## Examples: <br> Connections and Tension Members

## Example 1

A nominal $4 \times 6$ in. redwood beam is to be supported by two $2 \times 6$ in. members acting as a spaced column. The minimum spacing and edge distances for the $1 / 2$ inch bolts are shown. How many $1 / 2 \mathrm{in}$. bolts will be required to safely carry a load of 1500 lb ? Use the chart provided.

SOLUTION:
The table requires that the length of the bolt in the main wood member be known, along with the diameter of bolt in inches, and if the bolt is seeing single shear or double shear and what direction it is bearing on the grain.

The main member is the beam. The 4 in . nominal size is actually $31 / 2 \mathrm{in}$. finished:


The bolt is $1 / 2$ inches in diameter, and sees two planes of shear at the interfaces with the $2 \times 6$ 's. This means double shear.

The vertical force is pushing the beam down onto the bolt, so the bolt is in contact with the grain running horizontally. That means the bolt is bearing perpendicular to the grain, and we should look up $q$.

The allowable load per bolt multiplied by the number of bolts will determine the capacity, which we need to be at least 1500 lb :
$q \times n \geq P$
knowing $q$ \& $P$, the equation for $n$ becomes:
$\mathrm{n} \geq \frac{P}{q}=\frac{1500 \mathrm{lb}}{980 \mathrm{lb} / \text { bolt }}=1.5$ bolt

## rounded up $=2$ bolts required

Table: Holding Power of Bolts

| $p=$ Safe loads parallel to grain in pounds <br> $q=$ Safe loads perpendicular to grain in pounds |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Length of Boit in Main Wood Member ${ }^{3}$ (In Inches) | DIAMETER OF BOLT (IN INCHES) |  |  |  |  |  |  |  |  |
|  | 36 | 1/2 | 5\% | $7 / 4$ | 7/8 | ( | 11/8 | 11/4 | 11/2 |
| Single $p$ <br> Shear $q$ | $\begin{aligned} & 325 \\ & 185 \end{aligned}$ | $\begin{aligned} & 470 \\ & 215 \end{aligned}$ | $\begin{aligned} & 590 \\ & 245 \end{aligned}$ | $\begin{aligned} & 710 \\ & 270 \end{aligned}$ | $\begin{aligned} & 830 \\ & 300 \end{aligned}$ | $\begin{aligned} & 945 \\ & 325 \end{aligned}$ |  |  |  |
| Double $p$ <br> Shear $q$ | $\begin{aligned} & 650 \\ & 370 \end{aligned}$ | $\begin{aligned} & 940 \\ & 430 \end{aligned}$ | $\begin{array}{r} 1180 \\ 490 \end{array}$ | $\begin{array}{r} 1420 \\ 540 \end{array}$ | $\begin{array}{r} 1660 \\ 600 \end{array}$ | $\begin{array}{r} 1890 \\ 650 \end{array}$ |  |  |  |
| $\begin{aligned} & \quad \begin{array}{l} \text { Single } p \\ \text { Shear } q \end{array} \\ & \hline \end{aligned}$ |  | $\begin{aligned} & 630 \\ & 360 \end{aligned}$ | $\begin{aligned} & 910 \\ & 405 \end{aligned}$ | $\begin{array}{r} 1155 \\ 450 \end{array}$ | $\begin{array}{r} 1370 \\ 495 \end{array}$ | $\begin{array}{r} 1575 \\ 540 \end{array}$ |  |  |  |
| $21 / 2$ Double $p$ <br> Shear $q$ | $\begin{aligned} & 710 \\ & 620 \\ & \hline \end{aligned}$ | $\begin{array}{r} 1260 \\ 720 \\ \hline \end{array}$ | $\begin{array}{r} 1820 \\ 810 \end{array}$ | $\begin{array}{r} 2310 \\ 900 \end{array}$ | $\begin{array}{r} 2740 \\ 990 \end{array}$ | $\begin{aligned} & 3150 \\ & 1080 \end{aligned}$ |  |  |  |
| Single $p$ Shear $q$ |  |  | $\begin{aligned} & 990 \\ & 565 \end{aligned}$ | $\begin{array}{r} 1400 \\ 630 \end{array}$ | $\begin{array}{r} 1790 \\ 695 \end{array}$ | $\begin{array}{r} 2135 \\ 760 \end{array}$ | $\begin{array}{r} 2455 \\ 825 \end{array}$ | $\begin{array}{r} 2740 \\ 895 \end{array}$ | $\begin{aligned} & 3305 \\ & 1020 \end{aligned}$ |
| $\begin{aligned} & \text { Double } p \\ & \text { Shear } q \end{aligned}$ | $\begin{aligned} & 710 \\ & 640 \end{aligned}$ | $\begin{array}{r} 1270 \\ 980 \end{array}$ | $\begin{aligned} & 1980 \\ & 1130 \end{aligned}$ | $\begin{aligned} & 2800 \\ & 1260 \end{aligned}$ | $\begin{aligned} & 3580 \\ & 1390 \end{aligned}$ | $\begin{aligned} & 4270 \\ & 1520 \end{aligned}$ | $\begin{aligned} & 4910 \\ & 1650 \end{aligned}$ | $\begin{aligned} & 5480 \\ & 1780 \end{aligned}$ | $\begin{aligned} & 6610 \\ & 2040 \end{aligned}$ |

${ }^{1}$ Tabulated values are on a normal load-duration basis and apply to joints made of seasoned lumber used in dry locations. See U.B.C. Standard No. 25-17 for other service conditions.
${ }^{2}$ Double shear values are for joints consisting of three wood members in which the side members are one half the thickness of the main member. Single shear values are for joints consisting of two wood members having a minimum thickness not less than that specified.
${ }^{3}$ The length specified is the length of the bolt in the main member of double shear joints or the length of the bolt in the thinner member of single shear joints.
${ }^{4}$ See U.B.C. Standard No. 25-17 for wood-to-metal bolted joints.

