

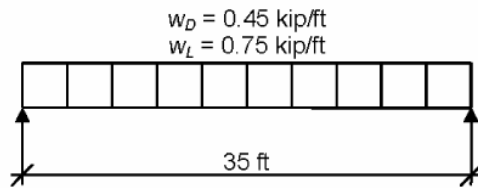
**Examples:  
Steel**

Example 1 (AISC Design Examples vV13.0)

**Example F.1-1a W-Shape Flexural Member Design in Strong-Axis Bending, Continuously Braced.**

**Given:**

Select an ASTM A992 W-shape beam with a simple span of 35 feet. Limit the member to a maximum nominal depth of 18 in. Limit the live load deflection to  $L/360$ . The nominal loads are a uniform dead load of 0.45 kip/ft and a uniform live load of 0.75 kip/ft. Assume the beam is continuously braced.



*Beam Loading & Bracing Diagram  
(full lateral support)*

**Solution:**

**Material Properties:**

ASTM A992  $F_y = 50 \text{ ksi}$   $F_u = 65 \text{ ksi}$

Manual  
Table 2-3

Calculate the required flexural strength

LRFD	ASD
$w_u = 1.2(0.450 \text{ kip/ft}) + 1.6(0.750 \text{ kip/ft})$ $= 1.74 \text{ kip/ft}$	$w_a = 0.450 \text{ kip/ft} + 0.750 \text{ kip/ft}$ $= 1.20 \text{ kip/ft}$
$M_u = \frac{1.74 \text{ kip/ft} (35.0 \text{ ft})^2}{8} = 266 \text{ kip-ft}$	$M_a = \frac{1.20 \text{ kip/ft} (35.0 \text{ ft})^2}{8} = 184 \text{ kip-ft}$

Calculate the required moment of inertia for live-load deflection criterion of  $L/360$

$$\Delta_{max} = \frac{L}{360} = \frac{35.0 \text{ ft}(12 \text{ in./ft})}{360} = 1.17 \text{ in.}$$

$$I_{x(reqd)} = \frac{5wl^4}{384E\Delta_{max}} = \frac{5(0.750 \text{ kip/ft})(35.0 \text{ ft})^4 (12 \text{ in./ft})^3}{384 (29,000 \text{ ksi})(1.17 \text{ in.})} = 748 \text{ in.}^4$$

Manual  
Table 3-23  
Diagram 1

Select a W18x50 from Table 3-2

Per the User Note in Section F2, the section is compact. Since the beam is continuously braced and compact, only the yielding limit state applies.

LRFD	ASD
$\phi_b M_n = \phi_b M_{px} = 379 \text{ kip-ft} > 266 \text{ kip-ft}$ <b>o.k.</b>	$\frac{M_n}{\Omega_b} = \frac{M_{px}}{\Omega_b} = 252 \text{ kip-ft} > 184 \text{ kip-ft}$ <b>o.k.</b>
$I_x = 800 \text{ in.}^4 > 748 \text{ in.}^4$ <b>o.k.</b>	

Manual  
Table 3-2

Manual  
Table 3-2

Example 1 (continued)

