Case Study in Steel

adapted from Structural Design Guide, Hoffman, Gouwens, Gustafson & Rice., 2nd ed.

Building description

The building is a one-story steel structure, typical of an office building. The figure shows that it has three 30 ft. bays in the short direction and a large number of bays in the long direction. Some options for the structural system include fully restrained with rigid connections and fixed column bases, simple framing with "pinned" connections and column bases requiring bracing against sideway, and simple framing with continuous beams and shear connections, pinned column bases and bracing against sidesway. This last situation is the one we'll evaluate as shown in Figure 2.5(c).



Live Loads:

Snow on Roof: $30 \text{ lb/ft}^2 (1.44 \text{ kPa})$

Wind: 20 lb/ft² (0.96 kPa)

Dead Loads:

Roofing: 8 lb/ft² (0.38 kPa) Estimated decking: 3 lb/ft² (0.14 l Ceiling: 7 lb/ft² (0.34 kPa)

Total: 18 lb/ft² (0.86 kPa)

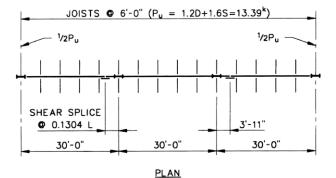
Materials

A36 steel for the connection angles at $(F_y = 36 \text{ ksi}, F_u = 58 \text{ ksi})$ and A992 of for the beams and columns $(F_y = 50 \text{ K series open web joists and roof de})$

Decking:

Decking selection is typically allowable stress design. Tables will give allowable total uniform load (taking self weight into account) based on stresses and deflection criteria for typical spans and how many spans are supported. The table (and description) for a Vulcraft 1.0 E deck is provided.

(3) **B**5 **B4 B6** (D) **B**5 JOISTS JOISTS JOISTS **B5 B6 B4** R6 ➅ 30'-0" 30'-0" 30'-0' JOISTS . 6'-0' SECTION X-X TYPICAL FRAME



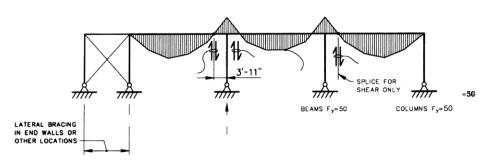


Figure 2.5(c) Type SF — cantilever-suspended span system, braced against sidesway

Areas in gray are governed by live load roof deflection.

The total load with snow and roofing = 30 psf + 8 psf = 38 psf.

VERTICAL LOADS FOR TYPE 1.0E

		Max.	Allowable Total (Dead + Live) Uniform Load (PSF) Span (ftin.) C. to C. of Support												
No. of	Deck	SDI Const.													
Spans	Type	Span	2'-6	3'-0	3'-6	4'-0	4'-6	5'-0	5'-6	6'-0	6'-6	7'-0	7'-6		
	E26	2'-10	178	107	71	51	39	31	26	22	20	18	16		
	E24	3'-5	249	148	97	68	51	40	32	27	24	21	19		
1	E22	3'-10	316	187	122	85	63	48	39	32	27	24	21		
	E20	4'-2	379	224	145	100	73	56	45	37	31	27	24		
	E26	3'-4	273	189	139	107	81	62	49	40	34	29	25		
	E24	4'-0	396	275	202	153	111	83	65	52	43	37	32		
2	E22	4'-6	515	357	263	190	137	102	79	63	52	44	37		
	E20	5'-0	634	440	323	227	162	121	94	74	61	51	43		
	E26	3'-4	310	198	128	89	66	51	40	33	28	25	22		
	E24	4'-0	469	276	177	122	89	67	53	43	36	31	27		
3	E22	4'-6	588	344	221	151	109	82	64	52	43	36	31		
	E20	5'-0	707	413	264	180	129	97	75	60	50	42	36		

Notes: 1. Load tables are calculated using sectional properties based on the steel design thickness shown in the Steel Deck Institute (SDI) Design Manual.