## Example 2

8.11 A built-up plywood box beam with $2 \times 4 \mathrm{~S} 4 \mathrm{~S}$ top and bottom flanges is held together by nails. Determine the pitch (spacing) of the nails if the beam supports a uniform load of 200 \#/ft. along the 26 -foot span. Assume the nails have a shear capacity of $80 \#$ each.


## Solution:

Construct the shear ( $V$ ) diagram to obtain the critical shear condition and its location
Note that the condition of shear is critical at the supports, and the shear intensity decreases as you approach the center line of the beam. This would indicate that the nail spacing $P$ varies from the support to midspan. Nails are closely spaced at the support, but increasing spacing occurs toward midspan, following the shear diagram.

$$
f_{v}=\frac{V Q}{I b}
$$

$$
I_{x}=\frac{\left(4.5^{\prime \prime}\right)\left(18^{\prime \prime}\right)^{3}}{12}-\frac{\left(3.5^{\prime \prime}\right)\left(15^{\prime \prime}\right)^{3}}{12}=1,202.6 \text { in. }{ }^{4}
$$



$$
Q=\Sigma A \bar{y}=\left(9^{\prime \prime}\right)\left(1 / 22^{\prime \prime}\right)\left(4.5^{\prime \prime}\right)+\left(9^{\prime \prime}\right)\left(1 / 22^{\prime \prime}\right)\left(4.5^{\prime \prime}\right)+\left(1.5^{\prime \prime}\right)\left(3.5^{\prime \prime}\right)\left(8.255^{\prime \prime}\right)=83.8 \mathrm{in}^{3}
$$



$$
f_{v-\max }=\frac{(2,600 \#)\left(83.3 \mathrm{in.} .^{3}\right)}{\left(1,202.6 \text { in. }^{4}\right)\left(1 / 2^{\prime 2}+1 / 2^{\prime \prime}\right)}=180.2 \mathrm{psi}
$$

Assume:
$F=$ Capacity of two nails (one each side) at the flange; representing two shear surfaces


$$
Q=A \bar{y}=\left(5.25 \mathrm{in} .^{2}\right)\left(8.25^{\prime \prime}\right)=43.3 \mathrm{in} .^{3}
$$

Shear force $=f_{v} \times A_{v}$
where:

$$
A_{v}=\text { shear area }
$$

(n) $F \geq f_{v} \times b \times p=\frac{V Q}{I b} \times b p$

$\therefore(\mathrm{n}) F \geq p \times \frac{V Q}{I} ; \quad p \leq \frac{(\mathrm{n}) F I}{V Q}$


At the maximum shear location (support) where $V=2,600$ \#

$$
p=\frac{(2 \text { nails } \times 80 \# / \text { nail })\left(1,202.6 \text { in. } .^{4}\right)}{(2,600 \#)\left(43.3 \text { in. }{ }^{3}\right)}=1.71^{\prime \prime}
$$

## Example 3

10.2 The butt splice shown in Figure 10.22 uses two $8 \times$ $3 / 8^{\prime \prime}$ plates to "sandwich" in the $8 \times 1 / 2$ " plates being joined. Four $7 / 8^{\prime \prime} \phi$ A325-SC bolts are used on both sides of the splice. Assuming A36 steel and standard round holes, determine the allowable capacity of the connection.


SOLUTION:
Shear, bearing and net tension will be checked to determine the critical conditions that governs the capacity of the connection. (The edge distance to the holes is presumed to be adequate.)

Shear: Using the AISC available shear in Table 7-3 (Group A):

$$
\phi R_{n}=26.4 \text { k/bolt x } 4 \text { bolts }=105.6 \mathrm{k}
$$

Bearing: Using the AISC available bearing in Table 7-4:
There are 4 bolts bearing on the center ( $1 / 2^{\prime \prime}$ ) plate, while there are 4 bolts bearing on a total width of two sandwich plates (3/4" total). The thinner bearing width will govern. Assume 3 in. spacing (center to center) of bolts. For A36 steel, $\mathrm{F}_{\mathrm{u}}=58 \mathrm{ksi}$.

$$
\phi R_{n}=91.4 \text { k/bolt/in. x } 0.5 \text { in. x } 4 \text { bolts }=182.8 \mathrm{k}
$$

Tension: The center plate is critical, again, because its thickness is less than the combined thicknesses of the two outer plates. We must consider tension yielding and tension rupture:


$$
\phi R_{n}=\phi F_{y} A_{g} \text { and } \phi R_{n}=\phi F_{u} A_{e} \text { where } A_{e}=A_{n e t} U
$$

$A_{g}=8$ in. $x^{1 / 2}$ in. $=4$ in $^{2}$
The holes are considered $1 / 8 \mathrm{in}$. larger than the bolt hole diameter $=(7 / 8+1 / 8)=1.0 \mathrm{in}$.
$A_{n}=\left(8 \mathrm{in} .-2\right.$ holes $\times 1.0 \mathrm{in}$.) $\times 1 / 2 \mathrm{in}$. $=3.0 \mathrm{in}^{2}$
The whole cross section sees tension, so the shear lag factor $U=1$

$$
\begin{aligned}
& \phi F_{y} A_{g}=0.9 \times 36 \mathrm{ksi} \times 4 \mathrm{in}^{2}=129.6 \mathrm{k} \\
& \phi F_{u} A_{e}=0.75 \times 58 \mathrm{ksi} \times(1) \times 3.0 \mathrm{in}^{2}=130.5 \mathrm{k}
\end{aligned}
$$

Block Shear Rupture: It is possible for the center plate to rip away from the sandwich plates
 leaving the block (shown hatched) behind:

$$
\phi R_{n}=\phi\left(0.6 F_{u} A_{n v}+U_{b s} F_{u} A_{n t}\right) \leq \phi\left(0.6 F_{y} A_{g v}+U_{b s} F_{u} A_{n t}\right)
$$

where $A_{n v}$ is the area resisting shear, $A_{n t}$ is the area resisting tension, $A_{g v}$ is the gross area resisting shear, and $U_{b s}=1$ when the tensile stress is uniform.

