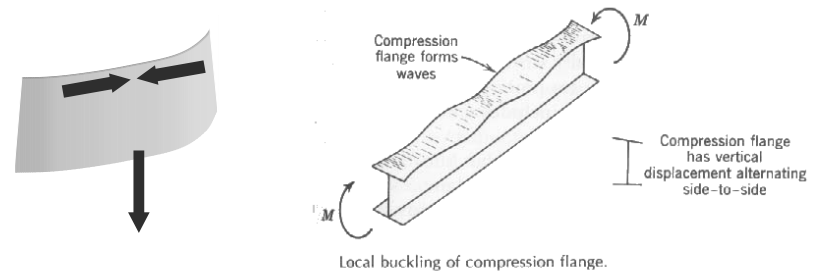
stiffeners to prevent lateral buckling

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# Steel Beams

- lateral stability - bracing
- local buckling - stiffen



Local buckling of compression flange.

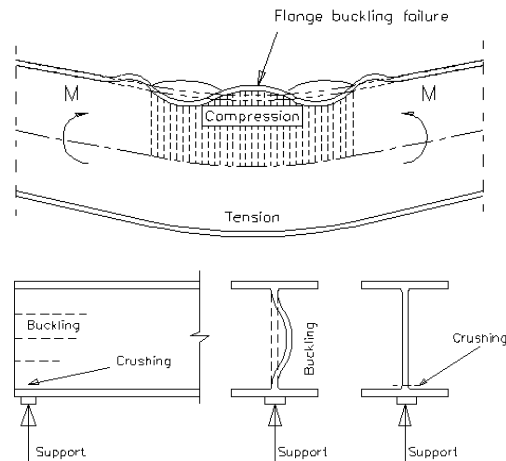
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## Local Buckling

- steel I beams
- flange
  - buckle in direction of smaller radius of gyration
- web
  - force
  - “crippling”



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## Local Buckling

- flange

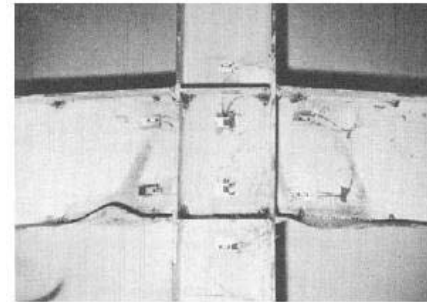


Figure 2-5. Flange Local Bending Limit State  
(Beedle, L.S., Christopher, R., 1964)

- web



Figure 2-7. Web Local Buckling Limit State  
(SAC Project)

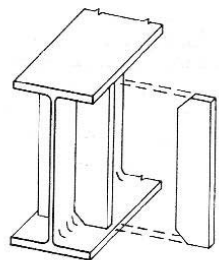
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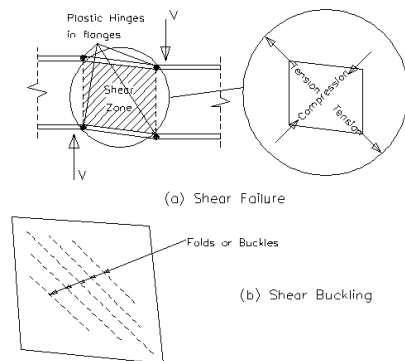
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## Shear in Web

- panels in plate girders or webs with large shear
- buckling in compression direction
- add stiffeners



stiffeners to prevent lateral buckling



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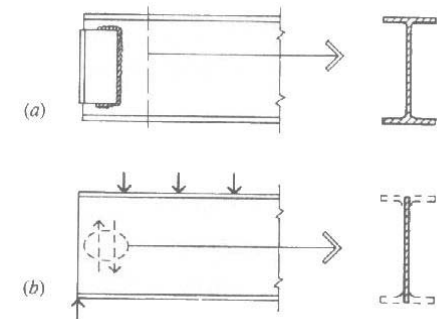
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## Steel Beams

