Steel Design

Notation:

a = name for width dimension
A = name for area
A_b = area of a bolt
A_e = effective net area found from the product of the net area A_n by the shear lag factor U
A_g = gross area, equal to the total area ignoring any holes
A_{gv} = gross area subjected to shear for block shear rupture
A_n = net area, equal to the gross area subtracting any holes, as is A_{net}
A_{nt} = net area subjected to tension for block shear rupture
A_{nv} = net area subjected to shear for block shear rupture
A_w = area of the web of a wide flange section
AISC= American Institute of Steel Construction
ASD = allowable stress design
b = name for a (base) width
= total width of material at a horizontal section
= name for height dimension
b_f = width of the flange of a steel beam cross section
B_1 = factor for determining M_u for combined bending and compression
c = largest distance from the neutral axis to the top or bottom edge of a beam
c_1 = coefficient for shear stress for a rectangular bar in torsion
C_b = lateral torsional buckling modification factor for moment in ASD & LRFD steel beam design
C_c = column slenderness classification constant for steel column design
C_m = modification factor accounting for combined stress in steel design
C_v = web shear coefficient
d = calculus symbol for differentiation
= depth of a wide flange section
= nominal bolt diameter
d_b = nominal bolt diameter
D = shorthand for dead load
DL = shorthand for dead load
e = eccentricity
E = shorthand for earthquake load
= modulus of elasticity
f_c = axial compressive stress
f_b = bending stress
f_p = bearing stress
f_v = shear stress
$f_{v\text{-}max}$ = maximum shear stress
f_y = yield stress
F = shorthand for fluid load
$F_{allow(able)}$ = allowable stress
F_a = allowable axial (compressive) stress
F_b = allowable bending stress
F_{cr} = flexural buckling stress
F_e = elastic critical buckling stress
F_{EXX} = yield strength of weld material
F_n = nominal strength in LRFD
= nominal tension or shear strength of a bolt
F_p = allowable bearing stress
F_t = allowable tensile stress
F_u = ultimate stress prior to failure
F_v = allowable shear stress
F_y = yield strength
F_{yw} = yield strength of web material
F.S. = factor of safety
g = gage spacing of staggered bolt holes
G = relative stiffness of columns to beams in a rigid connection, as is Ψ
h = name for a height
h_c = height of the web of a wide flange steel section
H = shorthand for lateral pressure load
I = moment of inertia with respect to neutral axis bending
I_{trial} = moment of inertia of trial section
$I_{req'd}$ = moment of inertia required at limiting deflection
I_y = moment of inertia about the y axis
J = polar moment of inertia

k = distance from outer face of W flange to the web toe of fillet
= shape factor for plastic design of steel beams
K = effective length factor for columns, as is k
l = name for length
ℓ_b = length of beam in rigid joint
ℓ_c = length of column in rigid joint
L = name for length or span length
= shorthand for live load
L_b = unbraced length of a steel beam
L_c = clear distance between the edge of a hole and edge of next hole or edge of the connected steel plate in the direction of the load
L_e = effective length that can buckle for column design, as is ℓ_e
L_r = shorthand for live roof load
= maximum unbraced length of a steel beam in LRFD design for inelastic lateral-torsional buckling
L_p = maximum unbraced length of a steel beam in LRFD design for full plastic flexural strength
L' = length of an angle in a connector with staggered holes
LL = shorthand for live load
$LRFD$ = load and resistance factor design
M = internal bending moment
M_a = required bending moment (ASD)
M_n = nominal flexure strength with the full section at the yield stress for LRFD beam design
M_{max} = maximum internal bending moment
$M_{max\text{-}adj}$ = maximum bending moment adjusted to include self weight
M_p = internal bending moment when all fibers in a cross section reach the yield stress
M_u = maximum moment from factored loads for LRFD beam design
M_y = internal bending moment when the extreme fibers in a cross section reach the yield stress
n = number of bolts
$n.a.$ = shorthand for neutral axis
N = bearing length on a wide flange steel section
= bearing type connection with threads included in shear plane
p = bolt hole spacing (pitch)
P = name for load or axial force vector
P_a = allowable axial force
= required axial force (ASD)
$P_{allowable}$ = allowable axial force
P_c = available axial strength
P_{e1} = Euler buckling strength
P_n = nominal column load capacity in LRFD steel design
P_r = required axial force
P_u = factored column load calculated from load factors in LRFD steel design
Q = first moment area about a neutral axis
= generic axial load quantity for LRFD design
r = radius of gyration
r_y = radius of gyration with respect to a y-axis
R = generic load quantity (force, shear, moment, etc.) for LRFD design
= shorthand for rain or ice load
= radius of curvature of a deformed beam
R_a = required strength (ASD)
R_n = nominal value (capacity) to be multiplied by ϕ in LRFD and divided by the safety factor Ω in ASD
R_u = factored design value for LRFD design
s = longitudinal center-to-center spacing of any two consecutive holes
S = shorthand for snow load
= section modulus
= allowable strength per length of a weld for a given size
$S_{req'd}$ = section modulus required at allowable stress
$S_{req'd\text{-}adj}$ = section modulus required at allowable stress when moment is adjusted to include self weight
SC = slip critical bolted connection

t = thickness of the connected material

t_f = thickness of flange of wide flange

t_w = thickness of web of wide flange

T = torque (axial moment)

= shorthand for thermal load

= throat size of a weld

U = shear lag factor for steel tension member design

U_{bs} = reduction coefficient for block shear rupture

V = internal shear force

V_a = required shear (ASD)

V_{max} = maximum internal shear force

$V_{max\text{-}adj}$ = maximum internal shear force adjusted to include self weight

V_n = nominal shear strength capacity for LRFD beam design

V_u = maximum shear from factored loads for LRFD beam design

w = name for distributed load

$w_{adjusted}$ = adjusted distributed load for equivalent live load deflection limit

$w_{equivalent}$ = the equivalent distributed load derived from the maximum bending moment

$w_{self\ wt}$ = name for distributed load from self weight of member

W = shorthand for wind load

x = horizontal distance

X = bearing type connection with threads excluded from the shear plane

y = vertical distance

Z = plastic section modulus of a steel beam

$Z_{req'd}$ = plastic section modulus required

Z_x = plastic section modulus of a steel beam with respect to the x axis

α = method factor for B_1 equation

Δ_{actual} = actual beam deflection

$\Delta_{allowable}$ = allowable beam deflection

Δ_{limit} = allowable beam deflection limit

Δ_{max} = maximum beam deflection

ε_y = yield strain (no units)

ϕ = resistance factor

= diameter symbol

ϕ_b = resistance factor for bending for LRFD

ϕ_c = resistance factor for compression for LRFD

ϕ_t = resistance factor for tension for LRFD

ϕ_v = resistance factor for shear for LRFD

γ = load factor in LRFD design

π = pi (3.1415 radians or 180°)

θ = slope of the beam deflection curve

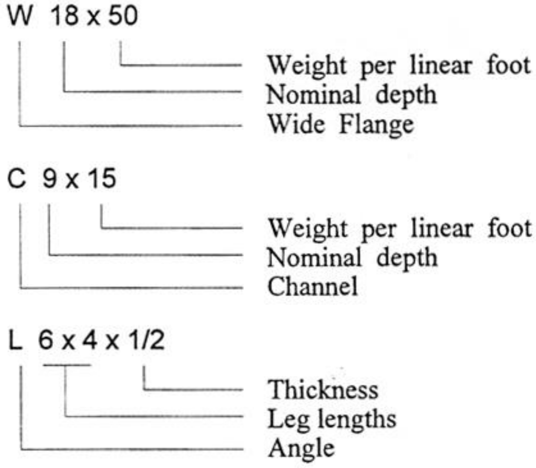
ρ = radial distance

Ω = safety factor for ASD

$\int$ = symbol for integration

Σ = summation symbol

Steel Design



Structural design standards for steel are established by the *Manual of Steel Construction* published by the American Institute of Steel Construction, and uses **Allowable Stress Design** and **Load and Factor Resistance Design**. With the 13th edition, both methods are combined in one volume which provides common requirements for analyses and design and requires the application of the same set of specifications.

Materials

American Society for Testing Materials (ASTM) is the organization responsible for material and other standards related to manufacturing. Materials meeting their standards are guaranteed to have the published strength and material properties for a designation.

