Applied Architectural Structures: Structural Analysis and Systems arch 631 Dr. Anne Nichols Fall 2012

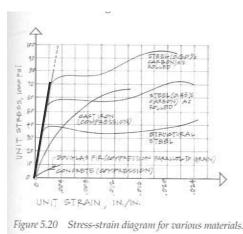
lecture

# design methods & beams



## Allowable Stress Design

- historical method
- a.k.a. working stress, stress design
- stresses stay in ELASTIC range



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## Allowable Stress Design

- codes
  - wood



- National Design Specification
- Manual of Timber Construction (glulam)
- masonry
  - Masonry Specification Joint Code
- steel
  - Steel Joist Institute
  - American Institute of Steel Construction

## Limit State Design

• stresses go to limit (strain outside elastic range)

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- · loads may be factored
- resistance or capacity reduced by a factor
- · based on material behavior
- "state of the art"





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## Limit State Design

#### • codes

- wood
  - National Design Specification



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- masonry
  - Masonry Specification Joint Code
- concrete
  - American Concrete Institute
  - Precast & Prestressed Concrete
- steel
  - American Institute of Steel Construction

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## Reinforced Concrete Design

- ultimate strength design
- $\phi$  factor applied to capacity
  - different for flexure, shear, bearing....
- factors applied to loads (ASCE 7)
  may be different for combinations

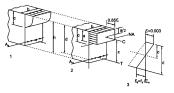
U = 1.2D + 1.6LU = 1.2D + 1.0W + 1.0L

- <u>can</u> use alternate values & factors (older codes)

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## Reinforced Concrete Design

- · want steel to yield first
  - ductile failure
  - underreinforced
- find flexure capacity or resistance from
  - ultimate stresses in steel
  - "uniform stress block" in concrete

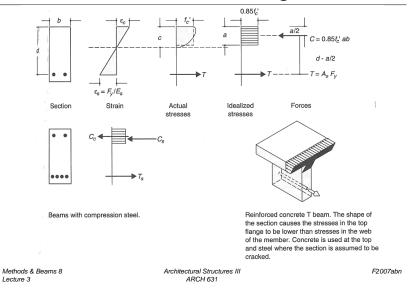


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## Reinforced Concrete Design

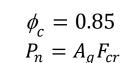


## Steel Design

- load and resistance factor design
- like concrete, but capacity related to material

 $R_{u} \leq \phi R_{\tilde{n}}$ nominal strength load factors load types resistance factor

- R<sub>11</sub> combinations, ex:
  - 1.4D
  - -1.2D + 1.6L
- compression
- capacity





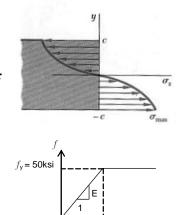
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## Elastic vs. Plastic Behavior

- Hooke's law valid  $f = E\varepsilon$
- yield point is end of elastic range for a ductile material



 $\varepsilon_{v} = 0.001724$ 

 continued strain with no more load



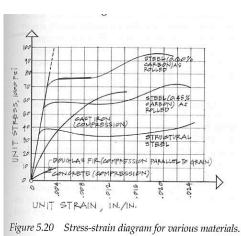
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Plastic Design

- bending & beams
- all of material sees ultimate stress
- refers primarily to steel behavior
- statically indeterminate systems



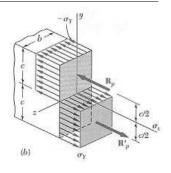
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## Internal Moments - ALL at yield

- all parts reach yield
- plastic hinge forms
- ultimate moment
- $A_{tension} = A_{compression}$



 $M_{ult} \text{ or } M_{p} = bc^{2}f_{y} = \frac{3}{2}M_{y}$ 

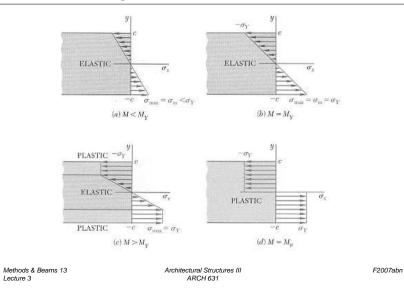
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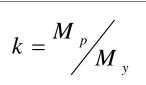
#### Plastic Hinge Development