- end conditions

- a) away from connection - full section effective
- b) high shear - only web effective



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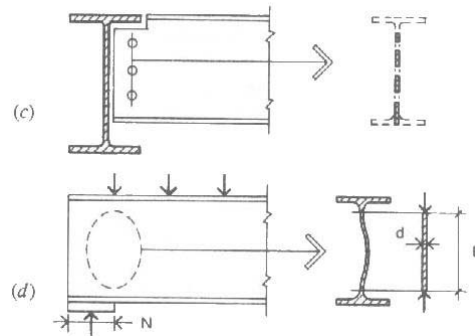
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# Steel Beams

- end conditions

- c) bolt holes – less material
- d) local web buckling



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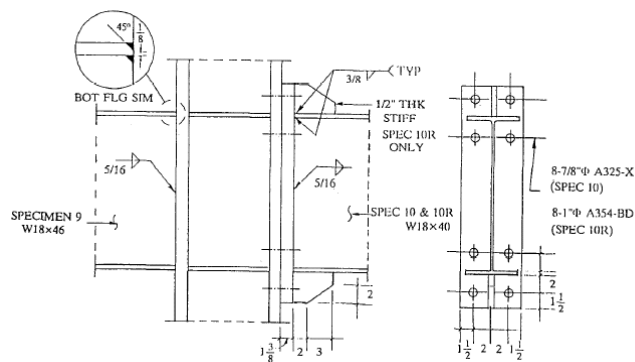
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# Steel Beams

- connections

- welds
- bolts



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# Steel Beams

- bearing

- provide adequate area
- prevent local yield of flange and web

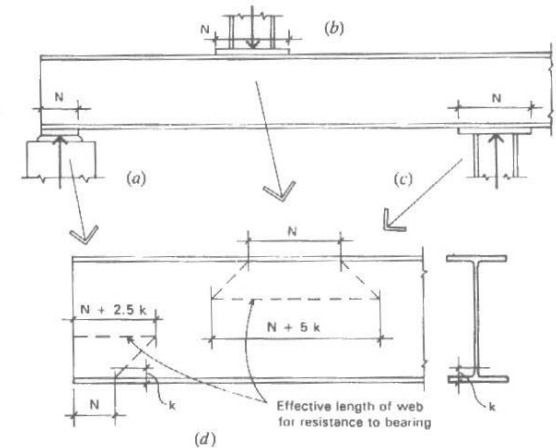


Figure 9.10 Considerations for bearing in beams with thin webs, as related to web crippling (buckling of the thin web in compression).

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# Steel Design – Open Web Joists

- SJI: [www.steeljoist.com](http://www.steeljoist.com)

- Vulcraft: [www.vulcraft.com](http://www.vulcraft.com)

- K Series (Standard)

- 8-30" deep, spans 8-50 ft

- LH Series (Long span)

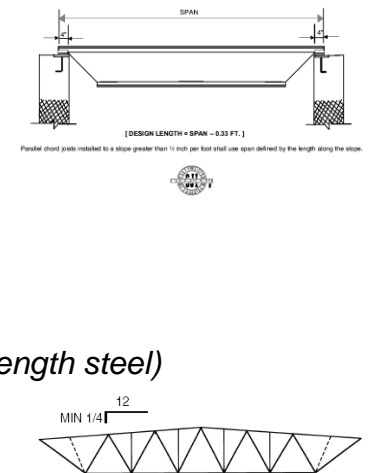
- 18-48" deep, spans 25-96 ft

- DLH (Deep Long Spans)

- 52-72" deep, spans 89-144 ft

- SLH (Long spans with high strength steel)

- pitched top chord
- 80-120" deep, spans 111-240 ft



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# Steel Design – Open Web Joists

