Applied Architectural Structures:

STRUCTURAL ANALYSIS AND SYSTEMS

ARCH 631 DR. Anne Nichols Fall 2012





# structural analysis (statics & mechanics)

Analysis 1 Lecture 2 Applied Architectural Structures ARCH 631

## Structure Requirements

- strength & equilibrium
  - safety
  - stresses
     not greater
     than
     strength
  - adequate foundation



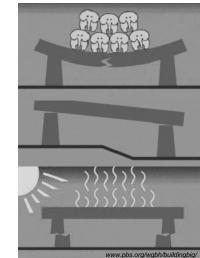
Figure 1.16 Equilibrium and Stability?—sculpture by Richard Byer. Photo by author.

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## Structural Requirements

- · serviceability
  - strength
  - deflections
- efficiency
  - economy of materials
- construction
- cost
- other



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## Structure Requirements

- stability & stiffness
  - stability of components
  - minimum deflection and vibration
  - adequate foundation

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Figure 1.15 Stability and the strength of a structure—the collapse of a portion of the UW Husky stadium during construction (1987) due to a lack of adequate bracing to ensure stability. Photo by author.

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### Structure Requirements

- economy and construction
  - minimum material
  - standard sized members
  - simple connections and details
  - maintenance
  - fabrication/ erection



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#### Relation to Architecture

"The geometry and arrangement of the load-bearing members, the use of materials, and the crafting of joints all represent opportunities for buildings to express themselves. The best buildings are not designed by architects who after resolving the formal and spatial issues, simply ask the structural engineer to make sure it doesn't fall down." - Onouy & Kane

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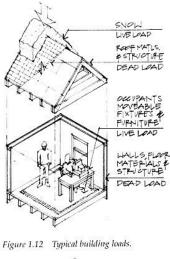
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## Structural Loads - STATIC

- dead load
  - static, fixed, includes material weights, fixed equipment
- live load
  - transient and moving loads (including occupants)
- snow load



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### Structural Loads – STATIC & DYNAMIC

- wind loads
  - dynamic, wind pressures treated as lateral static loads on walls, pressure or suction
  - pressure determined from wind velocity,  $q_h$
  - dynamic effects include motion from buffeting or "vortex shedding"

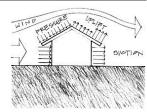


Figure 1.13 Wind loads on a structure

 $F_{W} = C_{d}q_{h}A$ 

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## Structural Loads - DYNAMIC

- earthquake loads
  - seismic, movement of ground (3D)

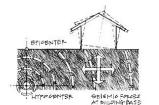


Figure 1.14 Earthquake loads on a structure.

- building mass responds
- static models often used. V is static shear
- impact loads
  - rapid, energy loads



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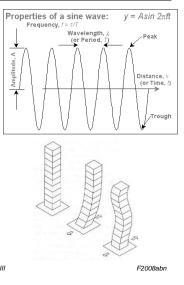
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## Dynamic Response

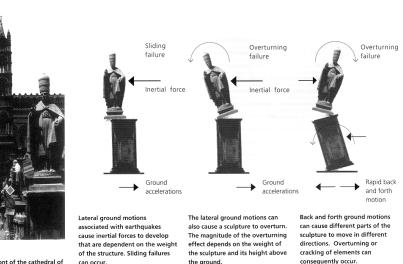
- period of vibration or frequency
  - wave
  - sway/time period
- damping
  - reduction in sway
- resonance
  - amplification of sway



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## Dynamic Response



Statue in front of the cathedral of Palermo, Sicily

the around.

consequently occur.

## Statics & Mechanics Review

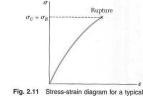
- how loads affect our structures
  - statics: things don't move
    - forces
    - supports & connections
    - equilibrium
  - mechanics: things can change shape

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- stress & strain
- deflections
- buckling

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brittle material Architectural Structures III

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#### Structural Math

- quantify environmental loads
   how big is it?
- · evaluate geometry and angles
  - where is it?
  - what is the scale?
  - what is the size in a particular direction?
- quantify what happens in the structure
  - how big are the internal forces?
  - how big should the beam be?