A36 – carbon steel used for plates, angles	F_y = 36 ksi, F_u = 58 ksi, E = 29,000 ksi
A572 – high strength low-alloy use for some beams	F_y = 60 ksi, F_u = 75 ksi, E = 29,000 ksi
A992 – for building framing used for most beams	F_y = 50 ksi, F_u = 65 ksi, E = 29,000 ksi

(A572 Grade 50 has the same properties as A992)

ASD $R_a \leq R_n/\Omega$

where R_a = required strength (dead or live; force, moment or stress)
R_n = nominal strength specified for ASD
Ω = safety factor

Factors of Safety are applied to the limit stresses for allowable stress values:

bending (braced, $L_b < L_p$)	Ω = 1.67
bending (unbraced, $L_p < L_b$ and $L_b > L_r$)	Ω = 1.67 (nominal moment reduces)
shear (beams)	Ω = 1.5 or 1.67
shear (bolts)	Ω = 2.00 (tabular nominal strength)
shear (welds)	Ω = 2.00

- L_b is the unbraced length between bracing points, laterally
- L_p is the limiting laterally unbraced length for the limit state of yielding
- L_r is the limiting laterally unbraced length for the limit state of inelastic lateral-torsional buckling

LRFD $R_u \leq \phi R_n$ $where \cdots R_u = \Sigma \gamma_i R_i$

where ϕ = resistance factor
γ = load factor for the type of load
R = load (dead or live; force, moment or stress)
R_u = factored load (moment or stress)
R_n = nominal load (ultimate capacity; force, moment or stress)

Nominal strength is defined as the

> capacity of a structure or component to resist the effects of loads, as determined by computations using specified material strengths (such as yield strength, F_y, or ultimate strength, F_u) and dimensions and formulas derived from accepted principles of structural mechanics or by field tests or laboratory tests of scaled models, allowing for modeling effects and differences between laboratory and field conditions

Factored Load Combinations

The design strength, ϕR_n, of each structural element or structural assembly must equal or exceed the design strength based on the ASCE-7 (2010) combinations of factored nominal loads:

$1.4D$
$1.2D + 1.6L + 0.5(L_r \text{ or } S \text{ or } R)$
$1.2D + 1.6(L_r \text{ or } S \text{ or } R) + (L \text{ or } 0.5W)$
$1.2D + 1.0W + L + 0.5(L_r \text{ or } S \text{ or } R)$
$1.2D + 1.0E + L + 0.2S$
$0.9D + 1.0W$
$0.9D + 1.0E$

Criteria for Design of Beams

Allowable normal stress or normal stress from LRFD should not be exceeded:

$$F_b \text{ or } \phi F_n \geq f_b = \frac{Mc}{I}$$
$$(M_a \leq M_n / \Omega \text{ or } M_u \leq \phi_b M_n)$$

Knowing M and F_y, the minimum plastic section modulus fitting the limit is:

$$Z_{req'd} \geq \frac{M_a}{F_y \Omega} \qquad \left(S_{req'd} \geq \frac{M}{F_b} \right)$$

Determining Maximum Bending Moment

Drawing V and M diagrams will show us the maximum values for design. Remember:

$$V = \Sigma(-w)dx \qquad \frac{dV}{dx} = -w \qquad \frac{dM}{dx} = V$$
$$M = \Sigma(V)dx$$

Determining Maximum Bending Stress

For a prismatic member (constant cross section), the maximum normal stress will occur at the maximum moment.

For a *non-prismatic* member, the stress varies with the cross section AND the moment.

Deflections

If the bending moment changes, M(x) across a beam of constant material and cross section then the curvature will change:

$$\frac{1}{R} = \frac{M(x)}{EI}$$

The slope of the n.a. of a beam, θ, will be tangent to the radius of curvature, R:

$$\theta = slope = \frac{1}{EI}\int M(x)dx$$

The equation for deflection, y, along a beam is:

$$y = \frac{1}{EI}\int \theta dx = \frac{1}{EI}\iint M(x)dx$$

Elastic curve equations can be found in handbooks, textbooks, design manuals, etc...Computer programs can be used as well. Elastic curve equations can be superimposed ONLY if the stresses are in the elastic range.

The deflected shape is roughly the same shape flipped as the bending moment diagram but is constrained by supports and geometry.

Allowable Deflection Limits

All building codes and design codes limit deflection for beam types and damage that could happen based on service condition and severity.

$$y_{\max}(x) = \Delta_{actual} \le \Delta_{allowable} = {}^{L}\!/_{value}$$

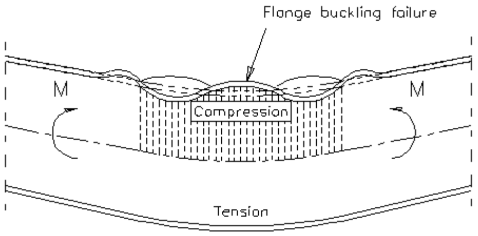
Use	LL only	DL+LL
Roof beams:		
Industrial	L/180	L/120
Commercial		
plaster ceiling	L/240	L/180
no plaster	L/360	L/240
Floor beams:		
Ordinary Usage	L/360	L/240
Roof or floor (damageable elements)		L/480

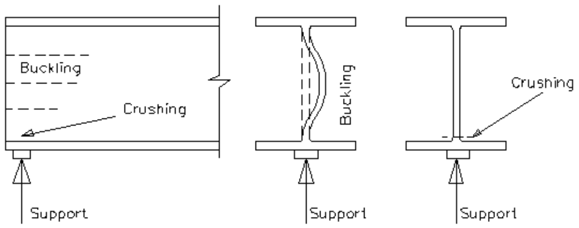
Lateral Buckling

With compression stresses in the top of a beam, a sudden "popping" or buckling can happen even at low stresses. In order to prevent it, we need to brace it along the top, or laterally brace it, or provide a bigger I_y.

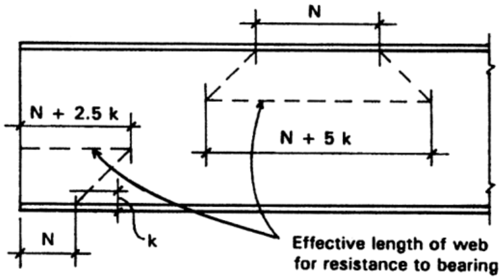
Local Buckling in Steel Wide-flange Beams– Web Crippling or Flange Buckling

Concentrated forces on a steel beam can cause the web to buckle (called **web crippling**). Web stiffeners under the beam loads and bearing plates at the supports reduce that tendency. Web stiffeners also prevent the web from shearing in plate girders.





The maximum support load and interior load can be determined from:



$$P_{n(\text{max-end})} = (2.5k + N)F_{yw}t_w$$

$$P_{n(\text{interior})} = (5k + N)F_{yw}t_w$$

where t_w = thickness of the web
F_{yw} = yield strength of the web
N = bearing length
k = dimension to fillet found in beam section tables

$\phi = 1.00$ (LRFD) $\Omega = 1.50$ (ASD)

Beam Loads & Load Tracing

In order to determine the loads on a beam (or girder, joist, column, frame, foundation...) we can start at the top of a structure and determine the *tributary area* that a load acts over and the beam needs to support. Loads come from material weights, people, and the environment. This area is assumed to be from half the distance to the next beam over to halfway to the next beam.

The reactions must be supported by the next lower structural element *ad infinitum*, to the ground.