STANDARD LOAD TABLE/OPEN WEB STEEL JOISTS, K-SERIES  
Based on a Maximum Allowable Tensile Stress of 30 ksi

| Joist Designation     | 8K1   | 10K1 | 12K1 | 12K3 | 12K5 | 14K1 | 14K3 | 14K4 | 14K6 | 16K2 | 16K3 | 16K4 | 16K5 | 16K6 | 16K7 | 16K9 |
|-----------------------|---|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|
| Depth (in.)           | 8   | 10   | 12   | 12   | 12   | 14   | 14   | 14   | 14   | 16   | 16   | 16   | 16   | 16   | 16   | 16   |
| Approx. Wt (lbs./ft.) | 5.1   | 5.0  | 5.0  | 5.7  | 7.1  | 5.2  | 6.0  | 6.7  | 7.7  | 5.5  | 6.3  | 7.0  | 7.5  | 8.1  | 8.6  | 10.0 |
| Span (ft.)            | load for live load<br>deflection limit in RED<br>total in BLACK |      |      |      |      |      |      |      |      |      |      |      |      |      |      |      |
| 8                     |   |      |      |      |      |      |      |      |      |      |      |      |      |      |      |      |
| 9                     |   |      |      |      |      |      |      |      |      |      |      |      |      |      |      |      |
| 10                    |   |      |      |      |      |      |      |      |      |      |      |      |      |      |      |      |
| 11                    |   |      |      |      |      |      |      |      |      |      |      |      |      |      |      |      |
| 12                    |   |      |      |      |      |      |      |      |      |      |      |      |      |      |      |      |
| 13                    |   |      |      |      |      |      |      |      |      |      |      |      |      |      |      |      |
| 14                    |   |      |      |      |      |      |      |      |      |      |      |      |      |      |      |      |
| 15                    |   |      |      |      |      |      |      |      |      |      |      |      |      |      |      |      |
| 16                    |   |      |      |      |      |      |      |      |      |      |      |      |      |      |      |      |
| 17                    |   |      |      |      |      |      |      |      |      |      |      |      |      |      |      |      |
| 18                    |   |      |      |      |      |      |      |      |      |      |      |      |      |      |      |      |
| 19                    |   |      |      |      |      |      |      |      |      |      |      |      |      |      |      |      |
| 20                    |   |      |      |      |      |      |      |      |      |      |      |      |      |      |      |      |
| 21                    |   |      |      |      |      |      |      |      |      |      |      |      |      |      |      |      |
| 22                    |   |      |      |      |      |      |      |      |      |      |      |      |      |      |      |      |
| 23                    |   |      |      |      |      |      |      |      |      |      |      |      |      |      |      |      |

