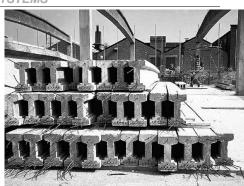
#### **APPLIED ACHITECTURAL STRUCTURES:**

STRUCTURAL ANALYSIS AND SYSTEMS

ARCH 631 DR. Anne Nichols Fall 2013

lecture ten



# reinforced concrete construction

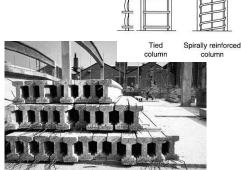
Reinforced Concrete Construction 1 Lecture 10 Applied Architectural Structures ARCH 631 F2012abn

http://nisee.berkeley.edu/godder

### Concrete Construction

- cast-in-place
- tilt-up
- prestressing
- post-tensioning





#### Reinforced Concrete Construction 3 Lecture 10

Architectural Structures III ARCH 631 F2009abn



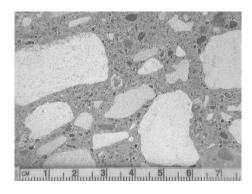
Reinforced Concrete Construction 2 Lecture 10

Architectural Structures III ARCH 631

F2009abn

#### Concrete Materials

- · low strength to weight ratio
- relatively inexpensive
  - Portland cement
  - aggregate
  - water



Reinforced Concrete Construction 4 Lecture 9 Architectural Structures III ARCH 631

### Concrete Materials

- reinforcement
  - deformed bars
  - prestressing strand
  - stirrups
  - development length
  - anchorage
  - splices





http://nisee.berkeley.edu/godden

F2009abr

#### Concrete Materials

- fire resistance
  - most fire-resistive structural material
  - low rate of penetration
  - retains strength if exposure not too long
    - stable to 900 1200 °F internally
    - loses 50% after that
  - no toxic fumes
  - cover necessary to protect steel

Architectural Structures III

ARCH 631

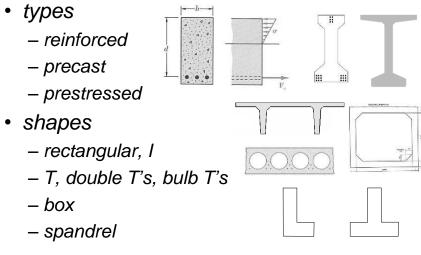
<b>UCAL</b> I	

F2007abn

Reinforced Concrete Construction 5
Lecture 10

Architectural Structures III ARCH 631

Concrete Beams



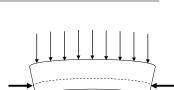
#### Concrete Beams

deformation

Reinforced Concrete Construction 6

Lecture 9

- camber (elastic)
  - hogging
  - sagging
- shrinkage strain
- creep strain
  - 2~3 times elastic strain
  - about 2-3 years



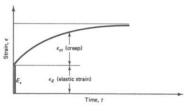


Figure 2.7 Strain-time curve.

Reinforced Concrete Construction 7 Lecture 9

Architectural Structures III ARCH 631

F2007abr

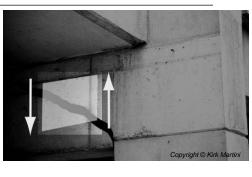
Reinforced Concrete Construction 8 Lecture 9

2

- - 200-400 x 10<sup>-6</sup>
  - · about 2-3 years

#### Concrete Beams

- shear
  - vertical
  - horizontal
  - combination:
    - tensile stresses at 45°
- bearing
  - crushing



F2009abr

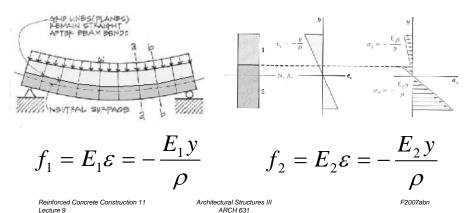
Lecture 10

Reinforced Concrete Construction 9

Architectural Structures III ARCH 631

#### Behavior of Composite Members

- plane sections remain plane
- stress distribution changes



#### Concrete Beam Design

- composite of concrete and steel
- American Concrete Institute (ACI)
  - design for failure
  - strength design (LRFD)
    - service loads x load factors
    - concrete holds no tension
    - failure criteria is yield of reinforcement
    - failure capacity x reduction factor
    - factored loads < reduced capacity</li>
  - concrete strength =  $f'_c$