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## Units

#### • measures

<sup>–</sup> US customary & SI

Units	US	SI
Length	in, ft, mi	mm, cm, m
Volume	gallon	liter
Mass	lb mass	g, kg
Force	lb force	N, kN
Temperature	F	С

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## Physical Math

- physics takes observable phenomena and relates the measurement with rules: <u>mathematical relationships</u>
- need
  - reference frame



- measure of length, mass, time, direction, velocity, acceleration, work, heat, electricity, light
- calculations & geometry

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#### Vectors

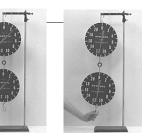
- scalars any quantity
- · vectors quantities with direction
  - like displacements
  - summation results in the "straight line path" from start to end
  - <u>normal</u> vector is perpendicular to something

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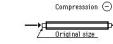
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### Forces & Reactions

- Newton's 3<sup>rd</sup> law:
  - for every force of action there is an equal and opposite reaction along the same line



- external forces act on bodies
  - can cause moments
- Tension (+) internal forces are - in bodies Original size



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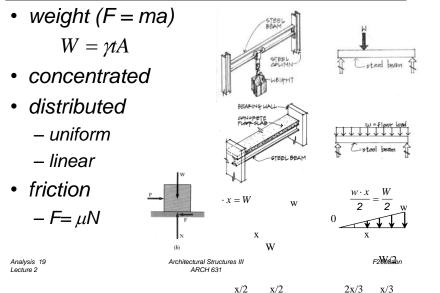
x/2 x/6 x/3

- between bodies (connections)

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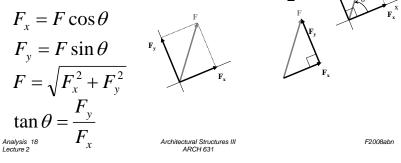
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Load Types



### Force Components

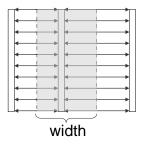
- convenient to resolve into 2 vectors
- at right angles
- in a "nice" coordinate system
- $\theta$  is between  $F_x$  and F from  $F_x$



## Load Tracing

- tributary load
  - think of water flow
  - "concentrates" load of area into center

$$w = \left(\frac{load}{area}\right) \times \left(tributary \ width\right)$$



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#### Moments

- · defined by magnitude and direction
- units: N·m, k·ft
- direction:
  - + ccw (right hand rule)
  - CW
- value found from F and ⊥ distance
  - $M = F \cdot d$
- d also called "lever" or "moment" arm

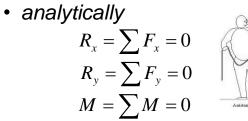
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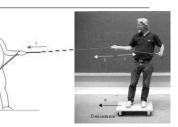
### Free Body Diagram

- FBD (sketch)
- tool to see all forces on a body or a point including
  - external forces
  - weights
  - force reactions
  - external moments
  - moment reactions
  - internal forces

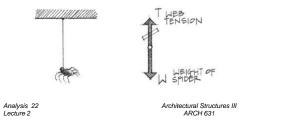
AB B W=100#

#### Equilibrium



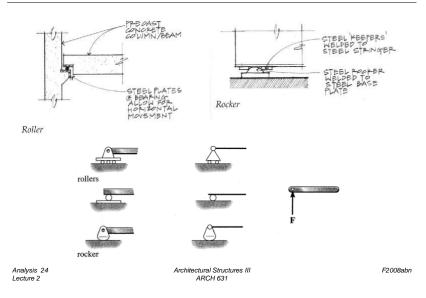


• free body diagrams



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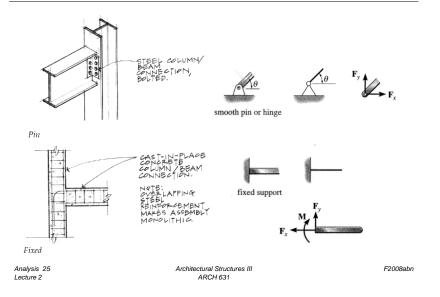
## Supports and Connections