## Plastic Section Modulus

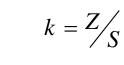
• shape factor, k

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= 3/2 for a rectangle

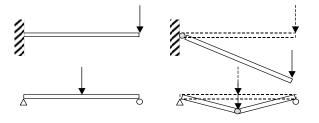
 $\approx$  1.1 for an I



 $Z = \frac{M_p}{p}$ 

• plastic modulus, Z

## Plastic Hinge Examples • stability can be effected



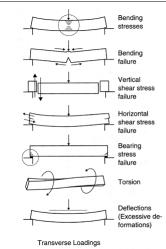
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#### Beams

- transverse loading
- sees:
  - bending
  - shear
  - deflection
  - torsion
  - bearing
- cross section shape



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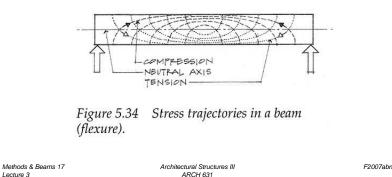
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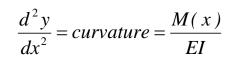
#### Beams

- maximum stress distribution
- principal stresses
  - resultant of shear and bending stress



#### Beams

deflections



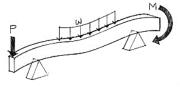


Figure 5.4 Bending (flexural) loads on a beam.

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#### Beams

- design:
  - bending stress not exceeding allowable or limit stress

$$F_{all} \ge f_b = \frac{Mc}{I} \qquad S_{req'd} \ge \frac{M}{F_{al}}$$

#### Beams

 bending stresses dominate



- shear stresses exist horizontally with shear
- no shear stresses with pure bending



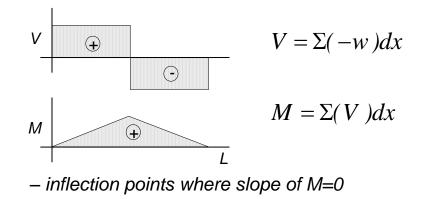


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#### Beams

V & M drawings help determine M<sub>max</sub>



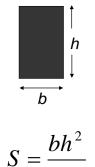
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Beam Design

- 1. Know  $F_{all}$  for the material or  $f_{,,}$  for LRFD
- 2. Draw V & M, finding M<sub>max</sub>
- 3. Calculate S<sub>reg'd</sub>
- Determine section size 4

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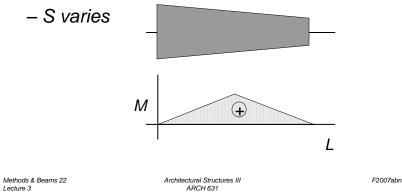


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#### Beams

- prismatic (constant cross section)
  - maximum stress ⇔ maximum moment
- non-prismatic



## Beam Design

- 4<sup>\*</sup>. Include self weight for  $M_{max}$ 
  - and repeat 3 & 4 if necessary

#### 5. Consider lateral stability

Unbraced roof trusses were blown down in 1999 at this project in Moscow, Idaho. Photo: Ken Carper

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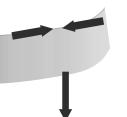
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## Beam Design

- 5. Consider lateral stability (cont)
  - lateral buckling caused by compressive forces at top couples with insufficient rigidity
  - can occur at low stress levels
  - stiffen or brace



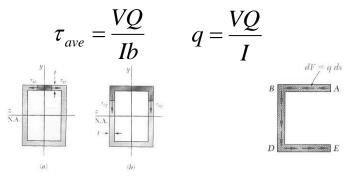
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## Beam Design

- 6. Evaluate shear stresses (cont)
  - thin walled open or closed



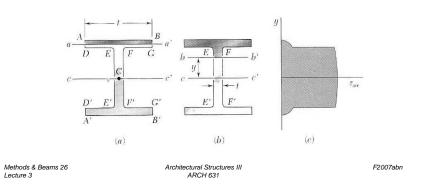
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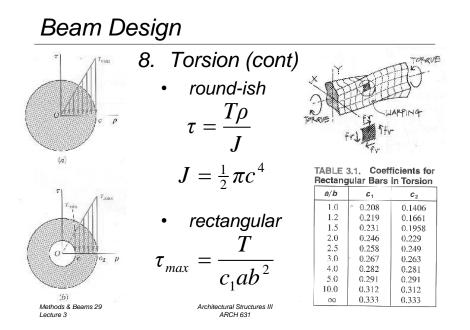
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## Beam Design