Reinforced Concrete Construction 10 Lecture 9

```
Architectural Structures III
ARCH 631
```

F2007abn

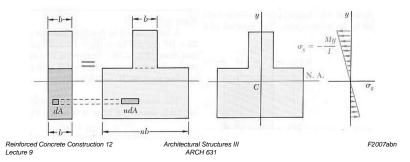
international

#### Transformation of Material

• n is the ratio of E's

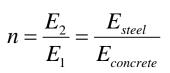
$$n=\frac{E_2}{E_1}$$

• effectively widens a material to get same stress distribution

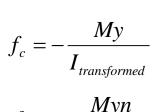


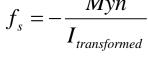
#### Stresses in Composite Section

 with a section transformed to one material, new I



- stresses in that material are determined as usual
- stresses in the other material need to be adjusted by n



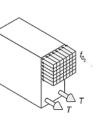


F2007abn

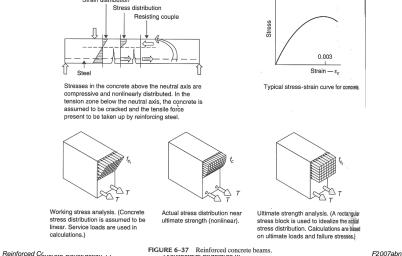
Reinforced Concrete Construction 13 Lecture 9 Architectural Structures III ARCH 631

#### Reinforced Concrete Analysis

- · for stress calculations
  - steel is transformed to concrete
  - concrete is in compression above n.a. and represented by an equivalent <u>stress block</u>
  - concrete takes no tension
  - steel takes tension
  - force ductile failure



#### Strain distribution Stress distribution



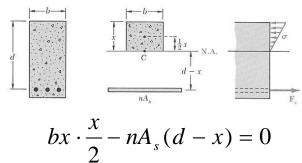
ARCH 631

Reinforced Concrete - stress/strain

#### Location of n.a.

Lecture 9

- ignore concrete below n.a.
- transform steel
- same area moments, solve for x

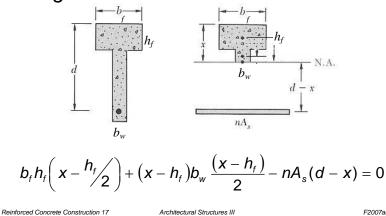


Reinforced Concrete Construction 15 Lecture 9 F2007abn

Reinforced Concrete Construction 16 Lecture 9 Architectural Structures III ARCH 631

#### T sections

• n.a. equation is different if n.a. below flange



### ACI Load Combinations\*

- 1.4D
- $1.2D + 1.6L + 0.5(L_r \text{ or } S \text{ or } R)$
- $1.2D + 1.6(L_r \text{ or } S \text{ or } R) + (1.0L \text{ or } 0.5W)$

Applied Architectural Structures

ARCH 631

- $1.2D + 1.0W + 1.0L + 0.5(L_r \text{ or } S \text{ or } R)$
- 1.2D + 1.0E + 1.0L + 0.2S
- 0.9D + 1.0W
- 0.9D + 1.0E

Reinforced Concrete Construction 18

Lecture 10



<sup>\*</sup>can also use old ACI factors

F2012abn

ARCH 631

F2007abn

#### Reinforcement

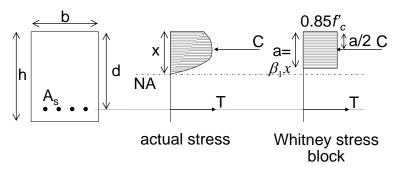
- deformed steel bars (rebar)
  - Grade 40,  $F_{y} = 40$  ksi
  - Grade 60,  $F_{y} = 60$  ksi most common
  - Grade 75,  $F_{y} = 75$  ksi
  - US customary in # of 1/8"  $\phi$
- longitudinally placed
  - bottom
  - top for compression reinforcement
  - spliced, hooked, terminated...