$$
\begin{aligned}
& A_{g v}=(4+2 \mathrm{in} .) \times 1 / 2 \mathrm{in} .=3 \mathrm{in}^{2} \\
& A_{n v}=A_{g v}-1 \frac{1}{2} \text { holes area }=3 \mathrm{in}^{2}-1.5 \times 1 \mathrm{in} . \times 1 / 2 \mathrm{in} .=2.25 \mathrm{in}^{2} \\
& A_{n t}=3.5 \mathrm{in} . \mathrm{xt}-1 \text { holes }=3.5 \mathrm{in} . \times 1 / 2 \mathrm{in}-1 \times 1 \mathrm{in} . \times 1 / 2 \mathrm{in} .=1.25 \mathrm{in}^{2} \\
& \phi\left(0.6 F_{u} A_{n v}+U_{b s} F_{u} A_{n t}\right)=0.75 \times\left(0.6 \times 58 \mathrm{ksi} \times 2.25 \mathrm{in}^{2}+1 \times 58 \mathrm{ksi} \times 1.25 \mathrm{in}^{2}\right)=113.1 \mathrm{k} \\
& \phi\left(0.6 F_{y} A_{g v}+U_{b s} F_{u} A_{n t}\right)=0.75 \times\left(0.6 \times 36 \mathrm{ksi} \times 3 \mathrm{in}^{2}+1 \times 58 \mathrm{ksi} \times 1.25 \mathrm{in}^{2}\right)=103.0 \mathrm{k}
\end{aligned}
$$

The maximum connection capacity (smallest value) is governed by block shear rupture.

```
\phiRn}=103.0\textrm{k
```


## Example 4

10.7 Determine the capacity of the connection in Figure 10.44 assuming A36 steel with E70XX electrodes.

## Solution:

Capacity of weld:
For a $5 / 16^{\prime \prime}$ fillet weld, $\phi S=6.96 \mathrm{k} / \mathrm{in}$
Weld length $=8$ in +6 in +8 in $=22 \mathrm{in}$.
Weld capacity $=22^{\prime \prime} \times 6.96 \mathrm{k} /$ in $=153.1 \mathrm{k}$

Capacity of plate: $\quad 0.9 \times 36 \mathrm{k} / \mathrm{in}^{2} \times 3 / 8^{\prime \prime} \times 6^{\prime \prime}=72.9 \mathrm{k}$
$\phi P_{n}=\phi F_{y} A_{g} \quad \phi=0.9$
Plate capacity $=0.9 \times 36 \mathrm{k} / \mathrm{in}^{2} \times 3 / 8^{\prime \prime} \times 6^{\prime \prime}=72.9 \mathrm{k}$
$\therefore$ Plate capacity governs, $P_{u}=72.9 \mathrm{k}$

| Available Strength of Fillet Welds <br> per inch of weld $(\phi S)$ |  |  |
| :---: | :---: | :---: |
| Weld Size <br> $(\mathrm{in})$. | E60XX <br> $(\mathrm{k} / \mathrm{in})$. | E70XX <br> $(\mathrm{k} / \mathrm{in})$. |
| $3 / 16$ | 3.58 | 4.18 |
| $1 / 4$ | 4.77 | 5.57 |
| $5 / 16$ | 5.97 | 6.96 |
| $3 / 8$ | 7.16 | 8.35 |
| $7 / 16$ | 8.35 | 9.74 |
| $1 / 2$ | 9.55 | 11.14 |
| $5 / 8$ | 11.93 | 13.92 |
| $3 / 4$ | 14.32 | 16.70 |

(not considering increase in throat with submerged arc weld process)


The weld size used is obviously too strong. What size, then, can the weld be reduced to so that the weld strength is more compatible to the plate capacity? To make the weld capacity $\approx$ plate capacity:

$$
\begin{aligned}
& 22^{\prime \prime} \times(\text { weld capacity per in. })=72.9 \mathrm{k} \\
& \text { Weld capacity per inch }=\frac{72.9 \mathrm{k}}{22 \mathrm{in} .}-3.31 \mathrm{k} / \mathrm{in} \text {. }
\end{aligned}
$$

From Available Strength table, use $3 / 16^{\prime \prime}$ weld

$$
(\phi S=4.18 \mathrm{k} / \mathrm{in} .)
$$

Minimum size fillet $=3 / 16^{\prime \prime}$ based on a $3 / 8^{\prime \prime}$ thick plate.