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#### Supports and Connections

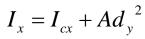


#### Moments of Inertia

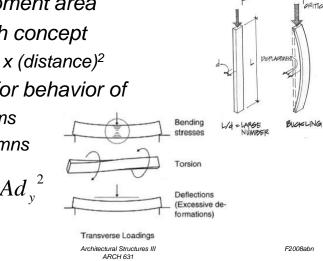
- 2<sup>nd</sup> moment area
  - math concept
  - area x (distance)<sup>2</sup>
- need for behavior of



- columns

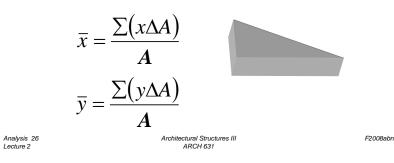


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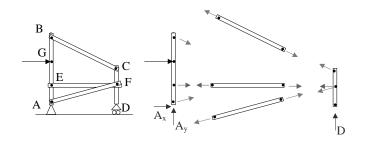
#### Centroid

- "average" x & y of an area
- for a volume of constant thickness
  - $-\Delta W = \gamma t \Delta A$ where  $\gamma$  is weight/volume
  - center of gravity = centroid of area



Internal and Pin Forces

- 3 equations per three-force body
- two-force body forces in line
- 2 reactions per pin + support forces



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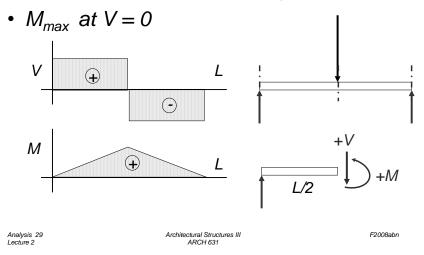
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#### Internal Beam V & M (+P)

• maximums needed for design



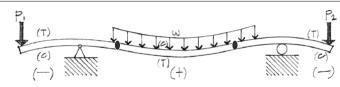
#### Stress

- stress is a term for the <u>intensity</u> of a force, like a pressure
- internal <u>or</u> applied
- force per unit area

stress = -Α



## Deflected Shape



- positive bending moment – tension in bottom, compression in top
- negative bending moment

  tension in top, compression in bottom
- zero bending moment – <u>inflection point</u>

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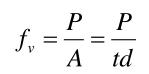
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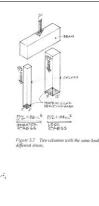
## Stress Types

 <u>normal</u> stress is normal to the cross section

$$f_{t \, or \, c} = \frac{P}{A}$$

 <u>shear</u> stress parallel to a surface





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Figure 5.10 Shear stress between two ghad blocks

### Stress Types

- <u>bearing</u> stress on a surface by contact in compression  $f_p = \frac{P}{A} = \frac{P}{td}$ • torsional stress by
- torsional stress by shear from twisting



T-TPF-RVE - X (( fvs small

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#### **Bending Stresses**

 tension and compressive stress caused by bending

$$f_b = \frac{Mc}{I} = \frac{M}{S}$$

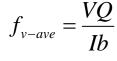


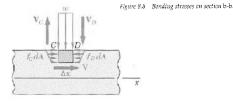
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Figure 5.3 Centric loads

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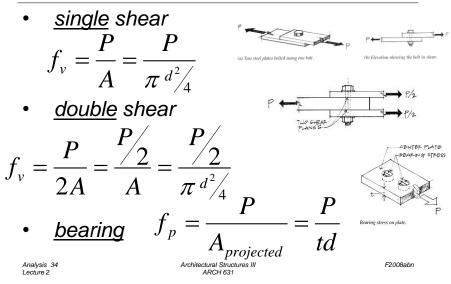
• <u>shear</u> stress from bending