LRFD - Bending or Flexure

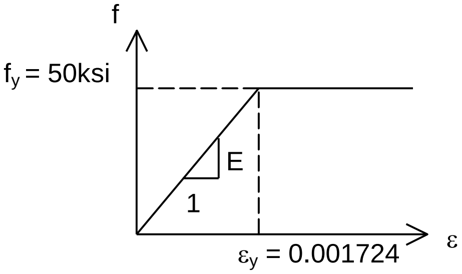
For determining the flexural design strength, $\phi_b M_n$, for resistance to pure bending (no axial load) in most flexural members where the following conditions exist, a single calculation will suffice:

$$\Sigma\gamma_i R_i = M_u \leq \phi_b M_n = 0.9F_y Z$$

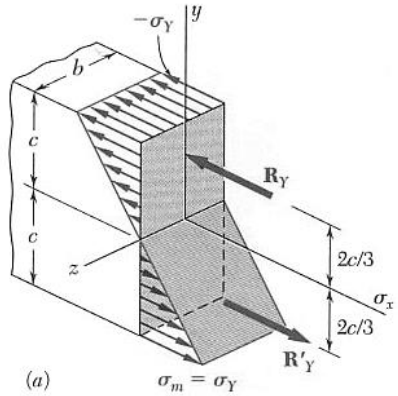
where M_u = maximum moment from factored loads
ϕ_b = resistance factor for bending = 0.9
M_n = nominal moment (ultimate capacity)
F_y = yield strength of the steel
Z = plastic section modulus

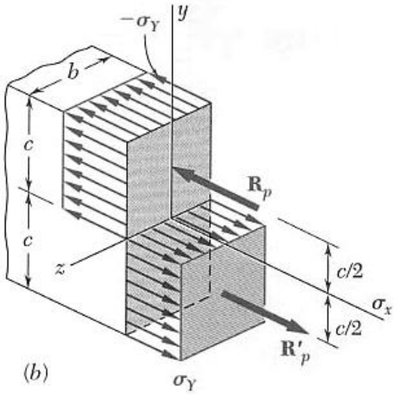
Plastic Section Modulus

Plastic behavior is characterized by a yield point and an increase in strain with no increase in stress.



Internal Moments and Plastic Hinges





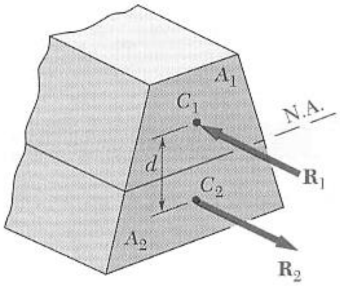
Plastic hinges can develop when all of the material in a cross section sees the yield stress. Because all the material at that section can strain without any additional load, the member segments on either side of the hinge can rotate, possibly causing instability.

For a rectangular section:

Elastic to f_y:
$$M_y = \frac{I}{c} f_y = \frac{bh^2}{6} f_y = \frac{b(2c)^2}{6} f_y = \frac{2bc^2}{3} f_y$$

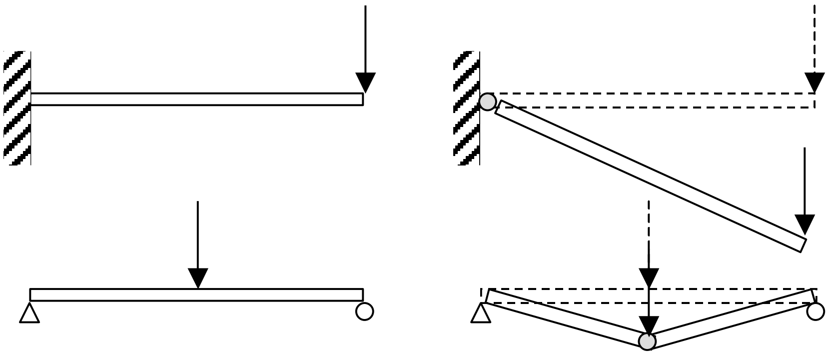
Fully Plastic:
$$M_{ult} \; or \; M_p = bc^2 f_y = {}^{3}\!/_{2} M_y$$

For a non-rectangular section and internal equilibrium at σ_y, the n.a. *will not necessarily be at the centroid.* The n.a. occurs where the $A_{tension} = A_{compression}$. The reactions occur at the centroids of the tension and compression areas.



$A_{tension} = A_{compression}$

Instability from Plastic Hinges



Shape Factor:

The ratio of the plastic moment to the elastic moment at yield:

$$k = {}^{M_p}\!/_{M_y}$$

k = 3/2 for a rectangle
k ≈ 1.1 for an I beam

Plastic Section Modulus

$$Z = \frac{M_p}{f_y} \quad and \quad k = {}^{Z}\!/_{S}$$

Design for Shear

$$V_a \le V_n / \Omega \text{ or } V_u \le \phi_v V_n$$

The nominal shear strength is dependent on the cross section shape. Case 1: With a thick or stiff web, the shear stress is resisted by the web of a wide flange shape (with the exception of a handful of W's). Case 2: When the web is not stiff for doubly symmetric shapes, singly symmetric shapes (like channels) (excluding round high strength steel shapes), inelastic web buckling occurs. When the web is very slender, elastic web buckling occurs, reducing the capacity even more:

Case 1) For $h/t_w \le 2.24\sqrt{\frac{E}{F_y}}$ $V_n = 0.6F_{yw}A_w$ ϕ_v = 1.00 (LRFD) Ω = 1.50 (ASD)

where h equals the clear distance between flanges less the fillet or corner radius for rolled shapes

V_n = nominal shear strength

F_{yw} = yield strength of the steel in the web

$A_w = t_w d$ = area of the web

Case 2) For $h/t_w > 2.24\sqrt{\frac{E}{F_y}}$ $V_n = 0.6F_{yw}A_wC_v$ ϕ_v = 0.9 (LRFD) Ω = 1.67 (ASD)

where C_v is a reduction factor (1.0 or less by equation)

Design for Flexure

$M_a \le M_n / \Omega$ or $M_u \le \phi_b M_n$ ϕ_b = 0.90 (LRFD) Ω = 1.67 (ASD)

The nominal flexural strength M_n is the *lowest* value obtained according to the limit states of

1. yielding, limited at length $L_p = 1.76r_y\sqrt{\frac{E}{F_y}}$, where r_y is the radius of gyration in *y*
2. lateral-torsional buckling limited at length L_r
3. flange local buckling
4. web local buckling

Beam design charts show available moment, M_n/Ω and $\phi_b M_n$, for unbraced length, L_b, of the compression flange in one-foot increments from 1 to 50 ft. for values of the bending coefficient $C_b = 1$. For values of $1<C_b\le2.3$, the required flexural strength M_u can be reduced by dividing it by C_b. ($C_b = 1$ when the bending moment at any point within an unbraced length is larger than that at both ends of the length. C_b of 1 is conservative and permitted to be used in any case. When the free end is unbraced in a cantilever or overhang, $C_b = 1$. The full formula is provided below.)

NOTE: the self weight <u>is not</u> included in determination of M_n/Ω $\phi_b M_n$

Compact Sections

For a laterally braced *compact* section (one for which the plastic moment can be reached before local buckling) only the limit state of yielding is applicable. For unbraced compact beams and non-compact tees and double angles, only the limit states of yielding and lateral-torsional buckling are applicable.

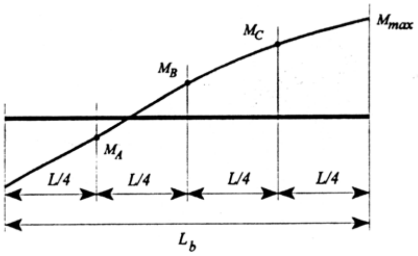
Compact sections meet the following criteria: $\frac{b_f}{2t_f} \le 0.38\sqrt{\frac{E}{F_y}}$ and $\frac{h_c}{t_w} \le 3.76\sqrt{\frac{E}{F_y}}$

where:

b_f = flange width in inches
t_f = flange thickness in inches
E = modulus of elasticity in ksi
F_y = minimum yield stress in ksi
h_c = height of the web in inches
t_w = web thickness in inches

With lateral-torsional buckling the nominal flexural strength is

$$M_n = C_b\left[M_p - (M_p - 0.7F_yS_x)\left(\frac{L_b - L_p}{L_r - L_p}\right)\right] \le M_p$$