Loads shown in the shaded areas are governed by the live load deflection not in excess of 1/240 of the span.A dead load of 10 PSF has been included.

1.0 E

Maximum Sheet Length 42'-0

Extra Charge for Lengths Under 6'-0

Open Web Joists:

Open web joist selection is either based on allowable stress design or LRFD resistance for flexure (*not for deflection*). The total <u>factored</u> distributed load for joists at 6 ft on center will be:



 $w_{\text{total}} = (1.2 \times 181 \text{b/ft}^2 + 1.6 \times 30 \text{ lb/ft}^2)(6 \text{ ft}) + 1.2(8 \text{ lb/ft estimated})$ $= 427.2 \text{ lb/ft} \quad (\text{with } 1.2D + 1.6(L, or L_r, or S, or R) \text{ by catalogue})$ $w_{\text{live}} = 30 \text{ lb/ft}^2(6 \text{ ft}) = 180 \text{ lb/ft}$

			Ва	sed or										TS, K-S			(plf)				
Joist Designation	18K3	18K4	18K5	18K6	18K7	18K9	18K10	20K3	20K4	20K5	20K6	20K7	20K9	20K10	22K4	22K5	22K6	22K7	22K9	22K10	22K1
Depth (In.)	18	18	18	18	18	18	18	20	20	20	20	20	20	20	22	22	22	22	22	22	22
Approx. Wt. (lbs./ft.)	6.6	7.2	7.7	8.5	9	10.2	11.7	6.7	7.6	8.2	8.9	9.3	10.8	12.2	8	8.8	9.2	9.7	11.3	12.6	13.
Span (ft.) ↓ 18	825 550																				
19	771 494	825 523	825 523	825 523	825 523	825 523	825 523														
20	694 423	825 490	825 490	825 490	825 490	825 490	825 490	775 517	825 550	825 550	825 550	825 550	825 550	825 550							
21	630 364	759 426	825 460	825 460	825 460	825 460	825 460	702 453	825 520	825 520	825 520	825 520	825 520	825 520							
22	573	690	777	825	825	825	825	639	771	825	825	825	825	825	825	825	825	825	825	825	82
	316	370	414	438	438	438	438	393	461	490	490	490	490	490	548	548	548	548	548	548	54
23	523	630	709	774	825	825	825	583	703	793	825	825	825	825	777	825	825	825	825	825	82
	276	323	362	393	418	418	418	344	402	451	468	468	468	468	491	518	518	518	518	518	51
24	480	577	651	709	789	825	825	535	645	727	792	825	825	825	712	804	825	825	825	825	82
	242	284	318	345	382	396	396	302	353	396	430	448	448	448	431	483	495	495	495	495	49
25	441	532	600	652	727	825	825	493	594	669	729	811	825	825	657	739	805	825	825	825	82:
	214	250	281	305	337	377	377	266	312	350	380	421	426	426	381	427	464	474	474	474	47:
26	408	492	553	603	672	807	825	456	549	618	673	750	825	825	606	682	744	825	825	825	82:
	190	222	249	271	299	354	361	236	277	310	337	373	405	405	338	379	411	454	454	454	45:
27	378	454	513	558	622	747	825	421	508	573	624	694	825	825	561	633	688	768	825	825	82
	169	198	222	241	267	315	347	211	247	277	301	333	389	389	301	337	367	406	432	432	43
28	351	423	477	519	577	694	822	391	472	532	579	645	775	825	522	588	640	712	825	825	82
	151	177	199	216	239	282	331	189	221	248	269	298	353	375	270	302	328	364	413	413	41
29	327	394	444	483	538	646	766	364	439	495	540	601	723	825	486	547	597	664	798	825	82
	136	159	179	194	215	254	298	170	199	223	242	268	317	359	242	272	295	327	387	399	39
30	304	367	414	451	502	603	715	340	411	462	504	561	675	799	453	511	556	619	745	825	82
	123	144	161	175	194	229	269	153	179	201	218	242	286	336	219	245	266	295	349	385	38
31	285	343 130	387 146	421 158	469 175	564 207	669 243	318 138	384 162	433 182	471 198	525 219	631 259	748 304	424 198	478 222	520 241	580 267	697 316	825 369	82

Deflection will limit the selection, and the most lightweight choice is the 22K4 which weighs approximately 8 lb/ft. Special provisions for bridging are required for the shaded area lengths and sections.