|  |  |  |  |  | Tabl lab h 0 |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Nominal Bolt Diameter, $d$, in. |  |  |  |  | $5 / 8$0.307 |  | $\begin{gathered} 3 / 4 \\ \hline 0.442 \end{gathered}$ |  | $\begin{gathered} 7 / 8 \\ \hline 0.601 \end{gathered}$ |  | 1 |  |
| Nominal Bolt Area, in. ${ }^{2}$ |  |  |  |  |  |  |  | 785 |  |  |
| ASTM <br> Desig. | Thread Cond. | $F_{n v} / \Omega$ (ksi) | $\phi F_{n v}$ <br> (ksi) | $\begin{gathered} \text { Load- } \\ \text { ing } \end{gathered}$ | $r_{n} / \Omega$ | $\phi r_{n}$ |  |  | $\boldsymbol{r}_{n} / \Omega$ | $\phi r_{n}$ | $r_{n} / \Omega$ | $\phi r_{n}$ | $r_{n} / \Omega$ | $\phi r_{n}$ |
|  |  | ASD | LRFD |  | ASD | LRFD | ASD | LRFD | ASD | LRFD | ASD | LRFD |
| Group A | N | 27.0 | 40.5 | $\begin{aligned} & \mathrm{S} \\ & \mathrm{D} \end{aligned}$ | $\begin{aligned} & 8.29 \\ & 16.6 \end{aligned}$ | $\begin{aligned} & 12.4 \\ & 24.9 \end{aligned}$ | $\begin{aligned} & 11.9 \\ & 23.9 \end{aligned}$ | $\begin{aligned} & 17.9 \\ & 35.8 \end{aligned}$ | $\begin{aligned} & 16.2 \\ & 32.5 \end{aligned}$ | $\begin{aligned} & 24.3 \\ & 48.7 \end{aligned}$ | $\begin{aligned} & 21.2 \\ & 42.4 \end{aligned}$ | $\begin{aligned} & 31.8 \\ & 63.6 \end{aligned}$ |
|  | X | 34.0 | 51.0 | $\begin{aligned} & \mathrm{S} \\ & \mathrm{D} \end{aligned}$ | $\begin{aligned} & 10.4 \\ & 20.9 \end{aligned}$ | $\begin{aligned} & 15.7 \\ & 31.3 \end{aligned}$ | $\begin{aligned} & 15.0 \\ & 30.1 \end{aligned}$ | $\begin{aligned} & 22.5 \\ & 45.1 \end{aligned}$ | $\begin{aligned} & 20.4 \\ & 40.9 \end{aligned}$ | $\begin{aligned} & 30.7 \\ & 61.3 \end{aligned}$ | $\begin{aligned} & 26.7 \\ & 53.4 \end{aligned}$ | $\begin{aligned} & 40.0 \\ & 80.1 \end{aligned}$ |
| Group B | N | 34.0 | 51.0 | $\begin{aligned} & \mathrm{S} \\ & \mathrm{D} \end{aligned}$ | $\begin{aligned} & 10.4 \\ & 20.9 \end{aligned}$ | $\begin{aligned} & 15.7 \\ & 31.3 \end{aligned}$ | $\begin{aligned} & 15.0 \\ & 30.1 \end{aligned}$ | $\begin{aligned} & 22.5 \\ & 45.1 \end{aligned}$ | $\begin{array}{r} 20.4 \\ 40.9 \\ \hline \end{array}$ | $\begin{aligned} & 30.7 \\ & 61.3 \end{aligned}$ | $\begin{array}{r} 26.7 \\ 53.4 \\ \hline \end{array}$ | $\begin{aligned} & 40.0 \\ & 80.1 \\ & \hline \end{aligned}$ |
|  | X | 42.0 | 63.0 | $\begin{aligned} & \mathrm{S} \\ & \mathrm{D} \end{aligned}$ | $\begin{aligned} & 12.9 \\ & 25.8 \end{aligned}$ | $\begin{aligned} & 19.3 \\ & 38.7 \end{aligned}$ | $\begin{aligned} & 18.6 \\ & 37.1 \end{aligned}$ | $\begin{aligned} & 27.8 \\ & 55.7 \end{aligned}$ | $\begin{aligned} & 25.2 \\ & 50.5 \end{aligned}$ | $\begin{aligned} & 37.9 \\ & 75.7 \end{aligned}$ | $\begin{aligned} & 33.0 \\ & 65.9 \end{aligned}$ | $\begin{aligned} & 49.5 \\ & 98.9 \end{aligned}$ |
| A307 | - | 13.5 | 20.3 | $\begin{aligned} & \mathrm{S} \\ & \mathrm{D} \end{aligned}$ | 4.14 <br> 8.29 | $\begin{gathered} 6.23 \\ 12.5 \end{gathered}$ | $\begin{gathered} 5.97 \\ 11.9 \end{gathered}$ | $\begin{gathered} 8.97 \\ 17.9 \end{gathered}$ | $\begin{gathered} 8.11 \\ 16.2 \end{gathered}$ | $\begin{aligned} & 12.2 \\ & 24.4 \end{aligned}$ | $\begin{aligned} & 10.6 \\ & 21.2 \end{aligned}$ | $\begin{aligned} & 15.9 \\ & 31.9 \end{aligned}$ |
| Nominal Bolt Diameter, d, in. |  |  |  |  | 11/8 |  | 11/4 |  | 13/8 |  | 11/2 |  |
| Nominal Bolt Area, in. ${ }^{2}$ |  |  |  |  | 0.994 |  | 1.23 |  | 1.48 |  | 1.77 |  |
| ASTM <br> Desig. | Thread Cond. | $\begin{aligned} & F_{n v} / \Omega \\ & (\mathrm{ksi}) \end{aligned}$ | $\phi F_{n v}$ <br> (ksi) | Loading | $r_{n} / \Omega$ | $\phi r_{n}$ | $r_{n} / \Omega$ | $\phi r_{n}$ | $r_{n} / \Omega$ | $\phi r_{n}$ | $r_{n} / \Omega$ | $\phi r_{n}$ |
|  |  | ASD | LRFD |  | ASD | LRFD | ASD | LRFD | ASD | LRFD | ASD | LRFD |
| Group A | $N$ | 27.0 | 40.5 | $\begin{aligned} & \mathrm{S} \\ & \mathrm{D} \end{aligned}$ | $\begin{aligned} & 26.8 \\ & 53.7 \end{aligned}$ | $\begin{aligned} & 40.3 \\ & 80.5 \end{aligned}$ | $\begin{aligned} & 33.2 \\ & 66.4 \end{aligned}$ | $\begin{aligned} & 49.8 \\ & 99.6 \end{aligned}$ | $\begin{array}{r} 40.0 \\ 79.9 \\ \hline \end{array}$ | $\begin{gathered} 59.9 \\ 120 \\ \hline \end{gathered}$ | $\begin{aligned} & 47.8 \\ & 95.6 \end{aligned}$ | $\begin{gathered} 71.7 \\ 143 \end{gathered}$ |
|  | X | 34.0 | 51.0 | $\begin{aligned} & \mathrm{S} \\ & \mathrm{D} \end{aligned}$ | $\begin{aligned} & 33.8 \\ & 67.6 \end{aligned}$ | $\begin{gathered} 50.7 \\ 101 \end{gathered}$ | $\begin{aligned} & 41.8 \\ & 83.6 \end{aligned}$ | $\begin{array}{\|c\|} \hline 62.7 \\ 125 \end{array}$ | $\begin{array}{\|c\|} \hline 50.3 \\ 101 \end{array}$ | $\begin{gathered} 75.5 \\ 151 \end{gathered}$ | $\begin{gathered} 60.2 \\ 120 \end{gathered}$ | $\begin{gathered} 90.3 \\ 181 \end{gathered}$ |
| Group B | N | 34.0 | 51.0 | $\begin{aligned} & \mathrm{S} \\ & \mathrm{D} \end{aligned}$ | $\begin{aligned} & 33.8 \\ & 67.6 \end{aligned}$ | $\begin{array}{\|c\|} \hline 50.7 \\ 101 \\ \hline \end{array}$ | $\begin{aligned} & 41.8 \\ & 83.6 \end{aligned}$ | $\begin{array}{\|c\|} \hline 62.7 \\ 125 \\ \hline \end{array}$ | 50.3 <br> 101 | $\begin{array}{\|c} 75.5 \\ 151 \\ \hline \end{array}$ | $\begin{gathered} 60.2 \\ 120 \\ \hline \end{gathered}$ | $\begin{array}{\|c\|} \hline 90.3 \\ 181 \\ \hline \end{array}$ |
|  | X | 42.0 | 63.0 | $\begin{aligned} & \mathrm{S} \\ & \mathrm{D} \end{aligned}$ | $\begin{aligned} & 41.7 \\ & 83.5 \end{aligned}$ | $\begin{gathered} 62.6 \\ 125 \end{gathered}$ | $\begin{array}{\|c\|} \hline 51.7 \\ 103 \\ \hline \end{array}$ | $\begin{gathered} 77.5 \\ 155 \end{gathered}$ | $\begin{gathered} 62.2 \\ 124 \end{gathered}$ | $\begin{gathered} 93.2 \\ 186 \end{gathered}$ | $\begin{gathered} 74.3 \\ 149 \end{gathered}$ | $\begin{aligned} & 112 \\ & 223 \end{aligned}$ |
| A307 | - | 13.5 | 20.3 | $\begin{aligned} & \mathrm{S} \\ & \mathrm{D} \end{aligned}$ | $\begin{aligned} & 13.4 \\ & 26.8 \end{aligned}$ | $\begin{aligned} & 20.2 \\ & 40.4 \end{aligned}$ | $\begin{aligned} & 16.6 \\ & 33.2 \end{aligned}$ | $\begin{aligned} & 25.0 \\ & 49.9 \end{aligned}$ | $\begin{aligned} & 20.0 \\ & 40.0 \end{aligned}$ | $\begin{aligned} & 30.0 \\ & 60.1 \end{aligned}$ | $\begin{aligned} & 23.9 \\ & 47.8 \end{aligned}$ | $\begin{aligned} & 35.9 \\ & 71.9 \end{aligned}$ |
| ASD | LRFD | For end loaded connections greater than 38 in., see AISC Specification Table J3.2 footnote b. |  |  |  |  |  |  |  |  |  |  |
| $\Omega=2.00$ | $\phi=0.75$ |  |  |  |  |  |  |  |  |  |  |  |