Reinforced Concrete Construction 19 Lecture 9 Architectural Structures III ARCH 631

F2007abn

# Reinforced Concrete Design

• stress distribution in bending



Wang & Salmon, Chapter 3

Reinforced Concrete Construction 20 Lecture 9 Architectural Structures III ARCH 631

Lecture 9

#### Force Equations

- $C = 0.85 f'_{c} ba$
- $T = A_s f_y$
- where

 $\begin{array}{c} \mathbf{a} = \\ \beta_1 x \\ \end{array}$ 

0.85*f*'<sub>c</sub>

\$a/2

F2007abn

- $-f'_{c} = concrete compressive strength$
- -a = height of stress block
- -b = width of stress block
- $-f_v = steel yield strength$
- $-A_s = area of steel reinforcement$

Reinforced Concrete Construction 21 Lecture 9 Architectural Structures III ARCH 631

#### Over and Under-reinforcement

- over-reinforced
   steel won't yield
- under-reinforced
  - steel will yield
- reinforcement ratio
  - $-\rho = \frac{A_s}{bd}$
  - use as a design estimate to find  $A_s$ , b, d
  - max  $\rho$  is found with  $\varepsilon_{\text{steel}} \ge 0.004$  (not  $\rho_{\text{bal}}$ )

Reinforced Concrete Construction 23 Lecture 9 www.thfrc.go



• T = C•  $M_n = T(d-a/2)$ -  $d = depth to the steel n.a. d <math>a = \int_{\beta_1 x} \int_{\beta_1 x} \frac{1}{\beta_1 x} C$ • with  $A_s$ 

 $-a = \frac{A_s f_y}{0.85 f_s b}$ 

 $-M_{u} \le \phi M_{n} \quad \phi = 0.9 \text{ for flexure} \\ -\phi M_{n} = \phi T(d-a/2) = \phi A_{s}f_{y} (d-a/2)$ 

Reinforced Concrete Construction 22 Lecture 10

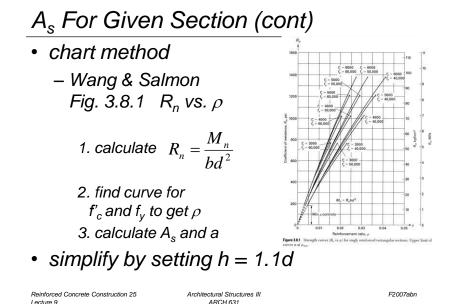
Architectural Structures III ARCH 631 F2008abn

## A<sub>s</sub> for a given Section

- several methods - guess a and iterate 1. guess a (less than n.a.) 2.  $A_s = \frac{0.85f'_cba}{f_y}$ 3. solve for a from  $M_u = \phi A_s f_y \left( d - \frac{a}{2} \right)$   $a \downarrow 0.85f'_ca/2 \\ A_{s-1} \downarrow a/2 \\ A_{s-1} \downarrow a$ 
  - 4. repeat from 2. until a from 3. matches a in 2.

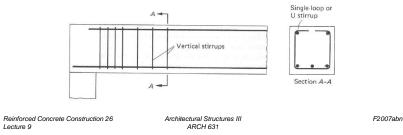
Reinforced Concrete Construction 24 Lecture 9 Architectural Structures III ARCH 631





#### Shear in Concrete Beams

- flexure combines with shear to form diagonal cracks
- horizontal reinforcement doesn't help
- stirrups = vertical reinforcement