Continuous Beams:

LRFD design is required for the remaining structural steel for the combinations of load involving Dead, Snow and Wind. The bracing must be designed to resist the lateral wind load.

The load values are:

$$\begin{split} \text{for D:} \quad & w_D = 18 \text{ lb/ft}^2 \cdot 30 \text{ ft} + (8 \text{ lb/ft} \cdot 30 \text{ ft}) / 6 \text{ ft} = 580 \text{ lb/ft} \\ \text{for S:} \quad & w_S = 30 \text{ lb/ft}^2 \cdot 30 \text{ ft} = 900 \text{ lb/ft} \\ \text{for W:} \quad & w_W = 20 \text{ lb/ft}^2 \cdot 30 \text{ ft} = 600 \text{ lb/ft} \text{ (up or down)} \\ & \text{and laterally } V = 600 \text{ lb/ft} (15 \text{ft/2}) = 4500 \text{ lb} \end{split}$$

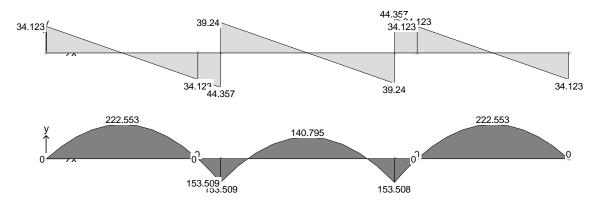
These DO NOT consider self weight of the beam.

The applicable combinations for the tributary width of 30 ft. are:

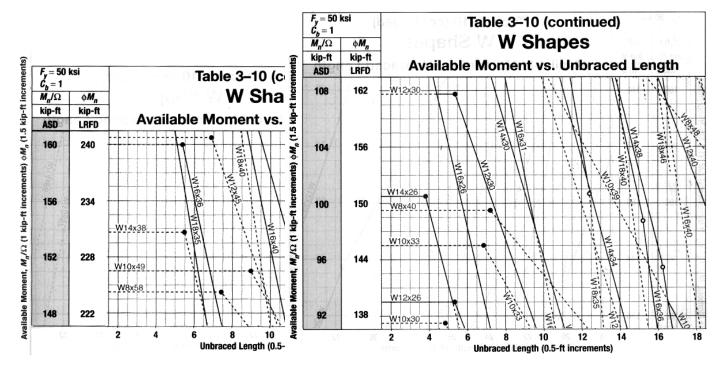
$$\begin{aligned} 1.4D & \text{$\text{w}_{\text{u}} = 1.4(580 \text{ lb/ft}) = 812 \text{ lb/ft}} \\ 1.2D + 1.6L + 0.5(L_r \, or \, S \, or \, R) & \text{$\text{w}_{\text{u}} = 1.2(580 \text{ lb/ft}) + 0.5(900 \text{ lb/ft}) = 1146 \text{ lb/ft}} \\ 1.2D + 1.6(L_r \, or \, S \, or \, R) + (L \, or \, 0.8W) & \text{$\text{w}_{\text{u}} = 1.2(580 \text{ lb/ft}) + 1.6(900 \text{ lb/ft}) + 0.8(600 \text{ lb/ft}) = 2616 \text{ lb/ft}} \\ 1.2D + 1.6W + L + 0.5(L_r \, or \, S \, or \, R) & \text{$\text{w}_{\text{u}} = 1.2(580 \text{ lb/ft}) + 1.6(600 \text{ lb/ft}) + 0.5(900 \text{ lb/ft}) = 2106 \text{ lb/ft}} \\ 1.2D + 1.0E + L + 0.25S & \text{$\text{w}_{\text{u}} = 1.2(580 \text{ lb/ft}) + 0.25(900 \text{ lb/ft}) = 921 \text{ lb/ft}} \\ 0.9D + 1.6W + 1.6H & \text{$\text{w}_{\text{u}} = 0.9(580 \text{ lb/ft}) + 1.6(-600 \text{ lb/ft}) \text{ } [uplift] = -438 \text{ lb/ft (up)}} \end{aligned}$$

L, R, L_r , E & H don't exist for our case.

