

**Examples:  
Timber**

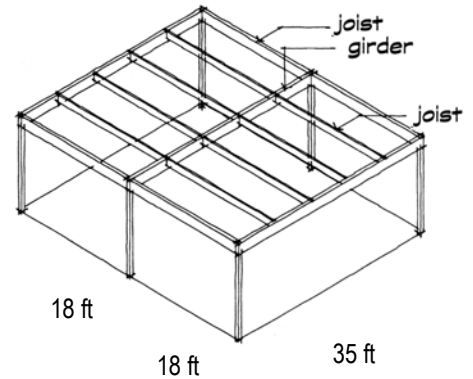
Example 1

Design a Flat Roof joist, 16 in. on center (o.c.), 18 ft span with Douglas fir-larch No. 2. Snow load is 30 psf. Dead load (including ballast, roofing, sheathing, joists & ceiling) = 18.9 psf.  $C_r = 1.15$  for bending only.

$$F_b = 875 \text{ psi}; F_v = 95 \text{ psi}; E = 1.6 \times 10^6 \text{ psi}$$

Also design the glulam girder supporting the joists if it spans 35 ft (simply supported) and  $F_b = 2400 \text{ psi}$ .

Assume the density of the glulam timber is  $32 \text{ lb/ft}^3$ .



SOLUTION:

The load case that is most likely to govern the design is Dead + Live. Because the live load is from snow,  $C_D = 1.15$ :

$$\frac{18.9 \text{ psf}}{0.9} = 21 \text{ psf} < \frac{(18.9 \text{ psf} + 30 \text{ psf})}{1.15} = 42.5 \text{ psf}$$

Joist

The distributed load for each joist needs to be found by multiplying the area load by the tributary width:

$$w = (30 \text{ lb/ft}^2 + 18.9 \text{ lb/ft}^2)(16 \text{ in})(1 \text{ ft}/12 \text{ in}) = 65.2 \text{ lb/ft}$$

$$M_{\text{max}} = \frac{wl^2}{8} = \frac{(65.2 \text{ lb/ft})(18 \text{ ft})^2}{8} = 2641 \text{ lb-ft}$$

Allowable stress is the tabulated stress multiplied by all applicable adjustment factors, which would be  $C_D$  and  $C_r$ :

$$F'_b = F_b C_D C_r = 875 \text{ lb/in}^2 (1.15)(1.15) = 1157 \text{ lb/in}^2$$

$$S_{\text{req'd}} \geq \frac{M}{F'_b} = \frac{2641 \text{ lb-ft}}{1157 \text{ lb/in}^2} \cdot (12 \text{ in/ft}) = 27.4 \text{ in}^3$$

Shear can quite often govern the design of timber beams:

$$V_{\text{max}} = \frac{wl}{2} = \frac{(65.2 \text{ lb/ft})(18 \text{ ft})}{2} = 587 \text{ lb}$$

Allowable stress is the tabulated stress multiplied by all applicable adjustment factors, which would be  $C_D$  only:

$$F'_v = F_v C_D = 95 \text{ lb/in}^2 (1.15) = 109 \text{ lb/in}^2$$

Shear stress in a rectangular beam is found from  $3V/2A$ :

$$A_{\text{req'd}} \geq \frac{3V}{2F'_v} = \frac{3(587 \text{ lb})}{2(109 \text{ lb/in}^2)} = 8.1 \text{ in}^2$$

**SECTION PROPERTIES  
JOISTS AND BEAMS**



Nominal Size In Inches b h	Surfaced Size In Inches For Design b h	Area (A) A = bh (in <sup>2</sup> )	Section Modulus (S) S = $\frac{bh^2}{6}$ (in <sup>3</sup> )	Moment of Inertia (I) I = $\frac{bh^3}{12}$ (in <sup>4</sup> )	Board Feet Per Linear Foot of Piece
2 x 2	1.5 x 1.5	2.25	0.562	0.422	0.33
2 x 3	1.5 x 2.5	3.75	1.56	1.95	0.50
2 x 4	1.5 x 3.5	5.25	3.06	5.36	0.67
2 x 5	1.5 x 4.5	6.75	5.06	11.39	.83
2 x 6	1.5 x 5.5	8.25	7.56	20.80	1.00
2 x 8	1.5 x 7.25	10.88	13.14	47.63	1.33
2 x 10	1.5 x 9.25	13.88	21.39	98.93	1.67
2 x 12	1.5 x 11.25	16.88	31.64	177.98	2.00
2 x 14	1.5 x 13.25	19.88	43.89	290.78	2.33
3 x 3	2.5 x 2.5	6.25	2.60	3.26	0.75
3 x 4	2.5 x 3.5	8.75	5.10	8.93	1.00
3 x 5	2.5 x 4.5	11.25	8.44	18.98	1.25
3 x 6	2.5 x 5.5	13.75	12.60	34.66	1.50
3 x 8	2.5 x 7.25	18.12	21.90	79.39	2.00
3 x 10	2.5 x 9.25	23.12	35.65	164.89	2.50
3 x 12	2.5 x 11.25	28.12	52.73	296.63	3.00
3 x 14	2.5 x 13.25	33.12	73.15	484.63	3.50
3 x 16	2.5 x 15.25	38.12	96.90	738.87	4.00