#### ACI Shear Values

- $V_u$  is at distance d from face of support
- shear capacity:  $V_c = \upsilon_c \times b_w d$ – where  $b_w$  means thickness of <u>web</u> at n.a.
- shear stress (beams)

$$- \upsilon_c = 2\sqrt{f'_c} \qquad \phi = 0.75 \text{ for shear}$$
  

$$\phi V_c = \phi 2\sqrt{f'_c} b_w d \qquad f'_c \text{ is in } \underline{psi}$$

- shear strength:
  - $-V_s$  is strength from stirrup reinforcement

 $V_{\mu} \leq \phi V_{c} + \phi V_{s}$ 

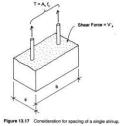
ACI 11.3, 11.12 Reinforced Concrete Construction 27 Lecture 9

Architectural Structures III ARCH 631 F2007abn

### Stirrup Reinforcement

• shear capacity:  $V_s = \frac{A_v f_y d}{s}$ 

 $-A_{\nu}$  = area in all legs of stirrups



- -s = spacing of stirrup
- may need stirrups when concrete has enough strength!

Reinforced Concrete Construction 28 Lecture 9 Architectural Structures III ARCH 631

### Required Stirrup Reinforcement

#### • spacing limits

Table 3-8 ACI Provisions for Shear Design\*

	(1월55, 2844) (고)	$V_u \leq \frac{\phi V_c}{2}$	$\varphi V_c \geq V_u > \frac{\varphi V_c}{2}$	$V_{u} > \phi V_{c}$
Required area of s	tirrups, A <sub>V</sub> **	none	50b <sub>w</sub> s fy	(V <sub>u</sub> – φV <sub>c</sub> )s φf <sub>y</sub> d
	Required		Avfy 50bw	$\frac{\phi A_v f_y d}{V_u - \phi V_c}$
Stirrup spacing, s Maximum <sup>††</sup> (ACI 11.5.4)		—	<u> </u>	4 in.
	1000 - 1000 - 1000 	d or 24 in.	$\frac{d}{2}$ or 24 in. for $(V_u - \phi V_c) \le \phi 4 \sqrt{t'_c} b_w d$	
				$\frac{d}{4}$ or 12 in. for $(V_u - \phi V_c) > \phi 4 \sqrt{f'_c} b_w d$

\*Members subjected to shear and flexure only;  $\phi V_c = \phi 2 \sqrt{f'_c} b_w d$ ,  $\phi = 0.75$  (ACI 11.3.1.1)

 $^{\star\star}A_v = 2 \times A_b$  for U stirrups;  $f_y \leq 60$  ksi (ACI 11.5.2)

†A practical limit for minimum spacing is d/4

++Maximum spacing based on minimum shear reinforcement (= A<sub>v</sub>f<sub>y</sub>/50b<sub>w</sub>) must also be considered (ACI 11.5.5.3).

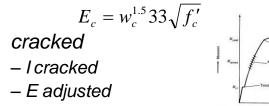
Reinforced Concrete Construction 29	Applied Architectural
Lecture 10	ARCH 631

chitectural Structures ARCH 631

#### F2012abn

# Concrete Deflections

- elastic range
  - I transformed
  - $-E_c$  (with  $f'_c$  in <u>psi</u>)
    - normal weight concrete (~ 145 lb/ft<sup>3</sup>)  $E_c = 57,000 \sqrt{f_c'}$
    - concrete between 90 and 155 lb/ft<sup>3</sup>





٠

on 30 Architectural Structures III ARCH 631

#### **Deflection Limits**

- relate to whether or not beam supports or is attached to a damageable nonstructural element
- need to check <u>service</u> live load and long term deflection against these

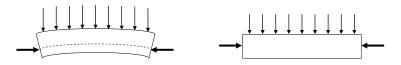
L/180	roof systems (typical) – live
L/240	floor systems (typical) – live + long term
L/360	supporting plaster – live
L/480	supporting masonry – live + long term

#### Reinforced Concrete Construction 31 Lecture 9

Architectural Structures III ARCH 631

#### Prestressed Concrete

 impose a longitudinal force on a member in order to <u>withstand more</u> <u>loading</u> until the member reaches a tensile limit