# Steel Design – Open Web Joists

## LRFD

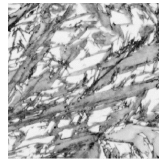
| STANDARD LOAD TABLE FOR OPEN WEB STEEL JOISTS, K-SERIES<br>Based on a 50 ksi Maximum Yield Strength - Loads Shown in Pounds per Linear Foot (plf) |   |      |      |      |      |      |      |      |      |      |      |      |      |      |      |      |
|---|---|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|
| Joist Designation   | 8K1   | 10K1 | 12K1 | 12K3 | 12K5 | 14K1 | 14K3 | 14K4 | 14K6 | 16K2 | 16K3 | 16K4 | 16K5 | 16K6 | 16K7 | 16K9 |
| Depth (in.)   | 8   | 10   | 12   | 12   | 12   | 14   | 14   | 14   | 14   | 16   | 16   | 16   | 16   | 16   | 16   | 16   |
| Approx. Wt (lbs./ft.)   | 5.1   | 5.0  | 5.0  | 5.7  | 7.1  | 5.2  | 6.0  | 6.7  | 7.7  | 5.5  | 6.3  | 7.0  | 7.5  | 8.1  | 8.6  | 10.0 |
| Span (ft.)  | load for live load deflection<br>limit (L/360) in RED<br>total in BLACK |      |      |      |      |      |      |      |      |      |      |      |      |      |      |      |
| 8   |   |      |      |      |      |      |      |      |      |      |      |      |      |      |      |      |
| 9   |   |      |      |      |      |      |      |      |      |      |      |      |      |      |      |      |
| 10  |   |      |      |      |      |      |      |      |      |      |      |      |      |      |      |      |
| 11  |   |      |      |      |      |      |      |      |      |      |      |      |      |      |      |      |
| 12  |   |      |      |      |      |      |      |      |      |      |      |      |      |      |      |      |
| 13  |   |      |      |      |      |      |      |      |      |      |      |      |      |      |      |      |
| 14  |   |      |      |      |      |      |      |      |      |      |      |      |      |      |      |      |
| 15  |   |      |      |      |      |      |      |      |      |      |      |      |      |      |      |      |
| 16  |   |      |      |      |      |      |      |      |      |      |      |      |      |      |      |      |
| 17  |   |      |      |      |      |      |      |      |      |      |      |      |      |      |      |      |
| 18  |   |      |      |      |      |      |      |      |      |      |      |      |      |      |      |      |
| 19  |   |      |      |      |      |      |      |      |      |      |      |      |      |      |      |      |
| 20  |   |      |      |      |      |      |      |      |      |      |      |      |      |      |      |      |
| 21  |   |      |      |      |      |      |      |      |      |      |      |      |      |      |      |      |
| 22  |   |      |      |      |      |      |      |      |      |      |      |      |      |      |      |      |
| 23  |   |      |      |      |      |      |      |      |      |      |      |      |      |      |      |      |

# Steel Beam Design

- American Institute of Steel Construction

- steel grades

- ASTM A36 – carbon
  - plates, angles
  - $F_y = 36 \text{ ksi}$  &  $F_u = 58 \text{ ksi}$



- ASTM A572 – high strength low-alloy
  - some beams
  - $F_y = 60 \text{ ksi}$  &  $F_u = 75 \text{ ksi}$
- ASTM A992 – for building framing
  - most beams
  - $F_y = 50 \text{ ksi}$  &  $F_u = 65 \text{ ksi}$

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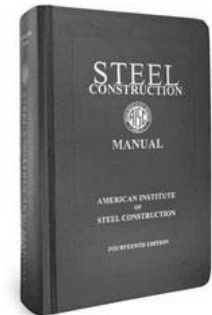
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# Steel Beam Design

- AISC: 14<sup>th</sup> ed.

- combined ASD & LRFD in one volume in 2005



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# LRFD Load Combinations

ASCE-7  
(2010)

- 1.4D
- 1.2D + 1.6L + 0.5(L<sub>r</sub> or S or R)
- 1.2D + 1.6(L<sub>r</sub> or S or R) + (L or 0.5W)
- 1.2D + 1.0W + L + 0.5(L<sub>r</sub> or S or R)
- 1.2D + 1.0E + L + 0.2S
- 0.9D + 1.0W
- 0.9D + 1.0E
  - F has same factor as D in 1-5 and 7
  - H adds with 1.6 and resists with 0.9 (permanent)



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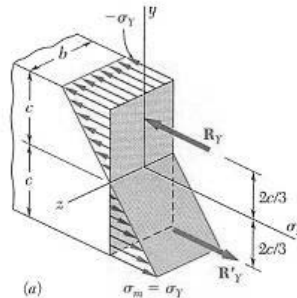
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## Internal Moments - at yield

- material hasn't failed

$$M_y = \frac{I}{c} f_y = \frac{bh^2}{6} f_y$$

$$= \frac{b(2c)^2}{6} f_y = \frac{2bc^2}{3} f_y$$



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# Pure Flexure

$$\sum \gamma_i R_i = M_u \leq \phi_b M_n = 0.9 F_y Z$$

$M_u$  - maximum moment

$\phi_b$  - resistance factor for bending = 0.9

$M_n$  - nominal moment (ultimate capacity)