Allowable deflection is not known, but  $I_{req'd}$  could be determined from  $\Delta = \frac{5wl^4}{384EI} \leq \Delta_{limit}$  then  $I_{req'd} \geq \frac{5wl^4}{384E\Delta_{limit}}$

From the section property table, a 2 x 12 satisfies  $A_{req'd}$  and  $S_{req'd}$ . (bending governs)

Girder

The distributed load on the girder is the reaction of each joist over the 16 inch spacing plus the self weight of the girder.

Guessing a self weight of 40 lb/ft ( $\approx 32 \text{ lb/ft}^3 \times 1\text{ft}^2$ ):

$$w = \frac{V}{spacing} + s.w. = \frac{587lb}{16in} \cdot \frac{12in}{ft} + 40 \text{ lb/ft} = 480 \text{ lb/ft}$$

$$M_{max} = \frac{wl^2}{8} = \frac{(480 \text{ lb/ft})(35 \text{ ft})^2}{8} = 73,500 \text{ lb-ft}$$

Allowable stress is the tabulated stress multiplied by all applicable adjustment factors, which would be  $C_F$ . The charts provided say that  $C_F$  has been included in the section modulus. If we didn't have a chart that included  $C_F$  and we don't know the depth, we could guess - say 18 inches:

$$C_F = \left(\frac{12}{d}\right)^{1/9} = \left(\frac{12}{18}\right)^{1/9} = 0.956 (< 1) \text{ which would need to be multiplied with all the other adjustment factors by } F_b \text{ to find } F'_b$$

$$S_{req'd} \geq \frac{M}{F'_b} = \frac{73,500 \text{ lb-ft}}{2400 \text{ lb/in}^2} \cdot (12 \text{ in/ft}) = 367.5 \text{ in}^3$$

No information is available to evaluate shear or deflection. Based on that, try a 5 1/8 x 22.5. It has a smaller area than the 8 3/4 section with a big enough adjusted S. (Real S =  $5.125 \times 22.5^2/6 = 432.42 \text{ in}^3$ ,  $C_F = 0.932$ ,  $S_{adjusted} = 403.2 \text{ in}^3$ )

$$\text{Check self weight: } \gamma \cdot A = 32 \text{ lb/ft}^3 (115.3 \text{ in}^2) \left(\frac{1 \text{ ft}}{12 \text{ in}}\right)^2 = 26 \text{ lb/ft} \text{ which is less than what was used.}$$

We could try a smaller section, which would mean calculating a new self weight, then moment, then  $S_{req'd}$  and comparing  $S_{actual}$  to  $S_{req'd}$ .

The lower self weight means a lower design moment, but the smaller  $C_F$  means a smaller allowed stress, so we might end up with the same section.

$w_{revised} = 480 \text{ lb/ft} + (26-40 \text{ lb/ft})$ ,  $M_{revised} = 71,356 \text{ lb-ft}$ ,  $S_{req'd \text{ now}} = 356.8 \text{ in}^3$  and the 5 1/8 x 22.5 is the choice for bending.

Of course, we need to satisfy shear and deflection criteria as well.