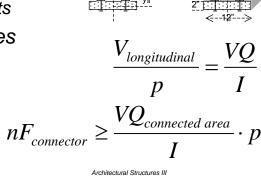
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Bolt Stresses



#### **Connectors Resisting Shear**

- · plates with
  - nails – rivets
  - bolts
- splices

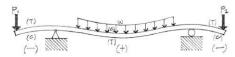


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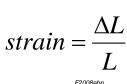
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#### Strain

- materials deform
- axially loaded materials change length
- · bending materials deflect



- STRAIN:
  - change in length over length



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## Stress to Strain

• important to us in *f*- $\varepsilon$  diagrams: - straight section - LINEAR-ELASTIC  $f = E \cdot \varepsilon$ - recovers shape (no permanent deformation)  $\delta = \frac{PL}{AE}$   $\delta = \frac{PL}{AE}$  $\delta$ 

## Problem Solving

1. STATICS:

equilibrium of external forces, internal forces, <u>stresses</u>

2. GEOMETRY:



#### 3. MATERIAL PROPERTIES:

<u>stress-strain relationship</u> for each material obtained from testing

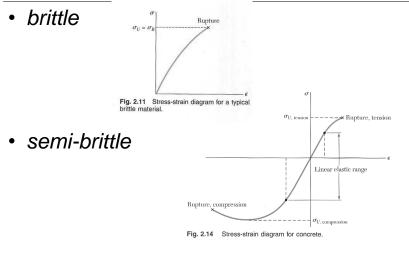
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## Behavior Types



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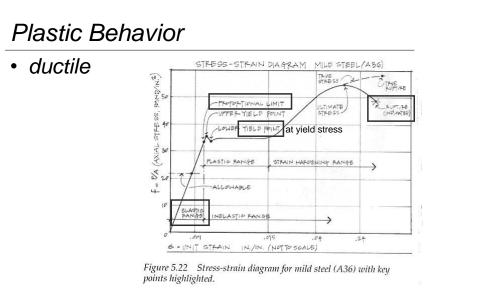
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#### Thermal Deformation

- $\alpha$  the rate of strain per degree
- UNITS : /°F , /°C
- length change:  $\delta_T = \alpha (\Delta T) L$
- thermal strain:
- $\varepsilon_T = \alpha(\Delta T)$
- <u>no stress</u> when movement allowed

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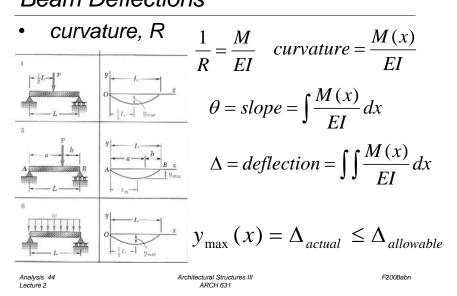
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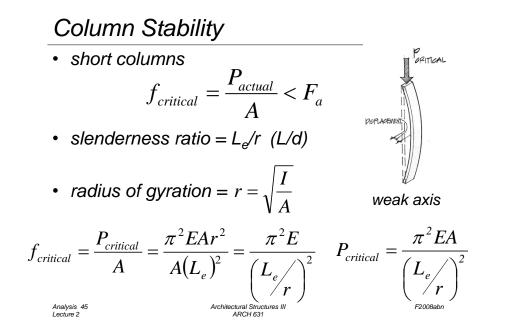
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#### Maximum Stresses

if we need to know where max f and  $f_{v} \leftarrow \int_{A}^{a} \int$ 

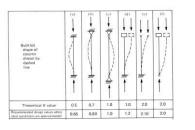
# Beam Deflections

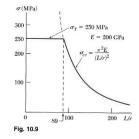




#### Column Stresses

- when a column gets stubby, F<sub>y</sub> will limit the load
- real world has loads with eccentricity
- end conditions  $L_e = K \cdot L$





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