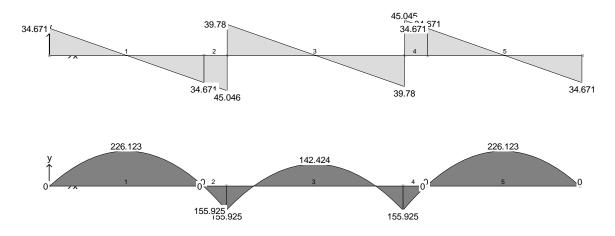
For the largest load case, the shear & bending moment diagrams are:



For the beams, we know that the maximum unbraced length is 6 ft. For the middle 6 feet of the end span, the moment is nearly uniform, so $C_b = 1$ is acceptable ($C_b = 1.08$ for constant moment). For the interior span, C_b is nearly 1 as well.



Choosing a W18x35 (M_u = 229 k-ft) for the end beams, and a W12x30 (M_u = 158 k-ft) for the interior beam, the self weight can be included in the total weight. The diagrams change to:



Check beam shear: $V_u \le \phi_v V_n = 1.0 (0.6 F_{yw} A_w)$

Exterior $V_u = 34.67 \text{ k} \le 1.0(0.6)(50 \text{ ksi})(17.1 \text{ in.})(0.3 \text{ in.}) = 153.9 \text{ k}$ OK

W18x35: d = 17.7 in., $t_w = 0.3$ in., $I_x = 510$ in.⁴

 $Interior \; V_u = 45.05 \; k \; \leq \; 1.0 (0.6) (50 \; ksi) (12.3 \; in.) (0.26 \; in.) = 95.94 \; k \; \; OK$

W12x30: d = 12.3 in., $t_w = 0.26$ in., $I_x = 238$ in.⁴

Check deflection (NO LOAD FACTORS) for total and live load (gravity and snow).

Exterior Beam: worst deflection is from no live load on the center span:



Maximum $\Delta_{\text{total}} = 2.20$ in.

Is
$$\Delta_{\text{total}} \le L/240 = 360 \text{ in.}/240 = 1.5 \text{ in.}$$
? NO GOOD We need an $I \ge (2.20 \text{in.}/1.5 \text{in.})(510 \text{ in.}^4) = 748 \text{ in.}^4$

Maximum $\Delta_{live} = 1.86$ in.

Is
$$\Delta_{live} \le L/360 = 360 \text{ in.}/360 = 1.0 \text{ in.}$$
? NO GOOD

We need an $I \ge (1.86in./1.0in.)(510 in.^4) = 949 in.^4$

The W21x48 looks promising, but it has a note that it exceeds the compact limit for flexure.

Choose a W21 x 50 ($I_x = 984 \text{ in.}^4$) (because the W21x48 would require extra work!)

Now, $\Delta_{live} = 1.07$ in., which is reasonable close.