	DEPTH, d in.	AREA, A in. <sup>2</sup>	MODIFIED SECTION MODULUS, S <sub>c</sub> in. <sup>3</sup>	MOMENT OF INERTIA, I in. <sup>4</sup>
3 1/4" WIDTH	6.0	18.8	18.8	56
	7.5	23.4	29.3	110
	9.0	28.1	42.2	190
	10.5	32.8	57.4	302
	12.0	37.5	75.0	450
	13.5	42.2	93.7	641
	15.0	46.9	114.3	879
	16.5	51.6	136.9	1,170
	18.0	56.3	161.3	1,519
	19.5	60.9	187.6	1,931
5" WIDTH	21.0	65.6	215.8	2,412
	22.5	70.3	245.9	2,966
	24.0	75.0	277.8	3,600
	7.5	38.4	48.0	180
	9.0	46.1	69.2	311
	10.5	53.8	94.2	494
	12.0	61.5	123.0	738
	13.5	69.2	153.6	1,051
	15.0	76.9	187.5	1,441
	16.5	84.6	224.5	1,919
5 1/8" WIDTH	18.0	92.3	264.6	2,491
	19.5	99.9	307.7	3,167
	21.0	107.6	354.0	3,955
	22.5	115.3	403.2	4,865
	24.0	123.0	455.5	5,904
	25.5	130.7	510.8	7,082
	27.0	138.4	569.0	8,406
	28.5	146.1	630.2	9,887
	30.0	153.8	694.3	11,531
	31.5	161.4	761.4	13,349
6" WIDTH	33.0	169.1	831.3	15,348
	34.5	176.8	904.1	17,538
	36.0	184.5	979.8	19,926
	12.0	31.0	162.0	972
	13.5	31.1	202.4	1,384
	15.0	101.3	246.9	1,898
16.5	111.4	295.6	2,527	
18.0	121.5	348.4	3,280	
19.5	131.6	405.3	4,171	
21.0	141.8	466.2	5,209	
22.5	151.9	531.1	6,407	

Example 2**Example Problem 10.20:  
Design of Wood Columns (Figure 10.66)**

A 22'-tall glu-lam column is required to support a roof load (including snow) of 40 kips. Assuming  $8\frac{3}{4}$ " in one dimension (to match the beam width above), determine the minimum column size if the top and bottom are pin supported.

Select from the following sizes:

$$8\frac{3}{4}" \times 9" \quad (A = 78.75 \text{ in.}^2)$$

$$8\frac{3}{4}" \times 10\frac{1}{2}" \quad (A = 91.88 \text{ in.}^2)$$

$$8\frac{3}{4}" \times 12" \quad (A = 105.00 \text{ in.}^2)$$

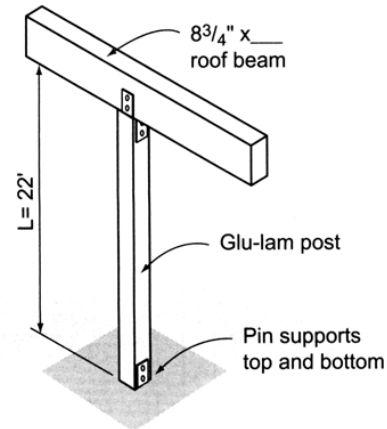


Figure 10.66 Glu-lam column design.

**Solution:**

Glu-lam column: ( $F_c = 1650 \text{ psi}$ ,  $E = 1.8 \times 10^6 \text{ psi}$ )

Try  $8\frac{3}{4}" \times 10\frac{1}{2}"$  ( $A = 105.00 \text{ in.}^2$ )

$$\frac{L_e}{d} = \frac{(22' \times 12 \text{ in./ft.})}{8.75 \text{ in.}}$$

$$= 30.2 < 50 \text{ (max. slenderness ratio)}$$

$$F_{cE} = \frac{0.418E}{(L_e/d)^2} = \frac{0.418(1.8 \times 10^6 \text{ lb./in.}^2)}{(30.2)^2} = 825 \text{ psi}$$

$$F_c^* \cong F_c C_D = (1650 \text{ psi}) \times (1.15)_{\text{(snow)}} = 1900 \text{ psi}$$

$$\frac{F_{cE}}{F_c^*} = \frac{825}{1900} = 0.43$$

From Appendix Table 14:  $C_p = 0.403$

$$F'_c = F_c^* C_p = (1900 \text{ lb./in.}^2) \times (0.403) = 765 \text{ psi}$$

$$P_a = F'_c \times A = (765 \text{ lb./in.}^2) \times (91.9 \text{ in.}^2) \\ = 70,300 \text{ lb.} > 40,000 \text{ lb.}$$

Cycle again, trying a smaller, more economical section. Try  $8\frac{3}{4}" \times 9"$  ( $A = 78.8 \text{ in.}^2$ )

Since the critical dimension is still  $8\frac{3}{4}"$ , the values for  $F_{cE}$ ,  $F_c^*$ , and  $F'_c$  all remain the same as in trial 1. The only change that affects the capability of the column is the available cross-sectional area.

$$\therefore P_a = F'_c \times A = (765 \text{ lb./in.}^2) \times (78.8 \text{ in.}^2) \\ = 60,300 \text{ lb.}$$

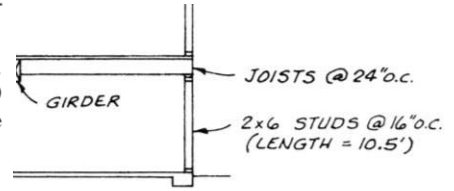
$$P_a = 60.3 \text{ k} > 40 \text{ k}$$

Use  $8\frac{3}{4}" \times 9"$  glu-lam section.