**Table 3-2 (continued)**  
**W Shapes**  
**Selection by  $Z_x$**

**Z**  
**X**

$F_y = 50$  ksi

Shape	$Z_x$ in. <sup>3</sup>	$M_{px}/\Omega_b$		$M_{rx}/\Omega_b$		BF		$L_p$ ft	$L_r$ ft	$I_x$ in. <sup>4</sup>	$V_{nx}/\Omega_v$	
		kip-ft	kip-ft	kip-ft	kip-ft	kips	kips				kips	kips
		ASD	LRFD	ASD	LRFD	ASD	LRFD				ASD	LRFD
W21x48 <sup>f</sup>	107	265	398	162	244	9.78	14.7	6.09	16.6	959	144	217
W16x57	105	262	394	161	242	7.98	12.0	5.65	18.3	758	141	212
W14x61	102	254	383	161	242	4.96	7.46	8.65	27.5	640	104	156
W18x50	101	252	379	155	233	8.69	13.1	5.83	17.0	800	128	192
W10x77	97.6	244	366	150	225	2.59	3.90	9.18	45.2	455	112	169
W12x65 <sup>f</sup>	96.8	237	356	154	231	3.60	5.41	11.9	35.1	533	94.5	148
<b>W21x44</b>	<b>95.4</b>	<b>238</b>	<b>358</b>	<b>143</b>	<b>214</b>	<b>11.2</b>	<b>16.8</b>	<b>4.45</b>	<b>13.0</b>	<b>843</b>	<b>145</b>	<b>217</b>
W16x50	92.0	230	345	141	213	7.59	11.4	5.62	17.2	659	124	185
W18x46	90.7	226	340	138	207	9.71	14.6	4.56	13.7	712	130	195
W14x53	87.1	217	327	136	204	5.27	7.93	6.78	22.2	541	103	155
W12x58	86.4	216	324	136	205	3.76	5.66	8.87	29.9	475	87.8	132
W10x68	85.3	213	320	132	199	2.57	3.86	9.15	40.6	394	97.8	147
W16x45	82.3	205	309	127	191	7.16	10.8	5.55	16.5	586	111	167
W18x40	78.4	196	294	119	180	8.86	13.3	4.49	13.1	612	113	169
W14x48	78.4	196	294	123	184	5.10	7.66	6.75	21.1	484	93.8	141
W12x53	77.9	194	292	123	185	3.65	5.48	8.76	28.2	425	83.2	125
W10x60	74.6	186	280	116	175	2.53	3.80	9.08	36.6	341	85.8	129

ASD    LRFD    <sup>f</sup> Shape exceeds compact limit for flexure with  $F_y = 50$  ksi.

$\Omega_y = 1.67$      $\phi_b = 0.90$   
 $\Omega_v = 1.50$      $\phi_v = 1.00$

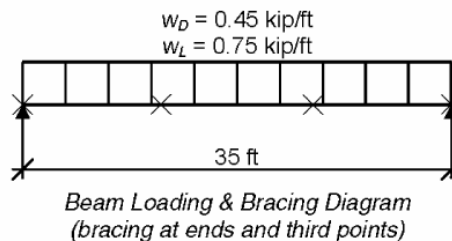
I required is in this grouping, with the W21x44 (bold) the most economical. But this section must be 18 inches maximum, and the W18 x 46 does not have enough (even though it has enough moment capacity of 340 k-ft ( $\phi_b M_{px}$ )).

Look to the next section above for a W18 with  $I > 748$  in<sup>4</sup>.

**Example F.1-2a    W-Shape Flexural Member Design in Strong-Axis Bending, Braced at Third Points**

Given:

Verify the strength of the W18x50 beam selected in Example F.1-1a if the beam is braced at the ends and third points rather than continuously braced.



Solution:

Required flexural strength at midspan from Example F.1-1a

LRFD	ASD
$M_u = 266$ kip-ft	$M_a = 184$ kip-ft

Example 1 (continued)

$$L_b = \frac{35.0 \text{ ft}}{3} = 11.7 \text{ ft}$$

By inspection, the middle segment will govern. For a uniformly loaded beam braced at the ends and third points,  $C_b = 1.01$  in the middle segment. Conservatively neglect this small adjustment in this case.