$F_y$  - yield strength of the steel

$Z$  - plastic section modulus\*

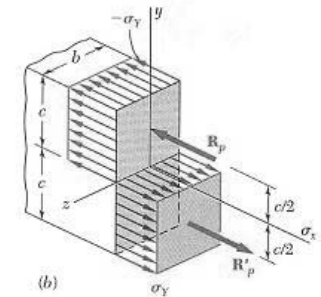
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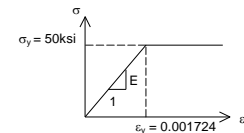
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## Internal Moments - ALL at yield

- all parts reach yield
- plastic hinge forms
- ultimate moment
- $A_{tension} = A_{compression}$



$$M_p = bc^2 f_y = \frac{3}{2} M_y$$



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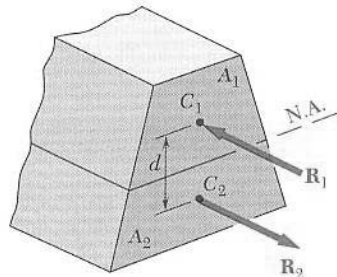
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## n.a. of Section at Plastic Hinge

- cannot guarantee at centroid
- $f_y \cdot A_1 = f_y \cdot A_2$
- moment found from yield stress times moment area



$$M_p = f_y A_1 d = f_y \sum_{n.a} A_i d_i$$

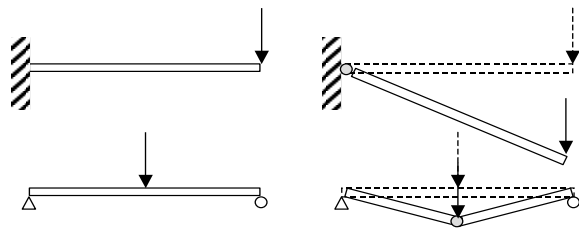
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## Plastic Hinge Examples

- stability can be effected

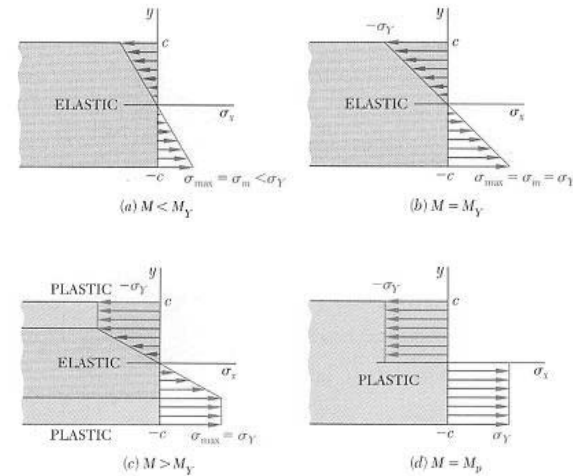


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## Plastic Hinge Development



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## Plastic Section Modulus

- shape factor,  $k$

$$k = \frac{M_p}{M_y}$$

= 3/2 for a rectangle

≈ 1.1 for an I



$$k = \frac{Z}{S}$$

- plastic modulus,  $Z$

$$Z = \frac{M_p}{f_y}$$

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## Shear

$$\sum \gamma_i R_i = V_u \leq \phi_v V_n = 1.0(0.6 F_{yw} A_w)$$

$V_u$  - maximum shear

$\phi_v$  - resistance factor for shear = 1.0

$V_n$  - nominal shear

$F_{yw}$  - yield strength of the steel in the web

$A_w$  - area of the web =  $t_w d$

## Compact Sections

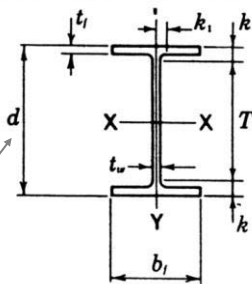
- plastic moment can form before any buckling