## Example 5

The steel used in the connection and beams is A992 with $\mathrm{F}_{\mathrm{y}}=50 \mathrm{ksi}$, and $\mathrm{F}_{\mathrm{u}}=65 \mathrm{ksi}$. Using A490-N bolt material, determine the maximum capacity of the connection based on shear in the bolts, bearing in all materials and pick the number of bolts and angle length (not staggered). Use A36 steel for the angles.

W21x93: $\mathrm{d}=21.62 \mathrm{in}, \mathrm{t}_{\mathrm{w}}=0.58 \mathrm{in}, \mathrm{t}_{\mathrm{f}}=0.93 \mathrm{in}$ $\mathrm{W} 10 \times 54: \mathrm{t}_{\mathrm{f}}=0.615$ in

## SOLUTION:



The maximum length the angles can be depends on how it fits between the top and bottom flange with some clearance allowed for the fillet to the flange, and getting an air wrench in to tighten the bolts. This example uses 1 " of clearance:

$$
\begin{aligned}
\text { Available length } & =\text { beam depth }- \text { both flange thicknesses }-1^{\prime \prime} \text { clearance at top } \& 1 " \text { at bottom } \\
& =21.62 \mathrm{in}-2(0.93 \mathrm{in})-2(1 \mathrm{in})=17.76 \mathrm{in} .
\end{aligned}
$$

With the spaced at 3 in. and $1 \frac{1}{4}$ in. end lengths (each end), the maximum number of bolts can be determined:

$$
\begin{aligned}
\text { Available length } & \geq 1.25 \text { in. }+1.25 \text { in. }+3 \text { in. } x \text { (number of bolts }-1) \\
& \text { number of bolts } \leq(17.76 \text { in }-2.5 \text { in. }-(-3 \text { in. })) / 3 \text { in. }=6.1 \text {, so } 6 \text { bolts. }
\end{aligned}
$$

It is helpful to have the All-bolted Double-Angle Connection Tables $10-1$. They are available for $3 / 4^{\prime \prime}, 7 / 8^{\prime \prime}$, and 1 " bolt diameters and list angle thicknesses of $1 / 4$ ", $5 / 16 ", 3 / 8 "$ ", and $1 / 2^{\prime \prime}$. Increasing the angle thickness is likely to increase the angle strength, although the limit states include shear yielding of the angles, shear rupture of the angles, and block shear rupture of the angles.

For these diameters the available shear (double) from Table $7-1$ for 6 bolts is ( 6 ) $41.5 \mathrm{k} /$ bolt $=270.6$ kips, (6) $61.3 \mathrm{k} / \mathrm{bolt}=367.8 \mathrm{kips}$, and (6) $80.1 \mathrm{k} / \mathrm{bolt}=$ 480.6 kips.