Example 3

**EXAMPLE 7.16 Combined Bending and Compression in a Stud Wall**

Check the 2 × 6 stud in the first-floor bearing wall in the building shown in Fig. 7.20a. Consider the given vertical loads and lateral forces. Lumber is No. 2 DF-L. MC ≤ 19 percent and normal temperatures apply. Allowable stresses are to be in accordance with the NDS.  $F'_b = 2152$  psi  $F_c = 1350$  psi



$A = 8.25$  in<sup>2</sup>  
 $S_x^* = 7.56$  in<sup>3</sup>

COLUMN CAPACITY:

Sheathing provides lateral support about the weak axis of the stud. Therefore, check column buckling about the  $x$  axis only ( $L = 10.5$  ft and  $d_x = 5.5$  in.):

$$\left(\frac{l_e}{d}\right)_y = 0 \quad \text{because of sheathing}$$

$$\left(\frac{l_e}{d}\right)_{\max} = \left(\frac{l_e}{d}\right)_x = \frac{10.5 \text{ ft} \times 12 \text{ in./ft}}{5.5 \text{ in.}} = 22.9$$

$E = 1,600,000$  psi

For visually graded sawn lumber:

$K_{cE} = 0.3$

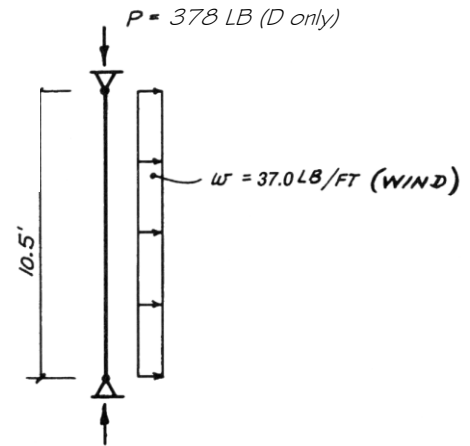
$c = 0.8$

$F_{cE} = \frac{K_{cE} E'}{(l_e/d)^2} = \frac{0.3(1,600,000)}{(22.9)^2} = 915$  psi

$F_c^* = F_c(C_D) \quad C_D = 1.6$  from wind loading  
 $= 1350(1.6) = 2376$  psi

$\frac{F_{cE}}{F_c^*} = \frac{915}{2376} = 0.385 \quad C_P = 0.35$

$F'_c = F_c(C_D)(C_P) = 2376(0.35) = 832$  psi



**Load Case 2: Gravity Loads + Lateral Forces**

BENDING:

Wind governs over seismic. Force to one stud:

Wind = 27.8 psf

$$w = 27.8 \text{ psf} \times \frac{16 \text{ in}}{12 \text{ in/ft}} = 37.0 \text{ lb/ft}$$

$$M = \frac{wL^2}{8} = \frac{37.0(10.5)^2}{8} = 510 \text{ ft-lb} = 6115 \text{ in.-lb}$$

AXIAL:  $f_b = \frac{M}{S} = \frac{6115}{7.56} = 809$  psi  $F'_b = 2152$  psi

D + W:  $f_c = \frac{P}{A} = \frac{378}{8.25} = 46$  psi

COMBINED STRESS:

The simplified interaction formula from Example 7.13 (Sec. 7.12) applies:

$$\left(\frac{f_c}{F'_c}\right)^2 + \frac{f_{bx}}{F'_{bx}(1 - f_c/F_{cEx})} \leq 1.0$$

$F_{cEx} = F_{cE} = 915$  psi

D + W:

In this load combination, D produces the axial stress  $f_c$  and W results in the bending stress  $f_{bx}$ .

$$\left(\frac{f_c}{F'_c}\right)^2 + \left(\frac{1}{1 - f_c/F_{cEx}}\right) \frac{f_{bx}}{F'_{bx}} =$$

$$\left(\frac{46}{832}\right)^2 + \left(\frac{1}{1 - 46/915}\right) \frac{809}{2152} = 0.399 < 1.0$$

2 × 6 No. 2 DF-L exterior bearing wall OK