- criteria

$$-\frac{b_f}{2t_f} \leq 0.38 \sqrt{\frac{E}{F_y}}$$

$$-\text{and } \frac{h_c}{t_w} \leq 3.76 \sqrt{\frac{E}{F_y}}$$

TABLE A.3 Properties of W Shapes



## Flexure Design

- limit states for beam failure

1. yielding

2. lateral-torsional buckling\*

3. flange local buckling

4. web local buckling

- minimum  $M_n$  governs

$$\sum \gamma_i R_i = M_u \leq \phi_b M_n$$

$$L_p = 1.76 r_y \sqrt{\frac{F_y}{E}}$$

## Lateral Torsional Buckling

$$M_n = C_b \left[ \begin{array}{l} \text{moment based on} \\ \text{lateral buckling} \end{array} \right] \leq M_p$$

$$C_b = \frac{12.5 M_{max}}{2.5 M_{max} + 3 M_A + 4 M_B + 3 M_C}$$

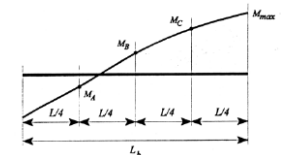
$C_b$  = modification factor

$M_{max}$  - |max moment|, unbraced segment

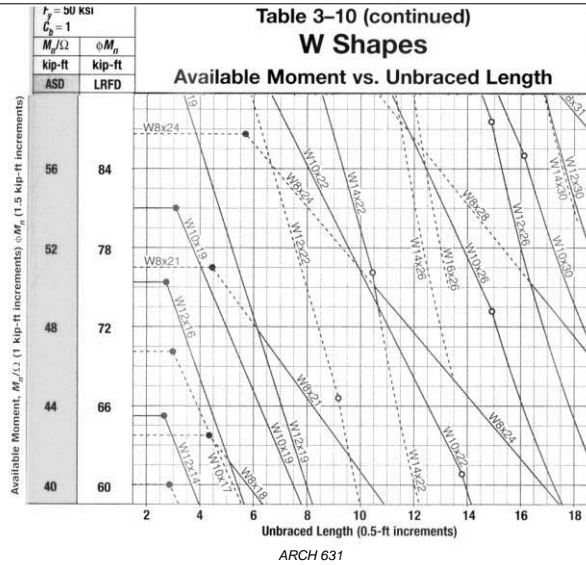
$M_A$  - |moment|, 1/4 point

$M_B$  = |moment|, center point

$M_C$  = |moment|, 3/4 point



# Beam Design Charts



Steel Constru  
Lecture 21

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# Deflection Limits

- based on service condition
- no "impairment" to serviceability
- avoid ponding
- $L/360$  due to live load for beams & girders supporting plaster (service)

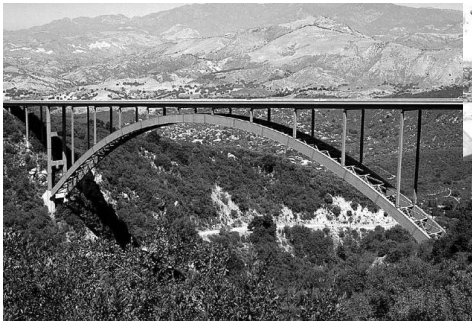
Steel Construction 40  
Lecture 20

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# Steel Arches and Frames

- solid sections or open web



<http://nisee.berkeley.edu/godden>

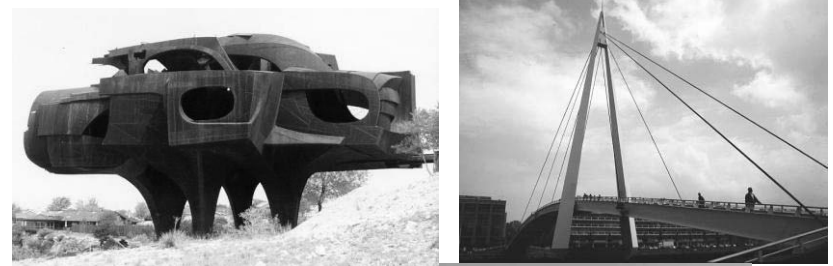


Steel Construction 41  
Lecture 21

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# Steel Shell and Cable Structures