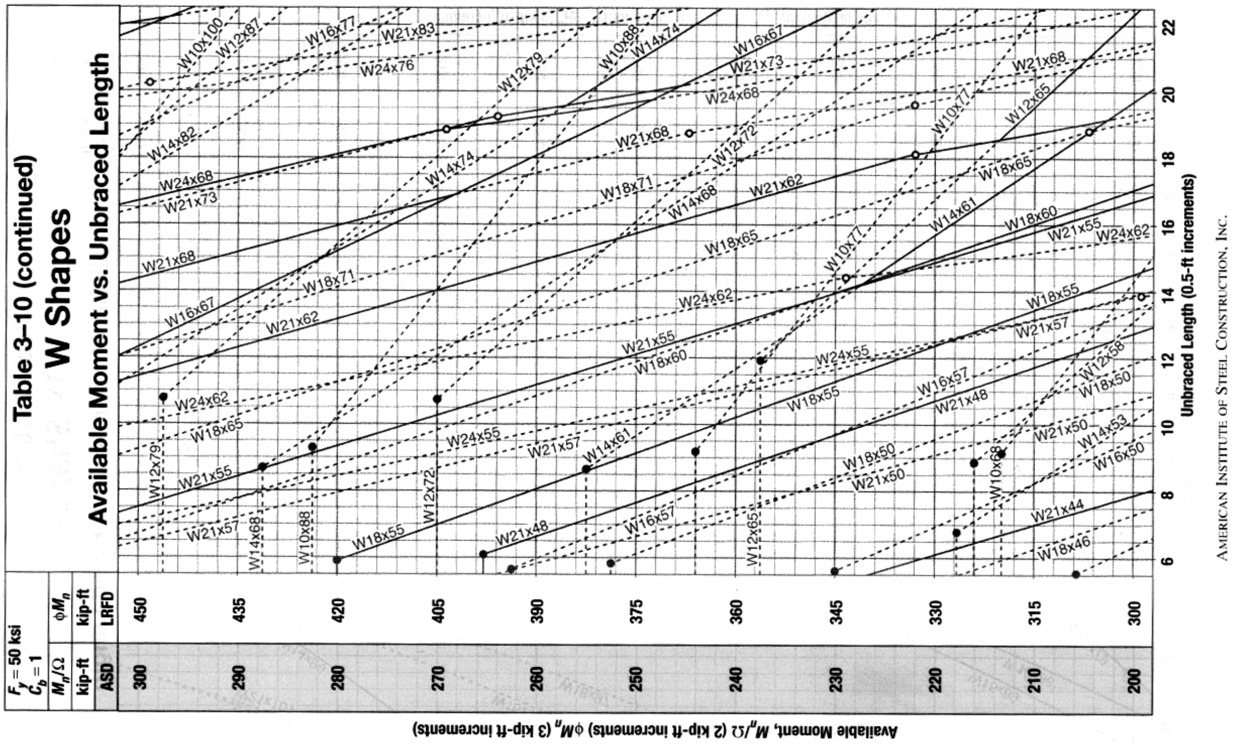
where $M_p = M_n = F_yZ_x$
and C_b is a modification factor for non-uniform moment diagrams where, when both ends of the beam segment are braced:

$$C_b = \frac{12.5M_{max}}{2.5M_{max} + 3M_A + 4M_B + 3M_C}$$

M_{max} = absolute value of the maximum moment in the unbraced beam segment
M_A = absolute value of the moment at the quarter point of the unbraced beam segment
M_B = absolute value of the moment at the center point of the unbraced beam segment
M_C = absolute value of the moment at the three quarter point of the unbraced beam segment length.

Available Flexural Strength Plots

Plots of the available moment for the unbraced length for wide flange sections are useful to find sections to satisfy the design criteria of $M_a \le M_n / \Omega \; or \; M_u \le \phi_b M_n$. The maximum moment that can be applied on a beam (taking self weight into account), M_a or M_u, can be plotted against the unbraced length, L_b. The limiting length, L_p (fully plastic), is indicated by a solid dot (•), while the limiting length, L_r (for lateral torsional buckling), is indicated by an open dot (○). Solid lines indicate the most economical, while dashed lines indicate there is a lighter section that could be used. C_b, which is a lateral torsional buckling modification factor for non-zero moments at the ends, is 1 for simply supported beams (0 moments at the ends). (see *figure)*



Design Procedure

The intent is to find the most light weight member (which is economical) satisfying the section modulus size.

1. Determine the unbraced length to choose the limit state (yielding, lateral torsional buckling or more extreme) and the factor of safety and limiting moments. Determine the material.
2. Draw V & M, finding V_{max} and M_{max}.for unfactored loads (ASD, V_a & M_a) or from factored loads (LRFD, V_u & M_u)
3. Calculate $Z_{req'd}$ when yielding is the limit state. This step is equivalent to determining if $f_b = \frac{M_{max}}{S} \leq F_b$, $Z_{req'd} \geq \frac{M_{max}}{F_b} = \frac{M_{max}}{F_y/\Omega}$ and $Z_{req'd} \geq \frac{M_u}{\phi_b F_y}$ to meet the design criteria that

$$M_a \leq M_n / \Omega \text{ or } M_u \leq \phi_b M_n$$

   If the limit state *is something other than yielding*, determine the nominal moment, M_n, or use plots of available moment to unbraced length, L_b.

4. For steel: use the section charts to find a trial Z *and remember that the beam self weight (the second number in the section designation) will increase $Z_{req'd.}$* The design charts show the lightest section within a grouping of similar Z's.

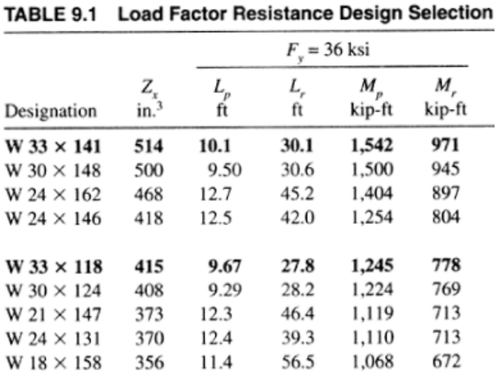


TABLE 9.1 Load Factor Resistance Design Selection

		F_y = 36 ksi			
Designation	Z_x in.^{3}	L_p ft	L_r ft	M_p kip-ft	M_r kip-ft
W 33 × 141	**514**	**10.1**	**30.1**	**1,542**	**971**
W 30 × 148	500	9.50	30.6	1,500	945
W 24 × 162	468	12.7	45.2	1,404	897
W 24 × 146	418	12.5	42.0	1,254	804
W 33 × 118	**415**	**9.67**	**27.8**	**1,245**	**778**
W 30 × 124	408	9.29	28.2	1,224	769
W 21 × 147	373	12.3	46.4	1,119	713
W 24 × 131	370	12.4	39.3	1,110	713
W 18 × 158	356	11.4	56.5	1,068	672

**** *Determine the "updated" V_{max} and M_{max} including the beam self weight, and verify that the updated $Z_{req'd}$ has been met.*******

5. Consider lateral stability.

6. Evaluate horizontal shear using V_{max}. This step is equivalent to determining if $f_v \le F_v$ is satisfied to meet the design criteria that $V_a \le V_n / \Omega$ or $V_u \le \phi_v V_n$

   For I beams: $f_{v-\max} = \frac{3V}{2A} \approx \frac{V}{A_{web}} = \frac{V}{t_w d}$ $\qquad V_n = 0.6F_{yw}A_w \quad or\ V_n = 0.6F_{yw}A_w C_v$

   Others: $f_{v-max} = \frac{VQ}{Ib}$

7. Provide adequate bearing area at supports. This step is equivalent to determining if $f_p = \frac{P}{A} \le F_p$ is satisfied to meet the design criteria that $P_a \le P_n / \Omega$ or $P_u \le \phi P_n$

8. Evaluate shear due to torsion $f_v = \frac{T\rho}{J}\ or\ \frac{T}{c_1 ab^2} \le F_v$ (circular section or rectangular)

9. Evaluate the deflection to determine if $\Delta_{maxLL} \le \Delta_{LL-allowed}$ and/or $\Delta_{maxTotal} \le \Delta_{Total\,allowed}$

**** *note: when $\Delta_{calculated} > \Delta_{limit}$, $I_{req'd}$ can be found with:*
and $Z_{req'd}$ will be satisfied for similar self weight *****

$$I_{req'd} \ge \frac{\Delta_{too\,big}}{\Delta_{limit}} I_{trial}$$

FOR ANY EVALUATION:

Redesign (with a new section) at any point that a stress or serviceability criteria is NOT satisfied and re-evaluate each condition until it is satisfactory.