----- Curvature,

F2007abn

Reinforced Concrete Construction 32 Lecture 9

#### Prestressed Concrete

- pretensioned
  - reinforcement bonded
- post-tensioned
  - bonded or unbonded
  - end bearing

=====**-**

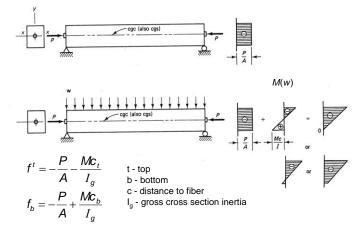
#### precast

 concrete premade in a position other than its final position in the structure

Reinforced Concrete Construction 33	Architectural Structures III	F2007abn
Lecture 9	ARCH 631	

#### Prestressed Concrete

• axial prestress (e=0)



Reinforced Concrete Construction 35 Lecture 9 Architectural Structures III ARCH 631 F2007abn

#### Prestressed Concrete

• high strength tendons

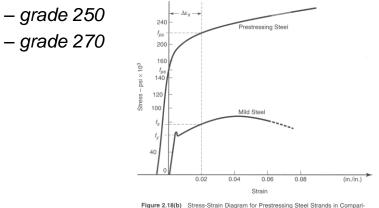
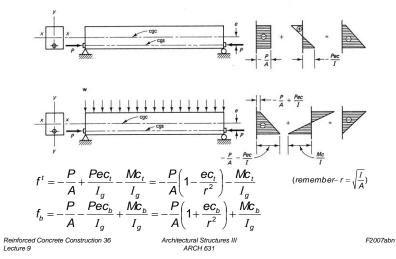


Figure 2.18(b) Stress-Strain Diagram for Prestressing Steel Strands in Comparison with Mild Steel Bar Reinforcement.

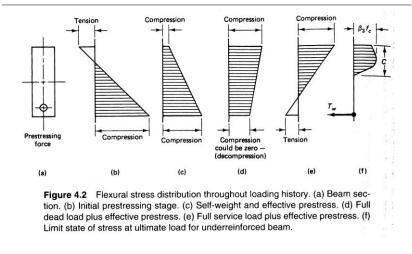
Reinforced Concrete Construction 34 Lecture 9 Architectural Structures III ARCH 631 F2007abn

#### Prestressed Concrete

• axial prestress (e≠0)

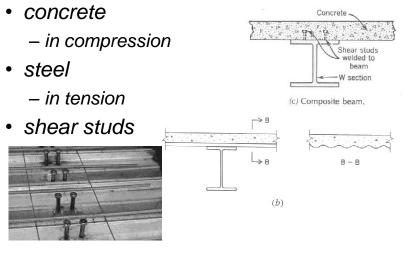


#### Prestressed Concrete

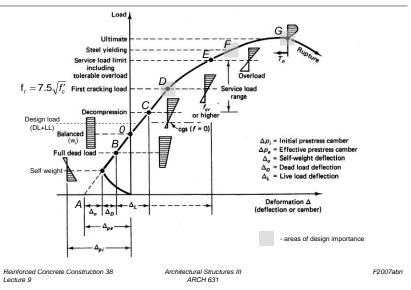


Reinforced Concrete Construction 37	Architectural Structures III	F2007abn
Lecture 9	ARCH 631	

#### Composite Beams

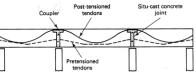


#### Prestressed Concrete



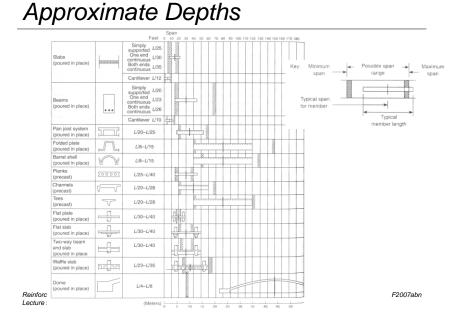
#### Continuous Beams

- reduced size
- reduced moments



- moments can reverse with loading patterns
- need top & bottom reinforcement
- sensitive to settlement