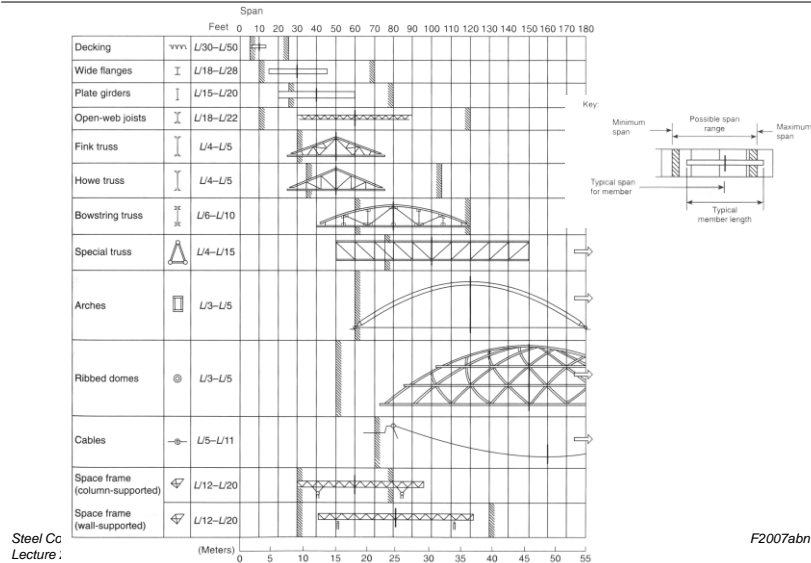


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Lecture 20

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## Approximate Depths



## Unified Column Design

- limit states for failure

$$\phi_c = 0.90$$

$$P_n = F_{cr} A_g$$

$$P_a \leq \frac{P_n}{\Omega}$$

$$P_u \leq \phi_c P_n$$

- yielding  $\frac{KL}{r} \leq 4.71 \sqrt{\frac{E}{F_y}}$  or  $F_e \geq 0.44F_y$
  - buckling  $\frac{KL}{r} > 4.71 \sqrt{\frac{E}{F_y}}$  or  $F_e < 0.44F_y$
- $F_e$  – elastic buckling stress (Euler)

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## Unified Column Design

- $P_n = F_{cr} A_g$
- for  $\frac{KL}{r} \leq 4.71 \sqrt{\frac{E}{F_y}}$   $F_{cr} = \left[ 0.658 \frac{F_y}{F_e} \right] F_y$
- for  $\frac{KL}{r} > 4.71 \sqrt{\frac{E}{F_y}}$   $F_{cr} = 0.877 F_e$
- where  $F_e = \frac{\pi^2 E}{\left(\frac{KL}{r}\right)^2}$

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## Procedure for Analysis

- calculate  $KL/r$ 
  - biggest of  $KL/r$  with respect to x axes and y axis
- find  $F_{cr}$  from appropriate equation
  - tables are available
- compute  $P_n = F_{cr} A_g$ 
  - or find  $f_c = P_d/A$  or  $P_u/A$
- is  $P_a \leq P_n/\Omega$  or  $P_u \leq \phi P_n$ ?
  - yes: ok
  - no: insufficient capacity and no good

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## Procedure for Design

1. guess a size (pick a section)
2. calculate  $KL/r$ 
  - biggest of  $KL/r$  with respect to x axes and y axis
3. find  $F_{cr}$  from appropriate equations
  - or find a table
4. compute  $P_n = F_{cr} A_g$ 
  - or find  $f_c = P_a/A$  or  $P_u/A$