Load Tables for Uniformly Loaded Joists & Beams

Tables exist for the common loading situation of uniformly distributed load. The tables either provide the safe distributed load based on bending and deflection limits, they give the allowable span for specific live and dead loads including live load deflection limits.
If the load is *not uniform*, an *equivalent uniform load* can be calculated from the maximum moment equation:

$$M_{max} = \frac{w_{equivalent}L^2}{8}$$

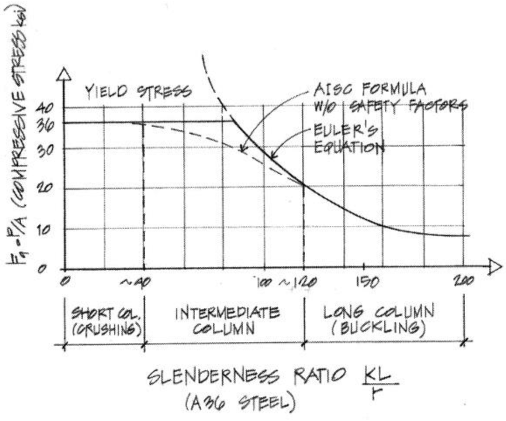
If the deflection limit is less, the design live load to check against allowable must be increased, ex.

$$w_{adjusted} = w_{ll-have}\left(\frac{L/360}{L/400}\right) \begin{matrix} \textit{table limit} \\ \textit{wanted} \end{matrix}$$

Criteria for Design of Columns

If we know the loads, we can select a section that is adequate for strength & buckling.

If we know the length, we can find the limiting load satisfying strength & buckling.



Allowable Stress Design

American Institute of Steel Construction (AISC) Manual of ASD, 9th ed:

Long and slender: [$L_e/r \geq C_c$, preferably < 200]

$$F_{allowable} = \frac{F_{cr}}{F.S.} = \frac{12\pi^2 E}{23\left(Kl/r\right)^2}$$

The yield limit is idealized into a parabolic curve that blends into the Euler's Formula at C_c.

With F_y = 36 ksi, C_c = 126.1

With F_y = 50 ksi, C_c = 107.0

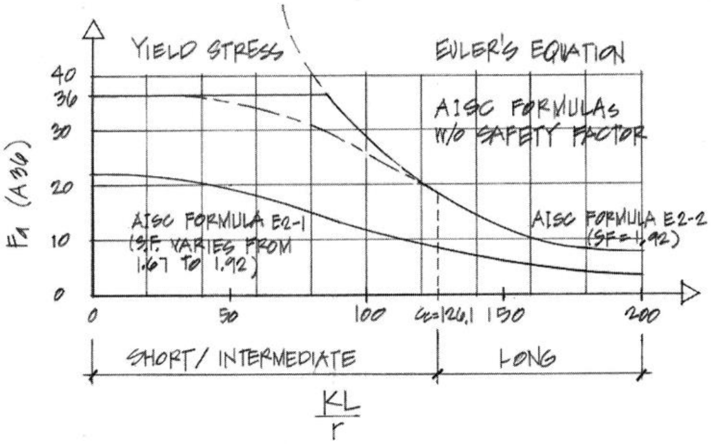
$$C_c = \sqrt{\frac{2\pi^2 E}{F_y}}$$

Short and stubby: [$L_e/r < C_c$]

$$F_a = \left[1 - \frac{\left(Kl/r\right)^2}{2C_c^2}\right]\frac{F_y}{F.S.}$$

with:

$$F.S. = \frac{5}{3} + \frac{3\left(Kl/r\right)}{8C_c} - \frac{\left(Kl/r\right)^3}{8C_c^3}$$



Design for Compression

American Institute of Steel Construction (AISC) Manual 14th ed:

$P_a \leq P_n/\Omega$ or $P_u \leq \phi_c P_n$ where $P_u = \Sigma\gamma_i P_i$

γ is a load factor
P is a load type
ϕ is a resistance factor
P_n is the nominal load capacity (strength)

ϕ = 0.90 (LRFD) Ω = 1.67 (ASD)

For compression $P_n = F_{cr} A_g$

where : A_g is the cross section area and F_{cr} is the flexural buckling stress

The flexural buckling stress, F_{cr}, is determined as follows:

when $\frac{KL}{r} \le 4.71\sqrt{\frac{E}{F_y}}$ or ($F_e \ge 0.44F_y$):

$$F_{cr} = \left[0.658^{\frac{F_y}{F_e}} \right] F_y$$

when $\frac{KL}{r} > 4.71\sqrt{\frac{E}{F_y}}$ or ($F_e < 0.44F_y$):

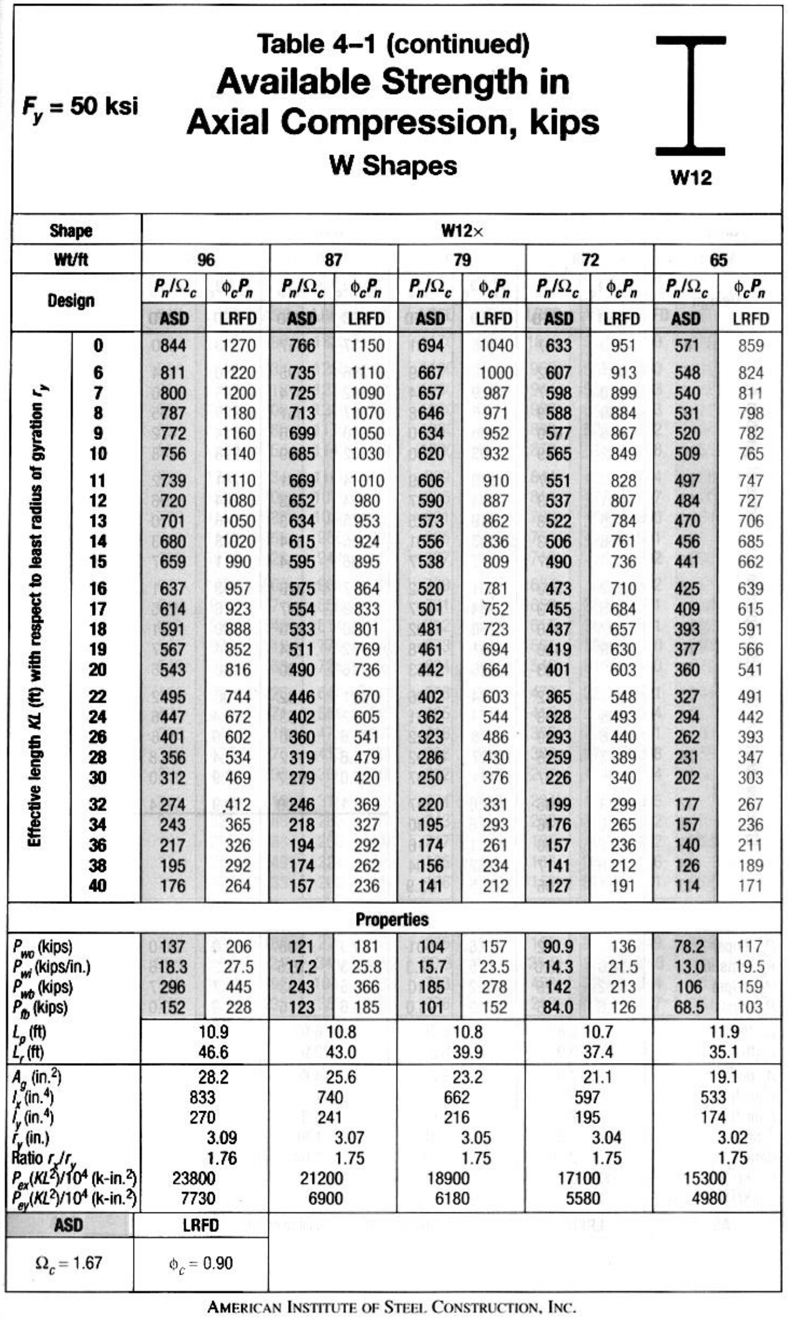
$$F_{cr} = 0.877F_e$$

where F_e is the elastic critical buckling stress: $F_e = \frac{\pi^2 E}{\left(\frac{KL}{r}\right)^2}$

Design Aids

Tables exist for the value of the flexural buckling stress based on slenderness ratio. In addition, tables are provided in the AISC Manual for Available Strength in Axial Compression based on the effective length with respect to least radius of gyration, r_y. If the critical effective length is about the largest radius of gyration, r_x, it can be turned into an effective length about the y axis by dividing by the fraction r_x/r_y.