Tables 10-1 (not all provided here) list a bolt and angle available strength of 271 kips for the $3 / 4$ " bolts, 296 kips for the 7/8" bolts, and 281 kips for the 1 " bolts. It appears that increasing the bolt diameter to 1 " will not gain additional load. Use 7/8" bolts.

| $\begin{array}{\|c\|c} \underset{W}{E} & F_{y}=50 \mathrm{ksi} \\ \underset{\sim}{\infty} & F_{u}=65 \mathrm{ksi} \end{array}$ | Table 10-1 (continued) All-Bolted Double-Angle Connections |  |  |  |  |  |  |  | 7/8-in.Bolts |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $$ |  |  |  |  |  |  |  |  |  |  |  |
|  | Bolt and Angle Available Strength, kips |  |  |  |  |  |  |  |  |  |  |
|  | $\begin{aligned} & \text { Bolt } \\ & \text { Group } \end{aligned}$ | Thread Cond. | $\begin{aligned} & \text { Hole } \\ & \text { Type } \end{aligned}$ | Angle Thickness, in. |  |  |  |  |  |  |  |
| $\begin{gathered} \hline \text { W40, } 36,33,30,27, \\ 24,21 \end{gathered}$ |  |  |  | $1 / 4$ |  | 5/16 |  | 3/8 |  | 1/2 |  |
|  |  |  |  | ASD | LRFD | ASD | LR | ASD | LRFD | ASD | LRFD |
|  | $\left.\begin{gathered} \text { Group } \\ A \end{gathered} \right\rvert\,$ | N | STD | 98.6 | 148 | 123 | 185 | 148 | 222 | 195 | 292 |
|  |  | x | STD | 98.6 | 148 | 123 | 185 | 148 | 222 | 197 | 296 |
|  |  |  | STD | 8.6 | 148 | ${ }^{106}$ | 159 | ${ }^{106}$ | 159 | ${ }^{106}$ | 159 |
|  |  | Class A | $\begin{aligned} & \text { ovs } \\ & \text { SSLT } \end{aligned}$ | $\begin{array}{\|l\|l\|} 90.1 \\ 97.3 \end{array}$ | $\begin{aligned} & 135 \\ & 146 \end{aligned}$ | $\begin{array}{\|c\|} \hline 90.1 \end{array}$ | 135 159 | $\begin{gathered} 90.1 \\ 106 \end{gathered}$ | 135 159 | $\begin{gathered} 90.1 \\ 106 \end{gathered}$ | 135 159 |
|  |  |  | STD | 98.6 | 148 | 123 | 185 | 148 | 222 | 176 | 264 |
|  |  | Class B | OVS | 93.5 | 140 | 117 | 175 | 140 | 210 | 150 | 225 |
|  |  |  | SSLT | 97.3 | 146 | 122 | 182 | 146 | 219 | 176 | 264 |
|  | $\left\|\begin{array}{c} \text { Group } \\ B \end{array}\right\|$ | N <br> X | STD STD | 98.6 98.6 | $\begin{aligned} & 148 \\ & 148 \end{aligned}$ | $\begin{aligned} & 123 \\ & 123 \end{aligned}$ | 185 185 | $\begin{aligned} & 148 \\ & 148 \end{aligned}$ | 222 222 | $\begin{aligned} & 197 \\ & 197 \end{aligned}$ | 296 296 |
|  |  |  |  | 98.6 | 148 | 123 | 185 | 133 | 199 | 133 | 199 |
|  |  | sc | ovs | 93.5 | 140 | 113 | 169 | 113 | 169 | 113 | 169 |
|  |  |  | SSLT | 97.3 | 146 | 122 | 182 | 133 | 199 | 133 | 199 |
|  |  |  | ${ }^{\text {STD }}$ | 98.6 | 148 | 123 | 185 | 148 | 222 | 197 | 296 |
|  |  | $\underset{\text { Class BC }}{\text { SC }}$ | OVS | 93.5 | 140 | 117 | 175 | 140 | 210 | 187 | 281 |
|  |  |  | SSLT | 97.3 | 146 | 122 | 182 | 146 | 219 | 195 | 292 |

$\phi R_{n}=368.7$ kips for double shear of $7 / 8^{\prime \prime}$ bolts
$\phi R_{n}=296$ kips for limit state in angles

We also need to evaluate bearing of bolts on the beam web, and column flange where there are bolt holes. Table 7-5 provides available bearing strength for the material type, bolt diameter, hole type, and spacing per inch of material thicknesses.
a) Bearing for beam web: There are 6 bolt holes through the beam web. This is typically the critical bearing limit value because there are two angle legs that resist bolt bearing and twice as many bolt holes to the column. The material is A 992 ( $\mathrm{F}_{\mathrm{u}}=65 \mathrm{ksi}$ ), $0.58^{\prime \prime}$ thick, with $7 / 8^{\prime \prime}$ bolt diameters at 3 in . spacing.

$$
\phi R_{n}=6 \text { bolts } \cdot(102 \mathrm{k} / \mathrm{bolt} / \mathrm{inch}) \cdot(0.58 \mathrm{in})=355.0 \mathrm{kips}
$$

b) Bearing for column flange: There are 12 bolt holes through the column. The material is A992 ( $\mathrm{F}_{\mathrm{u}}=65 \mathrm{ksi}$ ), 0.615 " thick, with 1 " bolt diameters.

$$
\phi R_{n}=12 \text { bolts } \cdot(102 \mathrm{k} / \mathrm{bolt} / \mathrm{inch}) \cdot(0.615 \mathrm{in})=752.8 \mathrm{kips}
$$

Although, the bearing in the beam web is the smallest at 355 kips, with the shear on the bolts even smaller at 324.6 kips, the maximum capacity for the simple-shear connector is 296 kips limited by the critical capacity of the angles.