## Procedure for Design (cont'd)

5. is  $P_a \leq P_n/\Omega$  or  $P_u \leq \phi P_n$ ?
  - yes: ok
  - no: pick a bigger section and **go back to step 2.**
6. check design efficiency
  - percentage of stress =  $\frac{P_r}{P_c} \cdot 100\%$
  - if between 90-100%: good
  - if < 90%: pick a smaller section and **go back to step 2.**

## Column Tables

| Table 4-1 (continued)<br>Available Strength in<br>Axial Compression, kips<br>W Shapes                    |       |                |      |              |      |                |      |              |      |                |      |              |      |
|--|-------|----------------|------|--------------|------|----------------|------|--------------|------|----------------|------|--------------|------|
| $F_y = 50$ ksi<br> W12 |       | W12x           |      |              |      |                |      |              |      |                |      |              |      |
|  |       | 96             |      | 87           |      | 79             |      | 72           |      | 65             |      |              |      |
| Shape  | Wt/ft | $P_n/\Omega_c$ |      | $\phi_c P_n$ |      | $P_n/\Omega_c$ |      | $\phi_c P_n$ |      | $P_n/\Omega_c$ |      | $\phi_c P_n$ |      |
|  |       | ASD            | LRFD | ASD          | LRFD | ASD            | LRFD | ASD          | LRFD | ASD            | LRFD | ASD          | LRFD |
| Radius of gyration $r_y$   | 0     | 844            | 1270 | 766          | 1150 | 694            | 1040 | 633          | 951  | 571            | 859  |              |      |
|  | 6     | 811            | 1220 | 735          | 1110 | 667            | 1000 | 607          | 913  | 548            | 824  |              |      |
|  | 7     | 800            | 1200 | 725          | 1090 | 657            | 987  | 598          | 899  | 540            | 811  |              |      |
|  | 8     | 787            | 1180 | 713          | 1070 | 646            | 971  | 588          | 884  | 531            | 798  |              |      |
|  | 9     | 772            | 1160 | 699          | 1050 | 634            | 952  | 577          | 867  | 520            | 782  |              |      |
|  | 10    | 756            | 1140 | 685          | 1030 | 620            | 932  | 565          | 849  | 509            | 765  |              |      |
| 11   | 739   | 1110           | 669  | 1010         | 606  | 910            | 551  | 828          | 497  | 747            |      |              |      |

## Beam-Column Design

- moment magnification ( $P-\Delta$ )

$$M_u = B_1 M_{max-factored} \quad B_1 = \frac{C_m}{1 - (P_u/P_{e1})}$$

$C_m$  – modification factor for end conditions  
 = 0.6 – 0.4( $M_1/M_2$ ) or  
 0.85 restrained, 1.00 unrestrained

$P_{e1}$  – Euler buckling strength  $P_{e1} = \frac{\pi^2 EA}{\left(\frac{KL}{r}\right)^2}$

## Beam-Column Design

- **LRFD (Unified) Steel**

- for  $\frac{P_r}{P_c} \geq 0.2$ :  $\frac{P_u}{\phi_c P_n} + \frac{8}{9} \left( \frac{M_{ux}}{\phi_b M_{nx}} + \frac{M_{uy}}{\phi_b M_{ny}} \right) \leq 1.0$

- for  $\frac{P_r}{P_c} < 0.2$ :  $\frac{P_u}{2\phi_c P_n} + \left( \frac{M_{ux}}{\phi_b M_{nx}} + \frac{M_{uy}}{\phi_b M_{ny}} \right) \leq 1.0$

$P_r$  is required,  $P_c$  is capacity

$\phi_c$  - resistance factor for compression = 0.9

$\phi_b$  - resistance factor for bending = 0.9

## Construction Supervision

- **proper grade material**
  - high strength bolts
- **quality welds**
- **proper bolted conditions (ex. sc)**
- **fabrication and erection of steel frame connection details**