Sample AISC Table for Available Strength in Axial Compression



F_y = 50 ksi

Table 4–1 (continued)
Available Strength in Axial Compression, kips
W Shapes

W12

Shape		W12×									
Wt/ft		96		87		79		72		65	
Design		P_n/Ω_c	$\phi_c P_n$	P_n/Ω_c	$\phi_c P_n$	P_n/Ω_c	$\phi_c P_n$	P_n/Ω_c	$\phi_c P_n$	P_n/Ω_c	$\phi_c P_n$
		ASD	LRFD	ASD	LRFD	ASD	LRFD	ASD	LRFD	ASD	LRFD
Effective length KL (ft) with respect to least radius of gyration r_y	0	844	1270	766	1150	694	1040	633	951	571	859
	6	811	1220	735	1110	667	1000	607	913	548	824
	7	800	1200	725	1090	657	987	598	899	540	811
	8	787	1180	713	1070	646	971	588	884	531	798
	9	772	1160	699	1050	634	952	577	867	520	782
	10	756	1140	685	1030	620	932	565	849	509	765
	11	739	1110	669	1010	606	910	551	828	497	747
	12	720	1080	652	980	590	887	537	807	484	727
	13	701	1050	634	953	573	862	522	784	470	706
	14	680	1020	615	924	556	836	506	761	456	685
	15	659	990	595	895	538	809	490	736	441	662
	16	637	957	575	864	520	781	473	710	425	639
	17	614	923	554	833	501	752	455	684	409	615
	18	591	888	533	801	481	723	437	657	393	591
	19	567	852	511	769	461	694	419	630	377	566
	20	543	816	490	736	442	664	401	603	360	541
	22	495	744	446	670	402	603	365	548	327	491
	24	447	672	402	605	362	544	328	493	294	442
	26	401	602	360	541	323	486	293	440	262	393
	28	356	534	319	479	286	430	259	389	231	347
	30	312	469	279	420	250	376	226	340	202	303
	32	274	412	246	369	220	331	199	299	177	267
	34	243	365	218	327	195	293	176	265	157	236
	36	217	326	194	292	174	261	157	236	140	211
	38	195	292	174	262	156	234	141	212	126	189
	40	176	264	157	236	141	212	127	191	114	171
Properties											
P_{wo} (kips)		137	206	121	181	104	157	90.9	136	78.2	117
P_{wi} (kips/in.)		18.3	27.5	17.2	25.8	15.7	23.5	14.3	21.5	13.0	19.5
P_{wb} (kips)		296	445	243	366	185	278	142	213	106	159
P_{fb} (kips)		152	228	123	185	101	152	84.0	126	68.5	103
L_p (ft)		10.9		10.8		10.8		10.7		11.9	
L_r (ft)		46.6		43.0		39.9		37.4		35.1	
A_g (in.^{2})		28.2		25.6		23.2		21.1		19.1	
I_x (in.^{4})		833		740		662		597		533	
I_y (in.^{4})		270		241		216		195		174	
r_y (in.)		3.09		3.07		3.05		3.04		3.02	
Ratio r_x/r_y		1.76		1.75		1.75		1.75		1.75	
$P_{ex}(KL^2)/10^4$ (k-in.^{2})		23800		21200		18900		17100		15300	
$P_{ey}(KL^2)/10^4$ (k-in.^{2})		7730		6900		6180		5580		4980	

ASD	LRFD
$\Omega_c = 1.67$	$\phi_c = 0.90$

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Procedure for Analysis

1. Calculate KL/r for each axis (if necessary). The largest will govern the buckling load.
2. Find F_a ***or*** F_{cr} as a function of KL/r from the appropriate equation (above) or table.
3. Compute $P_{allowable} = F_a \cdot A$ ***or*** $P_n = F_{cr} \cdot A_g$

   or alternatively compute $f_c = P/A$ or P_u/A
4. Is the design satisfactory?

   Is $P \leq P_{allowable}$ *(or $P_a \leq P_n/\Omega$)* or $P_u \leq \phi_c P_n$? ⇒ yes, it is; no, it is no good

   or Is $f_c \leq F_a$ *(or $\leq F_{cr}/\Omega$)* or $\phi_c F_{cr}$? ⇒ yes, it is; no, it is no good

Procedure for Design

1. Guess a size by picking a section.
2. Calculate KL/r for each axis (if necessary). The largest will govern the buckling load.
3. Find F_a ***or*** F_{cr} as a function of KL/r from appropriate equation (above) or table.
4. Compute $P_{allowable} = F_a \cdot A$ ***or*** $P_n = F_{cr} \cdot A_g$

   or alternatively compute $f_c = P/A$ or P_u/A
5. Is the design satisfactory?

   Is $P \leq P_{allowable}$ *($P_a \leq P_n/\Omega$)* or $P_u \leq \phi_c P_n$? yes, it is; *no, pick a bigger section and go back to step 2.*

   Is $f_c \leq F_a$ *($\leq F_{cr}/\Omega$)* or $\phi_c F_{cr}$? ⇒ yes, it is; *no, pick a bigger section and go back to step 2.*
6. Check design efficiency by calculating percentage of stress used:

$$\frac{P}{P_{allowable}} \cdot 100\% \left(\frac{P_a}{P_n/\Omega} \cdot 100\% \right) or \ \frac{P_u}{\phi_c P_n} \cdot 100\%$$

   If value is between 90-100%, it is efficient.

   If values is less than 90%, *pick a smaller section and go back to step 2.*

Columns with Bending (Beam-Columns)

In order to *design* an adequate section for allowable stress, we have to start somewhere:

1. Make assumptions about the limiting stress from:
   - buckling
   - axial stress
   - combined stress
2. See if we can find values for r or A or Z.
3. Pick a trial section based on if we think r or A is going to govern the section size.

4. Analyze the stresses and compare to allowable using the allowable stress method or interaction formula for eccentric columns.

5. Did the section pass the stress test?
   - If not, do you *increase* r or A or Z?
   - If so, is the difference really big so that you could *decrease* r or A or Z to make it more efficient (economical)?

6. Change the section choice and go back to step 4. Repeat until the section meets the stress criteria.

Design for Combined Compression and Flexure:

The interaction of compression and bending are included in the form for two conditions based on the size of the required axial force to the available axial strength. This is notated as P_r (either P from ASD or P_u from LRFD) for the axial force being supported, and P_c (either P_n/Ω for ASD or $\phi_c P_n$ for LRFD). The increased bending moment due to the P-Δ effect must be determined and used as the moment to resist.

For $\frac{P_r}{P_c} \geq 0.2$:

$$\frac{P}{P_n/\Omega} + \frac{8}{9}\left(\frac{M_x}{M_{nx}/\Omega} + \frac{M_y}{M_{ny}/\Omega}\right) \leq 1.0 \qquad \frac{P_u}{\phi_c P_n} + \frac{8}{9}\left(\frac{M_{ux}}{\phi_b M_{nx}} + \frac{M_{uy}}{\phi_b M_{ny}}\right) \leq 1.0$$

(ASD) (LRFD)

For $\frac{P_r}{P_c} < 0.2$:

$$\frac{P}{2P_n/\Omega} + \left(\frac{M_x}{M_{nx}/\Omega} + \frac{M_y}{M_{ny}/\Omega}\right) \leq 1.0 \qquad \frac{P_u}{2\phi_c P_n} + \left(\frac{M_{ux}}{\phi_b M_{nx}} + \frac{M_{uy}}{\phi_b M_{ny}}\right) \leq 1.0$$

(ASD) (LRFD)

where:

for compression	ϕ_c = 0.90 (LRFD)	Ω = 1.67 (ASD)
for bending	ϕ_b = 0.90 (LRFD)	Ω = 1.67 (ASD)

For a <u>braced </u>condition, the moment magnification factor B_1 is determined by $B_1 = \frac{C_m}{1-\alpha(P_u/P_{e1})} \geq 1.0$

where C_m is a modification factor accounting for end conditions

When not subject to transverse loading between supports in plane of bending:

= 0.6 – 0.4 (M_1/M_2) where M_1 and M_2 are the end moments and $M_1<M_2$. M_1/M_2 is positive when the member is bent in reverse curvature (same direction), negative when bent in single curvature.

When there is transverse loading between the two ends of a member:

= 0.85, members with restrained (fixed) ends

= 1.00, members with unrestrained ends

$$P_{e1} = \frac{\pi^2 EA}{\left(Kl/r\right)^2}$$

α = 1.00 (LRFD), 1.60 (ASD)

P_{e1} = Euler buckling strength

Criteria for Design of Connections

Connections must be able to transfer any axial force, shear, or moment from member to member or from beam to column.