| Based on Bolt Spacing <br> kips/in. thickness |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Hole Type | BoltSpacing, $s$, in. | $F_{l}, \mathrm{ksi}$ | Nominal Bolt Diameter, $d$, in. |  |  |  |  |  |  |  |
|  |  |  | 5/8 |  | $3 / 4$ |  | 7/8 |  | 1 |  |
|  |  |  | $r_{n} / \Omega$ | $\phi r_{n}$ | $r_{n} / \Omega$ | $\phi \boldsymbol{r}_{\boldsymbol{n}}$ | $r_{n} / \Omega$ | $\phi r_{n}$ | $r_{n} / \Omega$ | $\phi r_{n}$ |
|  |  |  | ASD | LRFD | ASD | LRFD | ASD | LRFD | ASD | LRFD |
| $\begin{aligned} & \text { STD } \\ & \text { SSLT } \end{aligned}$ | $2^{2} / 3 d_{b}$ | $\begin{aligned} & 58 \\ & 65 \\ & \hline \end{aligned}$ | $\begin{array}{r} 34.1 \\ 38.2 \\ \hline \end{array}$ | $\begin{aligned} & \hline 51.1 \\ & 57.3 \\ & \hline \end{aligned}$ | $\begin{aligned} & 41.3 \\ & 46.3 \\ & \hline \end{aligned}$ | $\begin{aligned} & \hline 62.0 \\ & 69.5 \\ & \hline \end{aligned}$ | $\begin{aligned} & \hline 48.6 \\ & 54.4 \end{aligned}$ | $\begin{array}{r} 72.9 \\ 81.7 \end{array}$ | $\begin{aligned} & 55.8 \\ & 62.6 \end{aligned}$ | $\begin{aligned} & 83.7 \\ & 93.8 \end{aligned}$ |
|  | 3 in . | $\begin{aligned} & 58 \\ & 65 \end{aligned}$ | $\begin{array}{r} 43.5 \\ 48.8 \\ \hline \end{array}$ | $\begin{aligned} & 65.3 \\ & 73.1 \\ & \hline \end{aligned}$ | $\begin{array}{r} 52.2 \\ 58.5 \\ \hline \end{array}$ | $\begin{array}{r} \hline 78.3 \\ 87.8 \\ \hline \end{array}$ | $\begin{aligned} & 60.9 \\ & 68.3 \\ & \hline \end{aligned}$ | $\begin{gathered} 91.4 \\ 102 \\ \hline \end{gathered}$ | $67.4$ | $\begin{aligned} & 101 \\ & 113 \end{aligned}$ |
| SSLP | $2^{2} / 3 d_{b}$ | $\begin{aligned} & 58 \\ & 65 \\ & \hline \end{aligned}$ | $\begin{array}{r} 27.6 \\ 30.9 \end{array}$ | $\begin{aligned} & 41.3 \\ & 46.3 \end{aligned}$ | $\begin{aligned} & 34.8 \\ & 39.0 \end{aligned}$ | $\begin{aligned} & \hline 52.2 \\ & 58.5 \end{aligned}$ | $\begin{aligned} & 42.1 \\ & 47.1 \end{aligned}$ | $\begin{aligned} & 63.1 \\ & 70.7 \end{aligned}$ | $\begin{aligned} & 47.1 \\ & 52.8 \end{aligned}$ | $\begin{aligned} & 70.7 \\ & 79.2 \end{aligned}$ |
|  | 3 in . | $\begin{aligned} & 58 \\ & 65 \end{aligned}$ | $\begin{array}{r} 43.5 \\ 48.8 \end{array}$ | $\begin{aligned} & 65.3 \\ & 73.1 \end{aligned}$ | $\begin{aligned} & 52.2 \\ & 58.5 \end{aligned}$ | $\begin{aligned} & \hline 78.3 \\ & 87.8 \\ & \hline \end{aligned}$ | $\begin{aligned} & 60.9 \\ & 68.3 \end{aligned}$ | $\begin{gathered} 91.4 \\ 102 \\ \hline \end{gathered}$ | $\begin{aligned} & 58.7 \\ & 65.8 \end{aligned}$ | $\begin{aligned} & 88.1 \\ & 98.7 \end{aligned}$ |
| OVS | $2{ }^{2} / 3 d_{b}$ | $\begin{aligned} & 58 \\ & 65 \\ & \hline \end{aligned}$ | $\begin{aligned} & 29.7 \\ & 33.3 \end{aligned}$ | $\begin{aligned} & 44.6 \\ & 50.0 \end{aligned}$ | $\begin{aligned} & 37.0 \\ & 41.4 \end{aligned}$ | $\begin{aligned} & 55.5 \\ & 62.2 \end{aligned}$ | $\begin{aligned} & 44.2 \\ & 49.6 \end{aligned}$ | $\begin{aligned} & 66.3 \\ & 74.3 \end{aligned}$ | $\begin{aligned} & 49.3 \\ & 55.3 \end{aligned}$ | $\begin{aligned} & 74.0 \\ & 82.9 \end{aligned}$ |
|  | 3 in . | $\begin{aligned} & 58 \\ & 65 \\ & \hline \end{aligned}$ | $\begin{aligned} & 43.5 \\ & 48.8 \end{aligned}$ | $\begin{aligned} & 65.3 \\ & 73.1 \end{aligned}$ | $\begin{array}{r} 52.2 \\ 58.5 \\ \hline \end{array}$ | $\begin{aligned} & \hline 78.3 \\ & 87.8 \\ & \hline \end{aligned}$ | $\begin{aligned} & \hline 60.9 \\ & 68.3 \\ & \hline \end{aligned}$ | $\begin{gathered} 91.4 \\ 102 \end{gathered}$ | $\begin{aligned} & 60.9 \\ & 68.3 \\ & \hline \end{aligned}$ | $\begin{gathered} 91.4 \\ 102 \end{gathered}$ |
| LSLP | $2{ }^{2} / 3 d_{b}$ | $\begin{aligned} & 58 \\ & 65 \end{aligned}$ | $\begin{aligned} & 3.62 \\ & 4.06 \end{aligned}$ | $\begin{aligned} & 5.44 \\ & 6.09 \end{aligned}$ | $\begin{aligned} & 4.35 \\ & 4.88 \end{aligned}$ | $\begin{aligned} & 6.53 \\ & 7.31 \end{aligned}$ | $\begin{aligned} & 5.08 \\ & 5.69 \end{aligned}$ | $\begin{aligned} & 7.61 \\ & 8.53 \end{aligned}$ | $\begin{aligned} & 5.80 \\ & 6.50 \end{aligned}$ | $\begin{aligned} & 8.70 \\ & 9.75 \end{aligned}$ |