F _y =	Table 3–2 (continued) W Shapes Selection by Z_x												
	V A _	M_{px}/Ω_b	ф _bМ_{рх}	M_{px}/Ω_b	$\phi_b M_{rx}$	-	BF			W.	V_{nx}/Ω_{v}	φ , V _{n,}	
Shape	Z _x	kip-ft	kip-ft	kip-ft	kip-ft	kips	kips	L _p	L,	I,	kips	kips	
	in.3	ASD	LRFD	ASD	LRFD	ASD	LRFD	ft	ft is	in. ⁴	ASD	LRFD	
W21×55	126	314	473	192	289	10.8	16.3	6.11	17.4	1140	156	234	
W14×74	126	314	473	196	294	5.34	8.03	8.76	31.0	795	128	191	
W18×60	123	307	461	189	284	9.64	14.5	5.93	18.2	984	151	227	
W12×79	119	297	446	187	281	3.77	5.67	10.8	39.9	662	116	175	
W14×68	115	287	431	180	270	5.20	7.81	8.69	29.3	722	117	175	
W10×88	113	282	424	172	259	2.63	3.95	9.29	51.1	534	131	197	
W18×55	112	279	420	172	258	9.26	13.9	5.90	17.5	890	141	212	
W21×50	110	274	413	165	248	12.2	18.3	4.59	13.6	984	158	237	
W12×72	108	269	405	170	256	3.72	5.59	10.7	37.4	597	105	158	
W21×48f	107	265	398	162	244	9.78	14.7	6.09	16.6	959	144	217	
W16×57	105	262	394	161	242	7.98	12.0	5.65	18.3	758	141	212	
W14×61	102	254	383	161	242	4.96	7.46	8.65	27.5	640	104	156	
W18×50	101	252	379	155	233	8.69	13.1.8	5.83	17.0	800	128	192	
W10×77	97.6	244	366	150	225	2.59	3.90	9.18	45.2	455	112	169	
W12×65f	96.8	237	356	154	231	3.60	5.41	11.9	35.1	533	94.5	142	
ASD	LRFD	f Shape e	xceeds c	ompact lin	nit for flex	ure with /	$F_y = 50 \text{ ks}$		mergri	2 - 11	23	0.85	
$ \Omega_b = 1.67 $ $ \Omega_v = 1.50 $	$\phi_b = 0.90 \\ \phi_v = 1.00$	ENV.											

<u>Interior Beam:</u> worst deflection is from load on all spans:



Maximum Δ_{total} (at midspan) = 1.31 in.

Is
$$\Delta_{\text{total}} \le L/240 = 360 \text{ in.}/240 = 1.5 \text{ in.}$$
? OK

Maximum Δ_{live} (at midspan) = 0.94 in.

Is
$$\Delta_{live} \le L/360 = 360 \text{ in.}/360 = 1.0 \text{ in.}$$
? OK

Columns:

The load in the interior columns: $P_u = 85 \text{ k}$ (sum of the shears). This column will see minimal eccentricity from the difference in shear and half the column depth as the moment arm.

The load in the exterior columns: $P_u = 35 \text{ k}$. These columns will see some eccentricity from the beam shear connections. We can determine this by using half the column depth as the eccentricity distance.

The effective length of the columns is 15 ft (no intermediate bracing). Table 4-1 shows design strength in kips for W8 shapes (the smallest). The lightest section at 15 feet has a capacity of 230 k; much greater than what we need even with eccentricity.

The exterior column connection moment (unmagnified) when the W8x31 depth = 8.0in

$$(35k)(8.0in/2)(\frac{1ft}{12in}) = 11.7$$
 k-ft.

The capacity of a W8x31 with an unbraced length of 15 ft (from another beam chart) = 114^{k-ft} .

For
$$\frac{P_r}{P_c} < 0.2$$
: $\frac{P_u}{2\phi_c P_n} + \left(\frac{M_{ux}}{\phi_b M_{nx}} + \frac{M_{uy}}{\phi_b M_{ny}}\right) \le 1.0$

$$\frac{35k}{230k} = 0.15 < 0.2: \qquad \frac{35k}{2(230k)} + \left(\frac{11.7^{k-ft}}{114^{k-ft}}\right) = 0.179 \le 1.0$$

so OK for eccentric loading of the beam-column (but we knew that).

Beam Shear Splice Connection:

For this all-bolted single-plate shear splice, $R_u = 35 \text{ k}$

$$W21x50$$
: $d = 20.8$ in., $t_w = 0.38$ in.

W12x30:
$$d = 12.3$$
 in., $t_w = 0.26$ in.