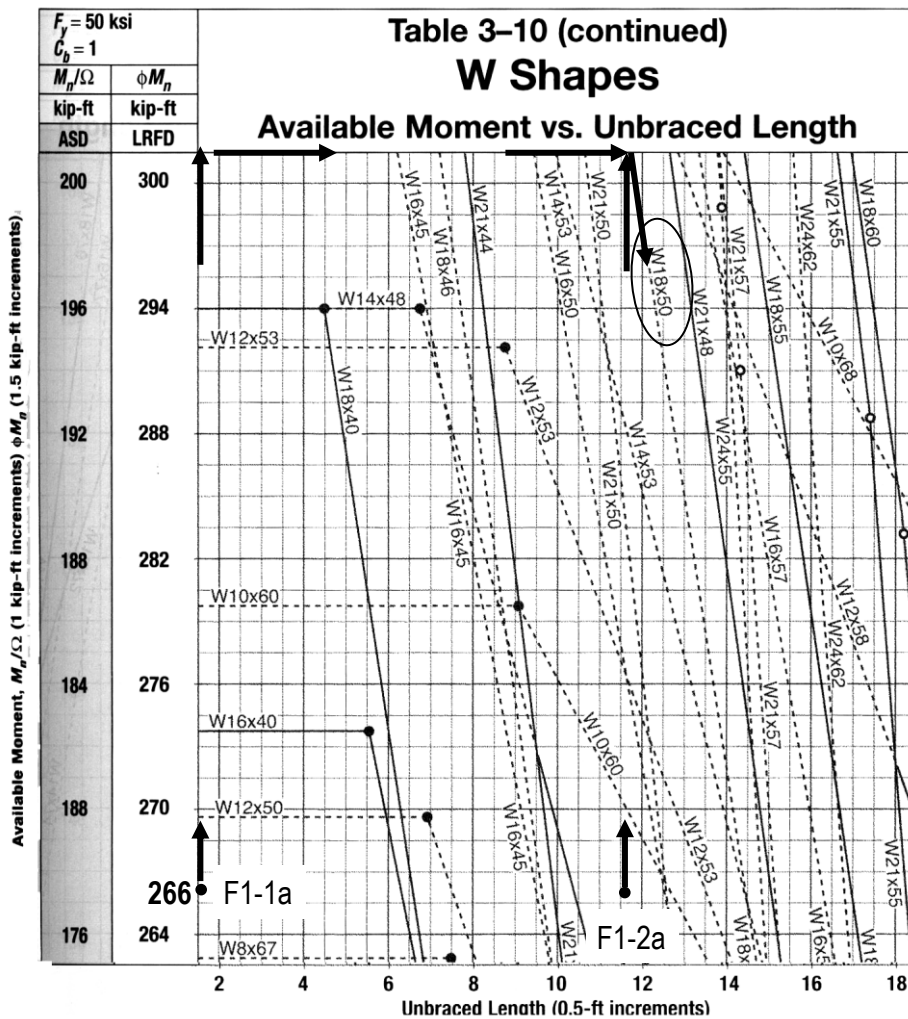
Manual  
Table 3-1

Obtain the available strength from Table 3-10

Enter Table 3-10 and find the intersection of the curve for the W18x50 with an unbraced length of 11.7 ft. Obtain the available strength from the appropriate vertical scale to the left.

LRFD	ASD
$\phi_b M_n \approx 302 \text{ kip-ft} > 266 \text{ kip-ft}$ o.k.	$\frac{M_n}{\Omega_b} \approx 201 \text{ kip-ft} > 184 \text{ kip-ft}$ o.k.

Manual  
Table 3-10



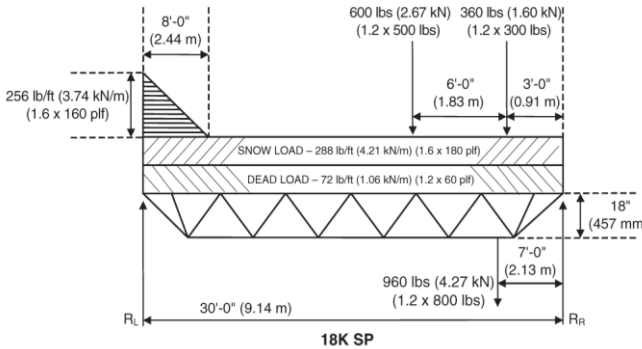
For F1-1a, the unbraced length is zero. There is no zero on the chart, so the far left is used starting at the moment required of 266 k-ft. When a W18 is not encountered with a greater moment capacity going up on the page, going to the right will intersect with a W18 line.

For F1-2a, the unbraced length is 11.7 ft. The same procedure applies, starting at a moment required of 266 k-ft. If no match is close to the

**Example 2 (LRFD)**

**U.S. CUSTOMARY UNITS AND (METRIC UNITS)**

**Factored Load diagram per ASCE 7 2.3.2(3) 1.2D + 1.6S**



Joist manufacturer to design joist to support factored loads as shown.

Joist Supplier to design joist to support loads as shown above.

$$\text{Total Load} = \frac{256}{2}(8) + (288 + 72)(30) + 600 + 960 + 360 = 13,744 \text{ lbs.}$$

$$R_L = \frac{256(8)}{2} \left[ \frac{30 - \frac{8}{3}}{30} \right] + \frac{(288 + 72)(30)}{2} + 600 \left[ \frac{9}{30} \right] + 960 \left[ \frac{7}{30} \right] + 660 \left[ \frac{3}{30} \right] =$$

$R_L = 6773 \text{ lbs.}$

$R_R = 6971 \text{ lbs.}$

Assume  $R_R = \frac{W_{e1}(L)}{2}$ ,  $W_{e1} = \frac{2(6971)}{30} = 465 \text{ lbs/ft}$

