## **ARCH 614: Practice Quiz 4**

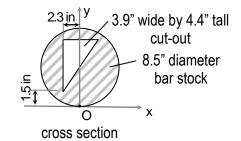
Note: No aids are allowed for part 1. One side of a letter sized paper with notes is allowed during part 2, along with a silent, **non-programm**able calculator. There is a reference chart for part 2 on page 2.

Clearly show your work and answer.

Part 1) Worth 5 points (conceptual questions)

Part 2) Worth 45 points

(NOTE: The units, dimensions, and basic shapes <u>can and will</u> be changed for the quiz! The shape will most likely consist of a solid with a hole of some type.)



A beam has a maximum shear of V = 3.2 k, and maximum bending moment of M = 56 k-ft. If the beam has the cross section shape and reference origin as shown to the right, find:

- a) The location of the centroid of the shape (vertically and horizontally).
- b) The moment of inertia about the x axis,  $I_x$ , of the section [or about the y axis,  $I_y$ ].
- c) The maximum bending stress,  $f_b$ , about the x axis for the section [if  $I_x$  is determined in part b) or is given as 246.68 in.<sup>4</sup>].

	A (in²)	$\bar{x}$ (in)	$\bar{x}A$ (in <sup>2</sup> )	$\overline{y}$ (in)	$\overline{y}A$ (in)	$I_x$ (in <sup>4</sup> )	d <sub>y</sub> (in)	$Ad_{y}^{2}$ (in <sup>3</sup> )
solid								
hole								

Answers – Not provided on actual quiz!

- a)  $\hat{x} = 0.18 \text{ in}, \hat{y} = 4.22 \text{ in}$
- b)  $I_x = 246.68 \text{ in}^4 [\text{or } I_v = 238.88 \text{ in}^4]$
- c)  $f_b = 11.7 \text{ ksi}$

## **REFERENCE CHART FOR QUIZ 4**

## Geometric Properties of Areas

Rectangle	$ \begin{array}{c c} y & y' \\ h & C & x' \\ \hline  & b & x \end{array} $	$\bar{I}_{x'} = \frac{1}{12}bh^{3}$ $\bar{I}_{y'} = \frac{1}{12}b^{3}h$ $I_{x} = \frac{1}{3}bh^{3}  about$ $I_{y} = \frac{1}{3}b^{3}h  bottom$ $I_{y} = \frac{1}{12}bh(b^{2} + h^{2})$	Area = bh $\overline{x}$ = b/2 $\overline{y}$ = h/2
Triangle $\overline{x}$	$ \begin{array}{c c} h & C \\ \hline  & \frac{h}{3} \\  & x \end{array} $	$\bar{I}_{x'} = \frac{1}{36}bh^{3}$ $I_{x} = \frac{1}{12}bh^{3}$ $\bar{I}_{y'} = \frac{1}{36}b^{3}h$	Area = $bh/2$ $\overline{x} = b/3$ $\overline{y} = h/3$
Circle		$ar{I}_x = ar{I}_y = rac{1}{4}\pi r^4$ $J_O = rac{1}{2}\pi r^4$	Area = $\pi r^2 = \pi d^2 / 4$ $\frac{\overline{x}}{\overline{y}} = 0$
Semicircle	$ \begin{array}{c c}  & y \\ \hline  & C \\  & C \\  & C \\  & C \\  & C \\ $	$\bar{I}_x = 0.1098 r^4$ $\bar{I}_y = \pi r^4 / 8$	Area = $\pi r^2 /_2 = \pi d^2 /_8$ $\bar{x} = 0 \qquad \bar{y} = 4r /_{3\pi}$
Quarter circle	$ \begin{array}{c c} y \\ \hline O \\ \hline \end{array} $	$\overline{I}_x = 0.0549 r^4$ $\overline{I}_y = 0.0549 r^4$	Area = $\pi r^2 /_4 = \pi d^2 /_{16}$ $\overline{x} = \frac{4r}{3\pi}$ $\overline{y} = \frac{4r}{3\pi}$
Ellipse	b	$egin{aligned} ar{I}_x &= rac{1}{4}\pi a b^3 \ ar{I}_y &= rac{1}{4}\pi a^3 b \ J_O &= rac{1}{4}\pi a b (a^2 + b^2) \end{aligned}$	Area = $\pi ab$ $ \overline{x} = 0 $ $ \overline{y} = 0 $
Semiparabolic area		$ar{I}_{x}$ = 16ah $^{3}/$ 175	Area = $\frac{4ah}{3}$
Parabolic area		$\overline{I}_y$ = 4a $^3$ h $/$ 15	$\overline{x} = 0$ $\overline{y} = 3h/5$
Parabolic span- drel	$y = kx^{2}$ $\bar{y}$	$\overline{I}_x$ = 37ah $^3/2$ 100 $\overline{I}_y$ = a $^3$ h $/8$ 0	Area = $\frac{ah}{3}$ $\bar{x} = \frac{3a}{4} \qquad \bar{y} = \frac{3h}{10}$