|  | 3 in . | $\begin{aligned} & 58 \\ & 65 \end{aligned}$ | $\begin{aligned} & 43.5 \\ & 48.8 \end{aligned}$ | $\begin{aligned} & 65.3 \\ & 73.1 \end{aligned}$ | $\begin{aligned} & 39.2 \\ & 43.9 \end{aligned}$ | $\begin{aligned} & \hline 58.7 \\ & 65.8 \end{aligned}$ | $\begin{aligned} & 28.3 \\ & 31.7 \end{aligned}$ | $\begin{aligned} & \hline 42.4 \\ & 47.5 \end{aligned}$ | $\begin{aligned} & 17.4 \\ & 19.5 \end{aligned}$ | $\begin{aligned} & 26.1 \\ & 29.3 \end{aligned}$ |
| LSLT | $2{ }^{2} / 3 d_{b}$ | $\begin{aligned} & 58 \\ & 65 \end{aligned}$ | $\begin{aligned} & 28.4 \\ & 31.8 \end{aligned}$ | $\begin{aligned} & 42.6 \\ & 47.7 \end{aligned}$ | $\begin{aligned} & 34.4 \\ & 38.6 \end{aligned}$ | $\begin{aligned} & \hline 51.7 \\ & 57.9 \end{aligned}$ | $\begin{aligned} & 40.5 \\ & 45.4 \end{aligned}$ | $\begin{aligned} & 60.7 \\ & 68.0 \end{aligned}$ | $\begin{aligned} & 46.5 \\ & 52.1 \end{aligned}$ | $\begin{aligned} & 69.8 \\ & 78.2 \end{aligned}$ |
|  | 3 in . | $\begin{aligned} & 58 \\ & 65 \\ & \hline \end{aligned}$ | $\begin{aligned} & 36.3 \\ & 40.6 \end{aligned}$ | $\begin{aligned} & 54.4 \\ & 60.9 \end{aligned}$ | $\begin{aligned} & 43.5 \\ & 48.8 \end{aligned}$ | $\begin{aligned} & 65.3 \\ & 73.1 \end{aligned}$ | $\begin{aligned} & 50.8 \\ & 56.9 \end{aligned}$ | $\begin{aligned} & 76.1 \\ & 85.3 \end{aligned}$ | $\begin{aligned} & 56.2 \\ & 63.0 \end{aligned}$ | $\begin{aligned} & 84.3 \\ & 94.5 \\ & \hline \end{aligned}$ |
| $\begin{gathered} \hline \text { STD, SSLT, } \\ \text { SSLP, OVS, } \\ \text { LSLP } \\ \hline \end{gathered}$ | $s \geq s_{\text {full }}$ | $\begin{aligned} & 58 \\ & 65 \end{aligned}$ | $\begin{aligned} & 43.5 \\ & 48.8 \end{aligned}$ | $\begin{aligned} & 65.3 \\ & 73.1 \end{aligned}$ | $\begin{aligned} & 52.2 \\ & 58.5 \end{aligned}$ | $\begin{aligned} & 78.3 \\ & 87.8 \end{aligned}$ | $\begin{aligned} & 60.9 \\ & 68.3 \end{aligned}$ | $\begin{gathered} 91.4 \\ 102 \end{gathered}$ | $\begin{aligned} & 69.6 \\ & 78.0 \end{aligned}$ | $\begin{aligned} & 104 \\ & 117 \end{aligned}$ |
| LSLT | $s \geq s_{\text {full }}$ | $\begin{aligned} & 58 \\ & 65 \end{aligned}$ | $\begin{aligned} & 36.3 \\ & 40.6 \end{aligned}$ | $\begin{aligned} & 54.4 \\ & 60.9 \end{aligned}$ | $\begin{aligned} & 43.5 \\ & 48.8 \end{aligned}$ | $\begin{aligned} & \hline 65.3 \\ & 73.1 \end{aligned}$ | $\begin{aligned} & 50.8 \\ & 56.9 \end{aligned}$ | $\begin{array}{r} 76.1 \\ 85.3 \\ \hline \end{array}$ | $\begin{aligned} & 58.0 \\ & 65.0 \\ & \hline \end{aligned}$ | $\begin{aligned} & 87.0 \\ & 97.5 \\ & \hline \end{aligned}$ |
| Spacing for full bearing strength $s_{\text {fuli }}{ }^{\text {a }}$, in. |  | $\begin{aligned} & \text { STD, } \\ & \text { SSLT, } \\ & \text { LSLT } \end{aligned}$ | 15/16 |  | 25/16 |  | 211/16 |  | $3^{1 / 16}$ |  |
|  |  | OVS | 21/16 |  | $2^{7 / 16}$ |  | $2^{13 / 16}$ |  | $31 / 4$ |  |
|  |  | SSLP | $21 / 8$ |  | $21 / 2$ |  | 27/8 |  | $35 / 16$ |  |
|  |  | LSLP | $2^{13 / 16}$ |  | 33/8 |  | $3^{15 / 16}$ |  | $41 / 2$ |  |
| Minimum Spacing ${ }^{2}=2^{2 / 3} d$, in. |  |  | 111/16 |  | 2 |  | $25 / 16$ |  | $2^{11 / 16}$ |  |
| $\begin{aligned} & \text { STD = standard hole } \\ & \text { SSLT = short-slotted hole oriented transverse to the line of force } \\ & \text { SSLP = short-slotted hole oriented parallel to the line of force } \\ & \text { OVS = oversized hole } \\ & \text { LSLP = long-slotted hole oriented parallel to the line of force } \\ & \text { LSLT = long-slotted hole oriented transverse to the line of force } \end{aligned}$ |  |  |  |  |  |  |  |  |  |  |
| ASD | LRFD | Note: Spacing indicated is from the center of the hole or slot to the center of the adjacent hole or slot in the line of force. Hole deformation is considered. When hole deformation is not considered, see AISC Specification Section J3.10. <br> ${ }^{\text {a }}$ Decimal value has been rounded to the nearest sixteenth of an inch. |  |  |  |  |  |  |  |  |
| $\Omega=2.00$ | $\phi=0.75$ |  |  |  |  |  |  |  |  |  |