Point of Max. Mom. = Point of Zero Shear (V) =  $L_1$   
(dist. from rt. end of Jst)

$V = \text{Zero} = 6971 - (360 + 600 + 960) - (288 + 72)(L_1)$

$L_1 = 14.03 \text{ ft.}$

$M @ L_1 = 6971(14.03) - 360(11.03) - 960(7.03) - 600(5.03) - \frac{(288+72)(14.03)^2}{2}$

$M = 48,634 \text{ ft. lbs.}$

Assume  $M = \frac{W_{e2}(L)^2}{8}$ ,  $W_{e2} = \frac{8(48,634)}{(30)^2} = 432.3 \text{ lbs./ft.}$

Using  $W_{e1} = 465 \text{ LB/ft. @ SPAN} = 30'$ ,  
and  $D = 18''$

Select 18K7 for total load (502) and live load (180) and call it: **18K9SP**

**(c) Special Considerations**

The **specifying professional** shall indicate on the construction documents special considerations including:

- a) Profiles for non-standard joist and Joist Girder configurations (Standard joist and Joist Girder configurations are as indicated in the Steel Joist Institute Standard Specifications Load Tables & Weight Tables of latest adoption).
- b) Oversized or other non-standard web openings
- c) Extended ends
- d) Deflection criteria for live and total loads for non-SJI standard joists
- e) Non-SJI standard bridging

**LRFD**

**STANDARD LOAD TABLE FOR OPEN WEB STEEL JOISTS, K-SERIES**

Based on a 50 ksi Maximum Yield Strength – Loads shown in Pounds per Linear Foot (plf)

Joist Designation	18K3	18K4	18K5	18K6	18K7	18K9	18K10
Depth (In.)	18	18	18	18	18	18	18
Approx. Wt. (lbs./ft.)	6.6	7.2	7.7	8.5	9	10.2	11.7
Span (ft.)							
↓							
18	825 550	825 550	825 550	825 550	825 550	825 550	825 550
19	771 494	825 523	825 523	825 523	825 523	825 523	825 523
20	694 423	825 490	825 490	825 490	825 490	825 490	825 490
21	630 364	759 426	825 460	825 460	825 460	825 460	825 460
22	573 316	690 370	777 414	825 438	825 438	825 438	825 438
23	523 276	630 323	709 362	774 393	825 418	825 418	825 418
24	480 242	577 284	651 318	709 345	789 382	825 396	825 396
25	441 214	532 250	600 281	652 305	727 337	825 377	825 377
26	408 190	492 222	553 249	603 271	672 299	807 354	825 361
27	378 169	454 198	513 222	558 241	622 267	747 315	825 347
28	351 151	423 177	477 199	519 216	577 239	694 282	822 331
29	327 136	394 159	444 179	483 194	538 215	646 254	766 298
30	304 123	367 144	414 161	451 175	502 194	603 229	715 269
31	285 111	343 130	387 146	421 158	469 175	564 207	669 243

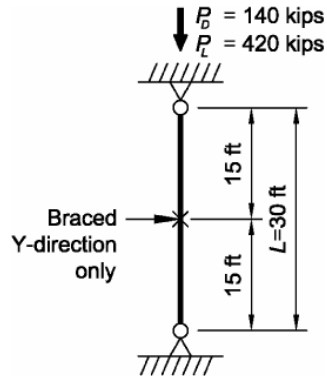
- Top values are total factored distributed load from strength and deflection criteria.
- Values below in gray are for live load deflection limit (unfactored).

Example 3 (AISC Design Examples vV13.0)

**Example E.1b W-Shape Column Design with Intermediate Bracing**

**Given:**

Redesign the column from Example E.1a assuming the column is laterally braced about the y-y axis and torsionally braced at the midpoint.



**Solution:**

Calculate the required strength

LRFD	ASD
$P_u = 1.2(140 \text{ kips}) + 1.6(420 \text{ kips}) = 840 \text{ kips}$	$P_a = 140 \text{ kips} + 420 \text{ kips} = 560 \text{ kips}$

Select a column using Manual Table 4-1.

For a pinned-pinned condition,  $K = 1.0$

Since the unbraced lengths differ in the two axes, select the member using the y-y axis then verify the strength in the x-x axis.