Reinforced Concrete Construction 40 Lecture 9 Architectural Structures III ARCH 631 F2007abn



#### Concrete Columns

- columns require
  - ties or spiral reinforcement to "confine" concrete (#3 bars minimum)

Tied column	Spirally reinforced column

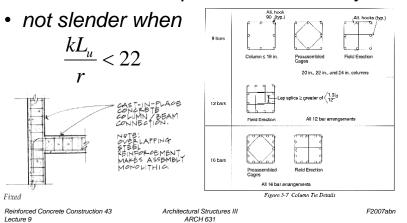
- minimum amount of longitudinal steel (#5 bars minimum: 4 with ties, 5 with spiral)

Architectural Structures III

ARCH 631

Concrete Columns

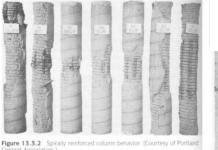
• effective length in monolithic casts must be found with respect to stiffness of joint

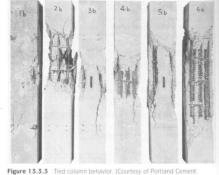


#### Concrete Columns

Reinforced Concrete Construction 42

Lecture 9





Reinforced Concrete Construction 44 Lecture 9

Architectural Structures III ARCH 631

F2007abn

#### Concrete Columns

- $P_o$  no bending  $P_o = 0.85 f'_c (A_g - A_{st}) + f_y A_{st}$
- $\phi_c = 0.65$  for ties with  $P_n = 0.8P_o$
- $\phi_c = 0.70$  for spirals with  $P_n = 0.85P_o$
- $P_u \leq \phi_c P_n$
- nominal axial capacity:
  - presumes steel yields
  - concrete at ultimate stress

Reinforced Concrete Construction 45 Lecture 9  $C_{\rm 1} = 0.85\, f_c^{~\prime} (A_g - A_{\rm sr}, \label{eq:C1}$  Architectural Structures III ARCH 631

...............

 $C_2 = f_y A_1 \qquad C_3 = f_y A_2$ 

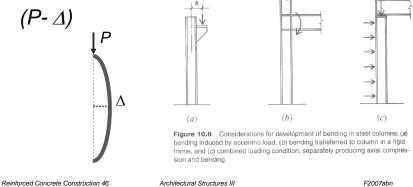
Po is located colinearly with the resultant of

 $C_1$ ,  $C_2$ , and  $C_3$  at the plastic centroid

F2007abr

#### Columns with Bending

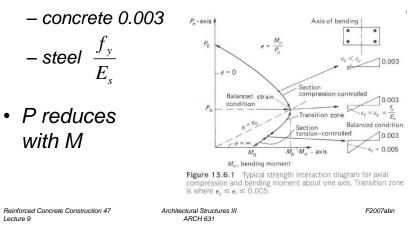
- · eccentric loads can cause moments
- moments can change shape and induce more deflection



ARCH 631

#### Columns with Bending

 for ultimate strength behavior, ultimate strains can't be exceeded



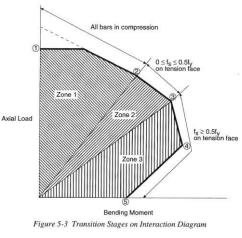
#### Columns with Bending

 need to consider combined stresses

Lecture 9

$$\frac{P_n}{P_o} + \frac{M_n}{M_o} \le 1$$

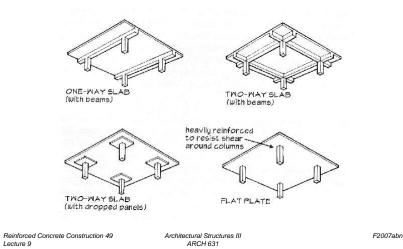
 plot <u>interaction</u> diagram



Reinforced Concrete Construction 48 Lecture 9 Architectural Structures III ARCH 631