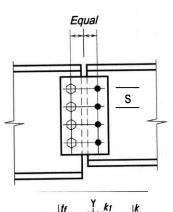
The plate material is A36 with $F_y = 36$ ksi and $F_u = 58$ ksi. We need to check that we can fit a plate within the fillets and provide enough distance from the last holes to the edge.

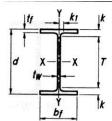
For the W12x30, T = 10.125 in., which limits the plate height.

For a plate, s (hole spacing) = 3" and minimum edge distance is $1\frac{1}{4}$ ".

Table 4-1 (continued)	_
Available Strength in	
Axial Compression, kips	
$F_y = 50 \text{ ksi}$ W Shapes	w8

Sha	ape	W8×								
W	l/ft	3	5	3	411 374 362 348 333 317					
Doc	ian	P_n/Ω_c	$\phi_c P_n$	P_n/Ω_c	$\phi_c P_n$					
Design		ASD	LRFD	ASD	LRFD					
	0	308	463	273	φ _c P _n LRFD 411 374 362 348 333					
^	6	281	423	249						
5	7	272	409	241	362					
2	8	262	394	232	348					
S S	9	251	377	222	333					
5	10	239	359	211	317					
Ĕ	11	226	340	200	301					
2	12	213	321	189	283					
ası	13	200	301	177	266					
<u>e</u>	14	187	281	165	248					
5	15	174	261	153	230					
sbe	16	160	241	141	212					
5	17	147	221	130	195					
	18	135	203	118	178					
2	19	123	184	108	162					
5	20	111	166	97.2	146					
Ě	22	91.5	138	80.3	121					
gua	24	76.9	116	67.5	101					
9	26	65.5	98.5	57.5	86.5					
ŧ	28	56.5	84.9	49.6	74.5					
Effective length KL (ft) with respect to least radius of gyration t_y	30	49.2	74.0	43.2	64.9					
ш	32	43.3	65.0	38.0	57.1					
	34	15000		M 255						





For ¾ in. diameter A325-N bolts and standard holes without a concern for deformation of the holes, the capacity per bolt is:

shear:
$$: R_u \le \phi_v R_n \quad \phi = 0.75, \ R_n = F_n A_b$$
, where $F_n = 54$ ksi
$$35k \le n(0.75)(54ksi) \left[\frac{\pi (0.75in)^2}{4} \right]$$
 so $n \ge 1.96$. Use 2 bolts (1@3 in. + 2@1.25 ≈ 5.5 in. < 10.125 in.)

bearing for 2 rows of bolts:

depends on thickness of thinnest web (t=0.26 in.) and the connected material

$$R_u \le \phi R_n$$
 $\phi = 0.75$, $R_n = 1.5 L_c t F_u \le 3.0 dt F_u$

 $L_c = 1.75$ in. from the vertical edge of the beam to the edge of a hole

$$35k \le 2^{bolts} [0.75(1.5)(1.75in)(0.26in)(65ksi) = 38.0 \text{ k}$$

 $\le 2^{bolts} [0.75(3)(0.75in)(0.26in)(65ksi) = 57.0 \text{ k OK}$

If the spacing between the holes across the splice is 4 in., the eccentricity, e_x is 2 inches. We need to find C, which represents the number of bolts that are effective in resisting the eccentric shear force.

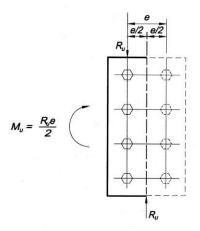


Fig. 10-22. Eccentricity in a symmetrical shear splice.

 r_n is the nominal shear per bolt:

Co	effic	cien	ts C	for	Ecc	entr	e 7-7 ricall e = 0	y Lo	oade	ed B	olt (Grou	ıps
φR _n	able stre or R_n/Ω R_n LRFD $\frac{P_u}{\phi r_n} = \frac{P_u}{\phi r_n}$, is deter	mined w	vith	$r_n = r$ $e = e$ t	nominal seccentric o centro not tabul determina norizonta polt space	force, P_u strength p ity of P wid of bolt ated, maded by geal comporting, in.	per bolt, with responding proup, in the period of the peri	kips ect n. , in.	80 Y		•x=•	P
s, in.	e _x , in.		- 9	at Row.	Nun	nber of E	Bolts in (ı, n			- 10		
111	Α,	1 0	2	3	4	5	6	7	8	9	10	11	12
	2	0.84	2.54	4.48	6.59	8.72	10.8	12.9	15.0	17.0	19.0	21.0	23.0
	3	0.65	2.03	3.68	5.67	7.77	9.91	12.1	14.2	16.3	18.3	20.4	22.
	4	0.54	1.67	3.06	4.86	6.84	8.93	11.1	13.2 12.2	15.4 14.4	17.5 16.5	19.6 18.7	21.
	5	0.45 0.39	1.42 1.22	2.59	4.21 3.69	6.01 5.32	8.00 7.17	9.16	11.2	13.4	15.5	17.7	19.
	6			1.99	3.09	4.74	6.46	8.33	10.3	12.4	14.5	16.7	18.
	7 8	0.35	1.08 0.96	1.78	2.93	4.74	5.86	7.60	9.50	11.5	13.6	15.7	17.
	9	0.31	0.86	1.60	2.65	3.87	5.34	6.97	8.75	10.7	12.7	14.7	16.
			0.00							0.04	44.0	40.0	1
	10	0.26	0.78	1.46	2.42	3.53	4.90	6.42	8.10	9.91	11.8	13.8	15.

$$C_{min} = \frac{35k}{0.75(54ksi)^{(0.75in)^2} \pi/4} = 1.95$$
 (which we found as n)

C off the table is 2.54 bolts which is more than the minimum of 1.95 (which is why we have 2). OK.

If the plate is 3/8 in. thick x 8 in. wide x 9 in. tall, check bolt bearing on plate:

$$\phi R_n = 2.4 dt F_u$$
 (per bolt)
2 bolts[2.4(0.75 in.)(0.375 in.)(58 ksi) = 78.3 k > 35 k OK

Check *flexure of the plate:*

design moment:
$$M_u = \frac{R_u e}{2} = \frac{35k \times 4in}{2} = 70.0 \text{ k-in}$$

<u>yielding capacity:</u> $\phi M_n = \phi F_y S_x \quad \phi = 0.9 \quad (5.5 \text{ in. tall section, } 3/8 \text{ in. thick})$

$$0.9(36ksi) \left| \frac{0.375in(5.5in)^2}{6} \right| = 61.25 \text{ k-in} > 70.0 \text{ k-in NOT OK}$$

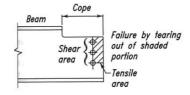
with 6 in. tall, $\phi M_n = 72.9$ k-in

rupture
$$\phi M_n = \phi F_u S_{net} \quad \phi = 0.75$$

 $S_{net} = \frac{I_{net}}{C}$ and can be looked up or calculated = 1.74 in³

 $0.75(58ksi)(1.74in^3) = 75.7 \text{ k-in} > 70.0 \text{ k-in}$ OK

Check shear yielding of the plate:
$$R_u \le \phi R_n \quad \phi = 1.00 \quad R_n = 0.6 F_y A_g$$
 (1.00)[0.6(36 ksi)(6 in.)(0.375 in.)] = 48.6 k > 35 k OK



Check shear rupture of the plate: $R_u \le \phi R_n$ $\phi = 0.75$ $R_n = 0.6 F_u A_{nv}$

for $\frac{3}{4}$ " diameter bolts, the effective hole width is (0.75 + 1/8) = 0.875 in.:

$$(0.75)[0.6(58 \text{ ksi})(6 \text{ in.} -2 \text{ x } 0.875 \text{ in.})(0.375 \text{ in.})] = 41.6 \text{ k} > 35 \text{ k}$$
 OK