Enter Table 4-1 with a y-y axis effective length,  $KL_{y}$ , of 15 ft and proceed across the table until reaching a shape with an available strength that equals or exceeds the required strength. Try a W14x90. A 15 ft long W14x90 provides an available strength in the y-y direction of

LRFD	ASD
$\phi P_n = 1000 \text{ kips}$	$P_n/\Omega = 667 \text{ kips}$

The  $r_x/r_y$  ratio for this column, shown at the bottom of Manual Table 4-1, is 1.66. The equivalent y-y axis effective length for strong axis buckling is computed as

$$KL = \frac{30.0 \text{ ft}}{1.66} = 18 \text{ ft}$$

From the table, the available strength of a W14x90 with an effective length of 18 ft is

LRFD	ASD
$\phi_c P_n = 928 \text{ kips} > 840 \text{ kips}$ <b>o.k.</b>	$P_n/\Omega_c = 618 \text{ kips} > 560 \text{ kips}$ <b>o.k.</b>


The available compression strength is governed by the x-x axis flexural buckling limit state.

Commentary  
Table  
C-C2.2

Manual  
Table 4-1

Example 3 (continued)

**Table 4-1 (continued)**  
**Available Strength in Axial Compression, kips**  
**W Shapes**

  
**W14**

$F_y = 50$  ksi

Shape		W14x											
		145		132		120		109		99		90	
Design	Wt/ft	$P_n/\Omega_c$	$\phi_c P_n$	$P_n/\Omega_c$	$\phi_c P_n$	$P_n/\Omega_c$	$\phi_c P_n$	$P_n/\Omega_c$	$\phi_c P_n$	$P_n/\Omega_c$	$\phi_c P_n$	$P_n/\Omega_c$	$\phi_c P_n$
		ASD	LRFD	ASD	LRFD	ASD	LRFD	ASD	LRFD	ASD	LRFD	ASD	LRFD
Effective length $KL$ (ft) with respect to least radius of gyration $r_y$	0	1280	1920	1160	1740	1060	1590	959	1440	872	1310	792	1190
	6	1250	1870	1130	1700	1030	1550	934	1400	849	1280	771	1160
	7	1240	1860	1120	1680	1020	1530	924	1390	840	1260	763	1150
	8	1220	1840	1110	1660	1010	1510	914	1370	831	1250	754	1130
	9	1210	1820	1090	1640	995	1500	902	1360	820	1230	745	1120
	10	1200	1800	1080	1620	981	1470	889	1340	808	1210	734	1100
	11	1180	1770	1060	1590	965	1450	875	1320	795	1200	722	1090
	12	1160	1740	1040	1570	949	1430	860	1290	781	1170	709	1070
	13	1140	1720	1020	1540	931	1400	844	1270	767	1150	696	1050
	14	1120	1690	1000	1510	912	1370	827	1240	751	1130	682	1020
	15	1100	1650	982	1480	893	1340	809	1220	734	1100	667	1000
	16	1080	1620	959	1440	872	1310	790	1190	717	1080	651	978
	17	1050	1580	936	1410	851	1280	771	1160	699	1050	635	954
	18	1030	1550	912	1370	829	1250	751	1130	681	1020	618	928
	19	1000	1510	887	1330	806	1210	730	1100	662	995	600	902
	20	979	1470	862	1300	783	1180	709	1070	642	966	583	876
	22	926	1390	809	1220	735	1100	665	1000	602	906	546	821
	24	871	1310	756	1140	685	1030	620	932	562	844	509	765
	26	815	1230	702	1050	636	956	575	864	520	782	471	708
	28	759	1140	647	973	586	881	530	797	479	720	434	652
30	702	1060	594	892	537	807	485	730	438	659	397	596	
32	647	972	541	814	489	735	442	664	399	599	361	542	
34	592	890	491	738	443	666	400	601	360	542	326	490	
36	540	811	441	663	398	598	359	540	323	486	292	439	
38	489	734	396	595	357	537	322	484	290	436	262	394	
40	441	663	358	537	322	484	291	437	262	393	236	355	
<b>Properties</b>													
$P_{no}$ (kips)	191	287	175	263	151	227	128	191	111	167	95.9	144	
$P_w$ (kips/in.)	22.7	34.0	21.5	32.3	19.7	29.5	17.5	26.3	16.2	24.3	14.7	22.0	
$P_{no}$ (kips)	477	717	407	612	312	468	220	330	173	260	129	194	
$P_w$ (kips)	222	334	199	298	165	249	138	208	114	171	94.3	142	
$L_p$ (ft)	14.1		13.3		13.2		13.2		13.5		15.2		
$L_r$ (ft)	61.7		56.0		52.0		48.4		45.3		42.6		
$A_g$ (in. <sup>2</sup> )	42.7		38.8		35.3		32.0		29.1		26.5		
$I_x$ (in. <sup>4</sup> )	1710		1530		1380		1240		1110		999		
$I_y$ (in. <sup>4</sup> )	677		548		495		447		402		362		
$r_x$ (in.)	3.98		3.76		3.74		3.73		3.71		3.70		
Ratio $r_x/r_y$	1.59		1.67		1.67		1.67		1.66		1.66		
$P_n (KL^2)/10^4$ (k-in. <sup>2</sup> )	48900		43800		39500		35500		31800		28600		
$P_w (KL^2)/10^4$ (k-in. <sup>2</sup> )	19400		15700		14200		12800		11500		10400		
<b>ASD</b>	<b>LRFD</b>												
$\Omega_c = 1.67$	$\phi_c = 0.90$												