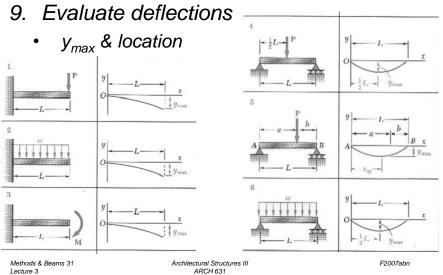
- 6. Evaluate shear stresses horizontal
  - W and rectangles  $\tau_{\max} = \frac{3V}{2A} \approx \frac{V}{A_{web}}$



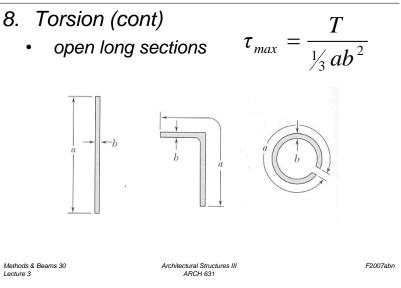
## Beam Design



## Beam Design



#### Beam Design



## **Deflection Limits**

• based on service condition, severity

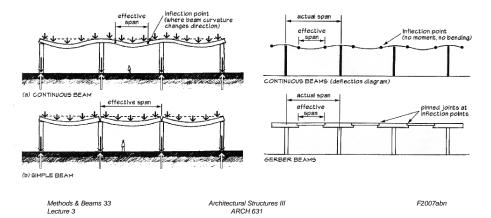
		-
Use	LL only	DL+LL
Roof beams:		
Industrial	L/180	L/120
Commercial		
plaster ceiling	L/240	L/180
no plaster	L/360	L/240
Floor beams:		
Ordinary Usage	L/360	L/240
Roof or floor (damageable elements)		L/480

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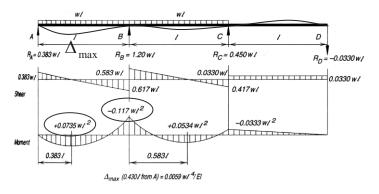
### Continuous Beams

- statically indeterminate
- · reduced moments than simple beam



### Continuous Beams

• unload end span

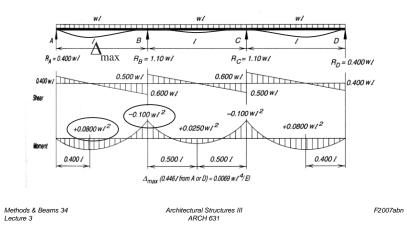


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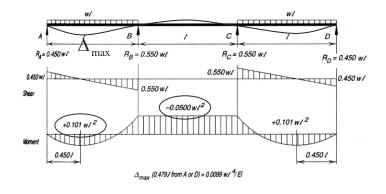
## Continuous Beams

- · loading pattern affects
  - moments & deflection



## Continuous Beams

• unload middle span



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### Beam Materials

- timber
- glu-lam wood
- concrete
- steel
- reinforced masonry

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S Fram

(2 N)

### Tools – Multiframe

- frame window
  - define beam members
  - select points, assign supports
  - select members. assign section
- load window
  - select point or member, add point or distributed loads

49 # 4 4 4 4 Member 2

用為田四四一个小

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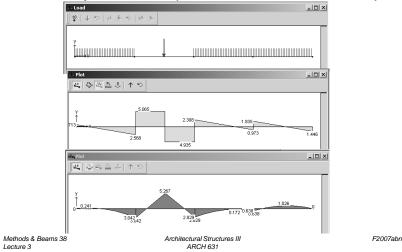
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• in computer lab (Multiframe3D w/ text)



Result

## Tools – Multiframe

- to run analysis choose
  - Analyze menu
    - Linear
- plot
  - choose options
  - double click (all)
- results
  - choose options

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