Connections for steel are typically high strength bolts and electric arc welds. Recommended practice for ease of construction is to specified *shop welding* and *field bolting.*

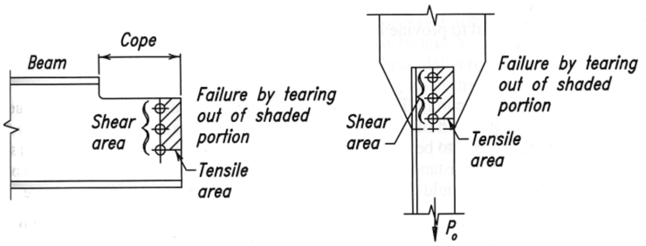


Fig. C-J4.1. Failure for block shear rupture limit state.

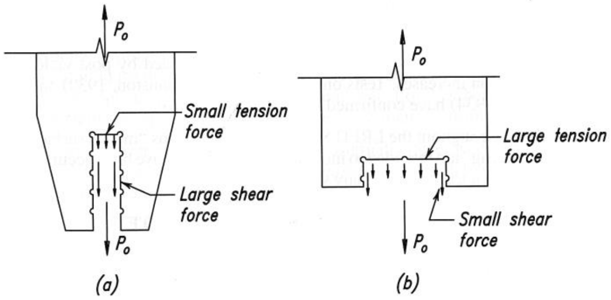
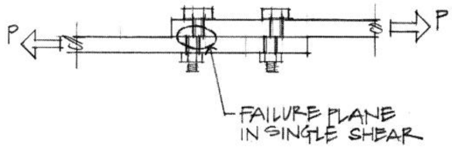


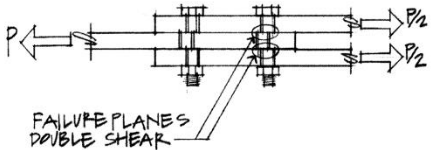
Fig. C-J4.2. Block shear rupture in tension.

Bolted and Welded Connections

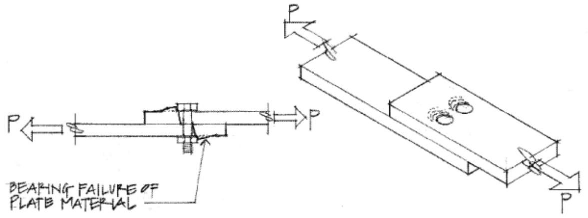
The limit state for connections depends on the loads:

1. tension yielding
2. shear yielding
3. bearing yielding
4. bending yielding due to eccentric loads
5. rupture





Welds must resist shear stress. The design strengths depend on the weld materials.



Bolted Connection Design

Bolt designations signify material and type of connection where

SC: slip critical
N: bearing-type connection with bolt threads *included* in shear plane
X: bearing-type connection with bolt threads *excluded* from shear plane

A307: similar in strength to A36 steel (also known as ordinary, common or unfinished bolts)
A325: high strength bolts (Group A)
A490: high strength bolts (higher than A325) (Group B)

Bearing-type connection: no frictional resistance in the contact surfaces is assumed and slip between members occurs as the load is applied. (Load transfer through bolt only).

Slip-critical connections: bolts are torqued to a high tensile stress in the shank, resulting in a clamping force on the connected parts. (Shear resisted by clamping force). Requires inspections and is useful for structures seeing dynamic or fatigue loading. Class A indicates the *faying* (contact) surfaces are clean mill scale or adequate paint system, while Class B indicates blast cleaning or paint for $\mu = 0.50$.

Bolts rarely fail in **bearing**. The material with the hole will more likely yield first.

For the determination of the net area of a bolt hole the width is taken as *1/16" greater* than the nominal dimension of the hole. Standard diameters for bolt holes are *1/16"* larger than the bolt diameter. (This means the net width will be *1/8"* larger than the bolt.)

Design for Bolts in Bearing, Shear and Tension

Available shear values are given by bolt type, diameter, and loading (Single or Double shear) in AISC manual tables. Available shear value for slip-critical connections are given for limit states of serviceability or strength by bolt type, hole type (standard, short-slotted, long-slotted or oversized), diameter, and loading. Available tension values are given by bolt type and diameter in AISC manual tables.

Available bearing force values are given by bolt diameter, ultimate tensile strength, F_u, of the connected part, and thickness of the connected part in AISC manual tables.

For shear OR tension (same equation) in bolts: $R_a \le R_n / \Omega$ or $R_u \le \phi R_n$

where $R_u = \Sigma \gamma_i R_i$

- single shear (or tension) $R_n = F_n A_b$
- double shear $R_n = F_n 2A_b$

where ϕ = the resistance factor
F_n = the nominal tension or shear strength of the bolt
A_b = the cross section area of the bolt

$\phi = 0.75$ (LRFD) $\Omega = 2.00$ (ASD)

For bearing of plate material at bolt holes: $R_a \le R_n / \Omega$ or $R_u \le \phi R_n$

where $R_u = \Sigma \gamma_i R_i$

- deformation at bolt hole is a concern

$$R_n = 1.2L_c tF_u \le 2.4dtF_u$$

- deformation at bolt hole is not a concern

$$R_n = 1.5L_c tF_u \le 3.0dtF_u$$

- long slotted holes with the slot perpendicular to the load

$$R_n = 1.0L_c tF_u \le 2.0dtF_u$$

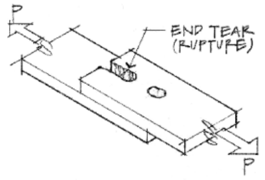


Figure 10.11 End tear-out.

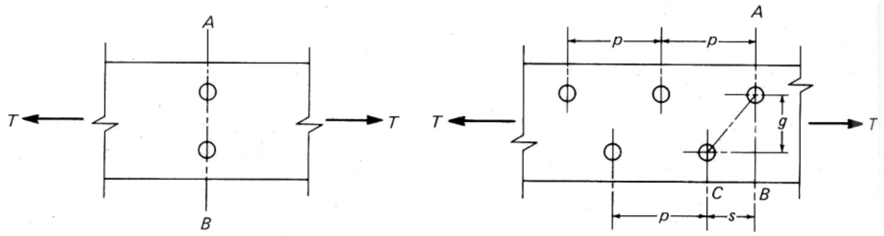
where R_n = the nominal bearing strength
F_u = specified minimum tensile strength
L_c = clear distance between the edges of the hole and the next hole or edge in the direction of the load
d = nominal bolt diameter
t = thickness of connected material

$\phi = 0.75$ (LRFD) $\Omega = 2.00$ (ASD)

The *minimum* edge desistance from the center of the outer most bolt to the edge of a member is generally 1¾ times the bolt diameter for the sheared edge and 1¼ times the bolt diameter for the rolled or gas cut edges.

The *maximum* edge distance should not exceed 12 times the thickness of thinner member or 6 in.

Standard bolt hole spacing is 3 in. with the minimum spacing of 2 ⅔ times the diameter of the bolt, d_b. Common edge distance from the center of last hole to the edge is 1¼ in..



Tension Member Design

In steel tension members, there may be bolt holes that reduce the size of the cross section.

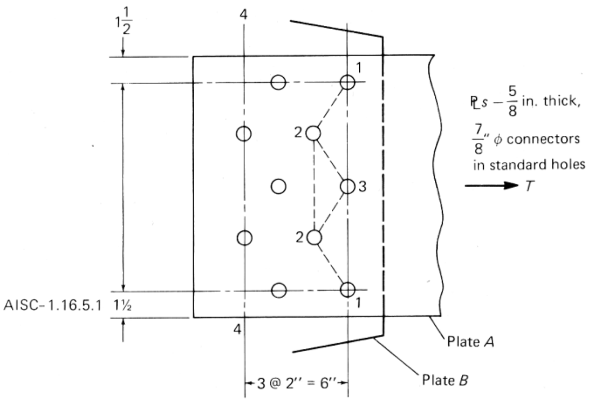
g refers to the row spacing or *gage*
p refers to the bolt spacing or *pitch*
s refers to the longitudinal spacing of two consecutive holes

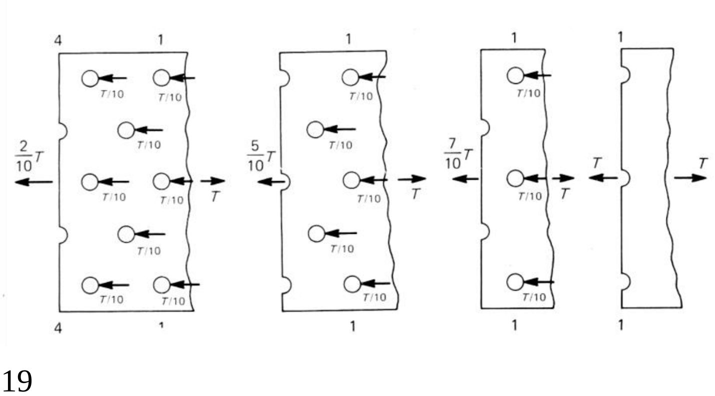
Effective Net Area:

The smallest effective are must be determined by subtracting the bolt hole areas. With staggered holes, the shortest length must be evaluated.