AMERICAN INSTITUTE OF STEEL CONSTRUCTION, INC.

**Example 4 (LRFD)**

Investigate the acceptability of a W16 x 67 used as a beam-column under the unfactored loading shown in the figure. It is A992 steel ( $F_y = 50$  ksi). Assume 25% of the load is dead load with 75% live load.

SOLUTION:

DESIGN LOADS (shown on figure):

$$\text{Axial load} = 1.2(0.25)(350k) + 1.6(0.75)(350k) = 525k$$

$$\text{Moment at joint} = 1.2(0.25)(60 \text{ k-ft}) + 1.6(0.75)(60 \text{ k-ft}) = 90 \text{ k-ft}$$

Determine column capacity and fraction to choose the appropriate interaction equation:

$$\frac{kL}{r_x} = \frac{15 \text{ ft}(12 \text{ in/ft})}{6.96 \text{ in}} = 25.9 \quad \text{and} \quad \frac{kL}{r_y} = \frac{15 \text{ ft}(12 \text{ in/ft})}{2.46 \text{ in}} = 73 \quad (\text{governs})$$

$$P_c = \phi_c P_n = \phi_c F_{cr} A_g = (30.5 \text{ ksi})19.7 \text{ in}^2 = 600.85k$$

$$\frac{P_r}{P_c} = \frac{525k}{600.85k} = 0.87 > 0.2 \quad \text{so use} \quad \frac{P_u}{\phi_c P_n} + \frac{8}{9} \left( \frac{M_{ux}}{\phi_b M_{nx}} + \frac{M_{uy}}{\phi_b M_{ny}} \right) \leq 1.0$$

There is no bending about the y axis, so that term will not have any values.

Determine the bending moment capacity in the x direction:

The unbraced length to use the full plastic moment ( $L_p$ ) is listed as 8.69 ft, and we are over that so of we don't want to determine it from formula, we can find the beam in the Available Moment vs. Unbraced Length tables. The value of  $\phi M_n$  at  $L_b = 15$  ft is 422 k-ft.

Determine the magnification factor when  $M_1 = 0$ ,  $M_2 = 90$  k-ft:

$$C_m = 0.6 - 0.4 \frac{M_1}{M_2} = 0.6 - \frac{0^{k-ft}}{90^{k-ft}} = 0.6 \leq 1.0 \quad P_{e1} = \frac{\pi^2 EA}{(KL/r)^2} = \frac{\pi^2 (30 \times 10^3 \text{ ksi})19.7 \text{ in}^2}{(25.9)^2} = 8,695.4k$$

$$B_1 = \frac{C_m}{1 - (P_u/P_{e1})} = \frac{0.6}{1 - (525k/8695.4k)} = 0.64 \geq 1.0 \quad \text{USE } 1.0 \quad M_u = (1)90 \text{ k-ft}$$

Finally, determine the interaction value:

$$\frac{P_u}{\phi_c P_n} + \frac{8}{9} \left( \frac{M_{ux}}{\phi_b M_{nx}} + \frac{M_{uy}}{\phi_b M_{ny}} \right) = 0.87 + \frac{8}{9} \left( \frac{90^{k-ft}}{422^{k-ft}} \right) = 1.06 \leq 1.0$$

This is **NOT OK**. (and outside error tolerance).  
The section should be larger.