Check block shear rupture of the plate: $R_u \le \phi R_n$ $\phi = 0.75$

$$R_n = 0.6F_u A_{nv} + U_{bs} F_u A_{nt} \le 0.6F_v A_{gv} + U_{bs} F_u A_{nt}$$

with $U_{bs} = 0.5$ when the tensile stress is non-uniform. (The tensile stress switches direction across the splice.) (and assuming 2 in. of width to the center of the bolt hole)

$$R_n = 0.60(58ksi)(0.375in)[1.5in + 3in - 1.5^{holes}(0.875)] + 0.5(58ksi)(0.375in)(2in - 0.875in/2) = 58.6.9k$$

$$\leq 0.6(36ksi)(0.375in)(1.5in + 3in) + 0.5(36ksi)(0.375in)(2in - 0.875in/2) = 47.0k$$

$$35 \text{ k} < 0.75(47.0 \text{ k}) = 35.2 \text{ k}$$
 OK

Column Base Plate:

Column base plates are designed for bearing on the concrete (concrete capacity) and plastic hinge development from flexure because the column "punches" down the plate and it could bend upward near the edges of the column (shown as $0.8b_f$ and 0.95d). The plate dimensions are B and N. The concrete has a compressive strength, $f_c = 3 \text{ ksi}$.

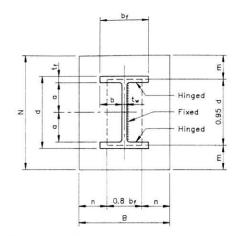


Figure 5.6. Column base plate dimensions

For W8 x 31: d = 8.0 in., $b_f = 8.0$ in., and if we provide width to put in bolt holes, we could use a 12 in. by12 in. plate (allowing about 2 inches each side). We will look at the interior column load of 85 k.

$$minimum \ thickness: \ t_{min} = l \sqrt{\frac{2P_u}{0.9F_yBN}}$$

where l is the larger of m, n and $\lambda n'$

$$m = (N - 0.95d)/2 = (12 \text{ in.} - 0.95 \text{ x } 8.0 \text{ in.})/2 = 2.2 \text{ in.}$$

$$n = (B - 0.8b_f)/2 = (12 \text{ in.} - 0.8 \times 8.0 \text{ in.})/2 = 2.8 \text{ in.}$$

$$n' = \frac{\sqrt{db_f}}{4} = \frac{\sqrt{8.0in \cdot 8.0in}}{4} = 2.0 \text{ in.}$$

 λ is derived from a term X which takes the bounding area of the column, the perimeter, the axial force, and the concrete compressive strength into account:

$$X = \frac{4db_f}{(d+b_f)^2} \cdot \frac{P_u}{\phi_c P_p} = \frac{4db_f}{(d+b_f)^2} \cdot \frac{P_u}{\phi_c (0.85f_c')BN} = \frac{4 \cdot 8.0 in \cdot 8.0 in}{(8.0 in + 8.0 in)^2} \cdot \frac{85k}{0.6(0.85 \cdot 3ksi)12 in \cdot 12 in}$$
$$= 0.386$$

$$\lambda = \frac{2\sqrt{X}}{(1+\sqrt{1-X})} \le 1 \qquad = \frac{2\sqrt{0.386}}{(1+\sqrt{1-0.386})} = 0.697 \text{ so } \lambda n' = (0.697)(2.0 \text{ in.}) = 1.39 \text{ in.}$$

$$t_p = l \sqrt{\frac{2P_u}{0.9F_v BN}} = (2.8in) \sqrt{\frac{2.85k}{0.9(36ksi)(12in)(12in)}} = 0.534 \text{ in.}$$

Use a 9/16 in. thick plate.

The anchor bolts must also be able to resist lateral shear. There also is friction between the steel and concrete to help. The International Building Code provided specifications for minimum edge distances and anchorage.

Continuous Beam Over Interior Column:

The design for this connection will involve a bearing plate at the top of the column, with a minimum number of bolts through the beam flanges to the plate. Because there will be high local compression, stiffener plates for the web will need to be added (refer to a plate girder design). Flexure with a reduced cross section area of the flanges should be checked.