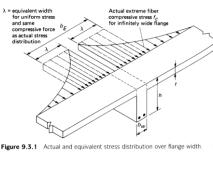
#### Concrete Floor Systems

• types & spanning direction



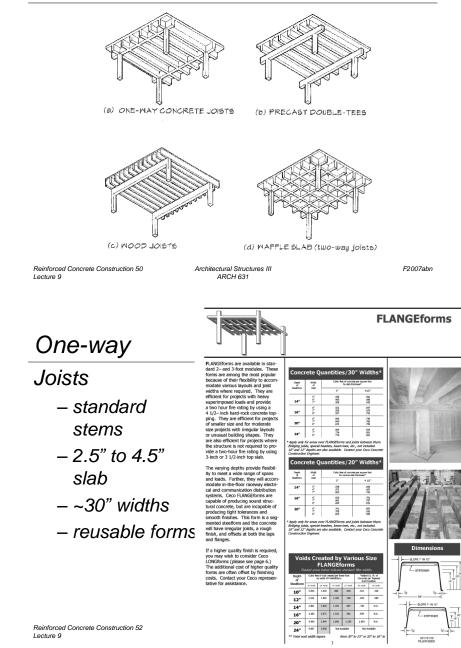
#### Concrete Floor Systems

- flexure design as T-beams (+/- M)
- increase of 10% V<sub>c</sub> permitted
- one-way and two-way moments
- slabs need steel
- · effective width is
  - L/4
  - $-b_w + 16t$
  - center-to-center of beams



Reinforced Concrete Construction 51 Lecture 9 Architectural Structures III ARCH 631 F2007abn

#### Concrete Floor Systems



#### One-way

#### Joists

- wide pans
- 5', 6' up
- light loads & long spans
- one-leg stirrups



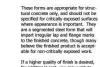
Reinforced Concrete Construction 53 Lecture 9

WIDE FLANCEforms are available in standard S3 and 6-inch yolss they pro-duce 5 and 6-ioch yolss they pro-duce 5 and 6-loch modules respec-tive of the statement of the statement between the statement of the statement between the statement of the statement can be used in combination with stan-dard width pans to address span and dat requirements. This system is very efficient for projects where the struc-testion.

WIDE FLANGEforms

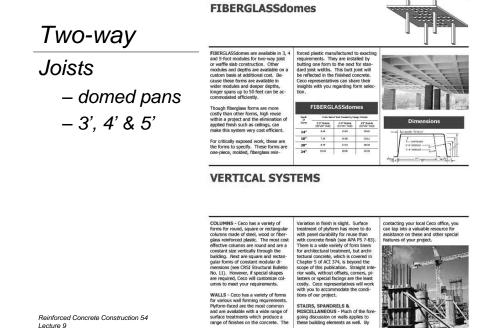
Using hard rock concrete, a 4 1/2-inch sibb and minimum slab reinforcement ull result in suiticinat capacity for a variety of superimposed bads while reducing structure deal bads. Shal-kower depth forms are appropriate for pages in the 25- to 35-foot range. Doddernie bads, for appart in the 35-boddernie bads, for appart of the 35-boddernie bads, for the 35-boddernie b with post-ter

By varying joist widths, different load-ing conditions can be accommodated using standard forming equipment without the need to add drop beams. Distribution ribs, which add unnecesary cost, are not required with wide module construction.



If a higher quality of finish is desired, for additional cost, you may wish to consider Ceco LONGforms (please see page 6). Your Ceco representative can assist in form type selection.





Reinforced Concrete Construction 54 Lecture 9

STAIRS, SPANDRELS & MISCELLANEOUS - Much of the fore going discussion on walls applies to these building elements as well. By

### Construction Supervision

- proper placement of all reinforcement
  - welding
  - splices
- mix design
  - slump
  - in-situ strength
    - cast cylinders
    - cylinder cores if needed

Reinforced Concrete Construction 55 Lecture 9

Architectural Structures III ARCH 631





F2007abn