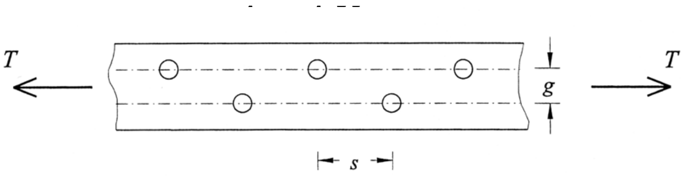
A series of bolts can also transfer a portion of the tensile force, and some of the effective net areas see reduced stress.

The effective net area, A_e, is determined from the net area, A_n, multiplied by a shear lag factor, U, which depends on the element type and connection configuration. If a portion of a connected member is not fully connected (like the leg of an angle), the unconnected part is not subject to the





full stress and the shear lag factor can range fro



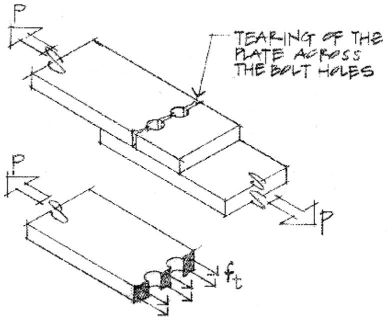
The staggered hole path area is determined by:

$$A_n = A_g - A_{of\ all\ holes} + t\Sigma\frac{s^2}{4g}$$

where *t* is the plate thickness, *s* is each stagger spacing, and *g* is the gage spacing.

For tension elements: $R_a \le R_n/\Omega$ or $R_u \le \phi R_n$

where $R_u = \Sigma\gamma_i R_i$



1. yielding $R_n = F_y A_g$

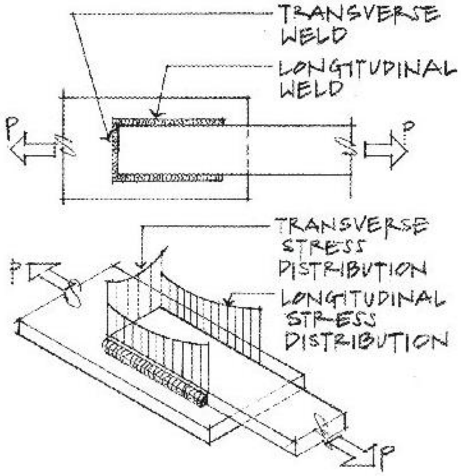
   $\phi = 0.90$ (LRFD) $\Omega = 1.67$ (ASD)

2. rupture $R_n = F_u A_e$

   $\phi = 0.75$ (LRFD) $\Omega = 2.00$ (ASD)

where A_g = the gross area of the member (excluding holes)
A_e = the effective net area (with holes, etc.)
F_y = the yield strength of the steel
F_u = the tensile strength of the steel (ultimate)

Welded Connections

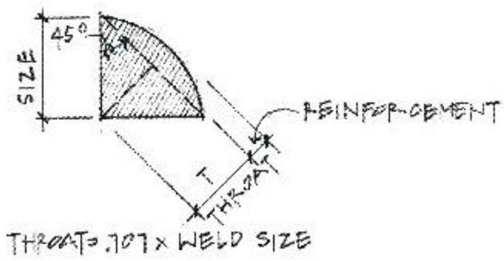


Weld designations include the strength in the name, i.e. E70XX has Fy = 70 ksi. Welds are weakest in shear and are assumed to always fail in the shear mode.

The throat size, T, of a fillet weld is determined trigonometry by: T = 0.707 ×weld size*

* When the submerged arc weld process is used, welds over 3/8" will have a throat thickness of 0.11 in. larger than the formula.

Weld sizes are limited by the size of the parts being put together and are given in AISC manual table J2.4 along with the allowable strength per length of fillet weld, referred to as *S*.



The *maximum* size of a fillet weld:

a) can't be greater than the material thickness if it is ¼" or less
b) is permitted to be 1/16" less than the thickness of the material if it is over ¼"

The *minimum length* of a fillet weld is 4 times the nominal size. If it is not, then the weld size used for design is ¼ the length.

Intermittent fillet welds cannot be less than four times the weld size, not to be less than 1 ½".

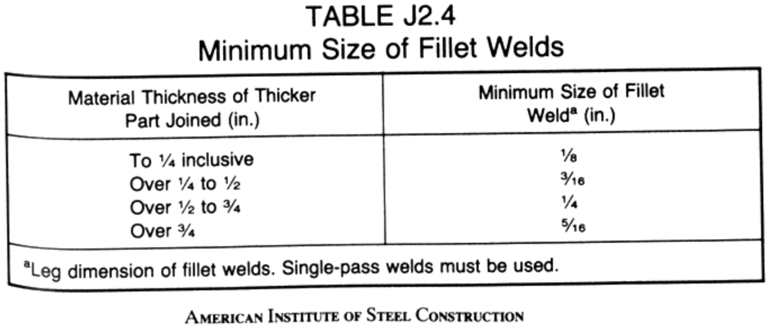


TABLE J2.4
Minimum Size of Fillet Welds

Material Thickness of Thicker Part Joined (in.)	Minimum Size of Fillet Weld[a] (in.)
To ¼ inclusive	⅛
Over ¼ to ½	3/16
Over ½ to ¾	¼
Over ¾	5/16

[a]Leg dimension of fillet welds. Single-pass welds must be used.

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<u>*For fillet welds:*</u> $R_a \leq R_n / \Omega$ or $R_u \leq \phi R_n$

where $R_u = \Sigma \gamma_i R_i$

for the weld metal: $R_n = 0.6 F_{EXX} Tl = Sl$

$\phi = 0.75$ (LRFD) $\Omega = 2.00$ (ASD)

where:

T is throat thickness
l is length of the weld

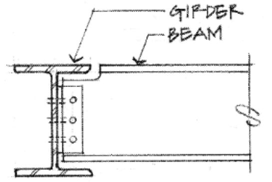
For a connected part, the other limit states for the base metal, such as tension yield, tension rupture, shear yield, or shear rupture **must** be considered.

Available Strength of Fillet Welds
per inch of weld (ϕS)

Weld Size (in.)	E60XX (k/in.)	E70XX (k/in.)
3/16	3.58	4.18
¼	4.77	5.57
5/16	5.97	6.96
3/8	7.16	8.35
7/16	8.35	9.74
½	9.55	11.14
5/8	11.93	13.92
¾	14.32	16.70

(not considering increase in throat with submerged arc weld process)

<u>Framed Beam Connections</u>

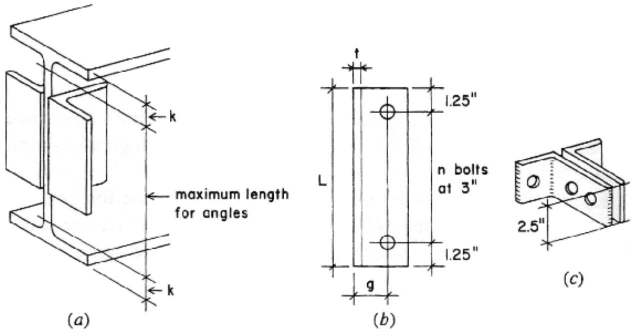


Coping is the term for cutting away part of the flange to connect a beam to another beam using welded or bolted angles.

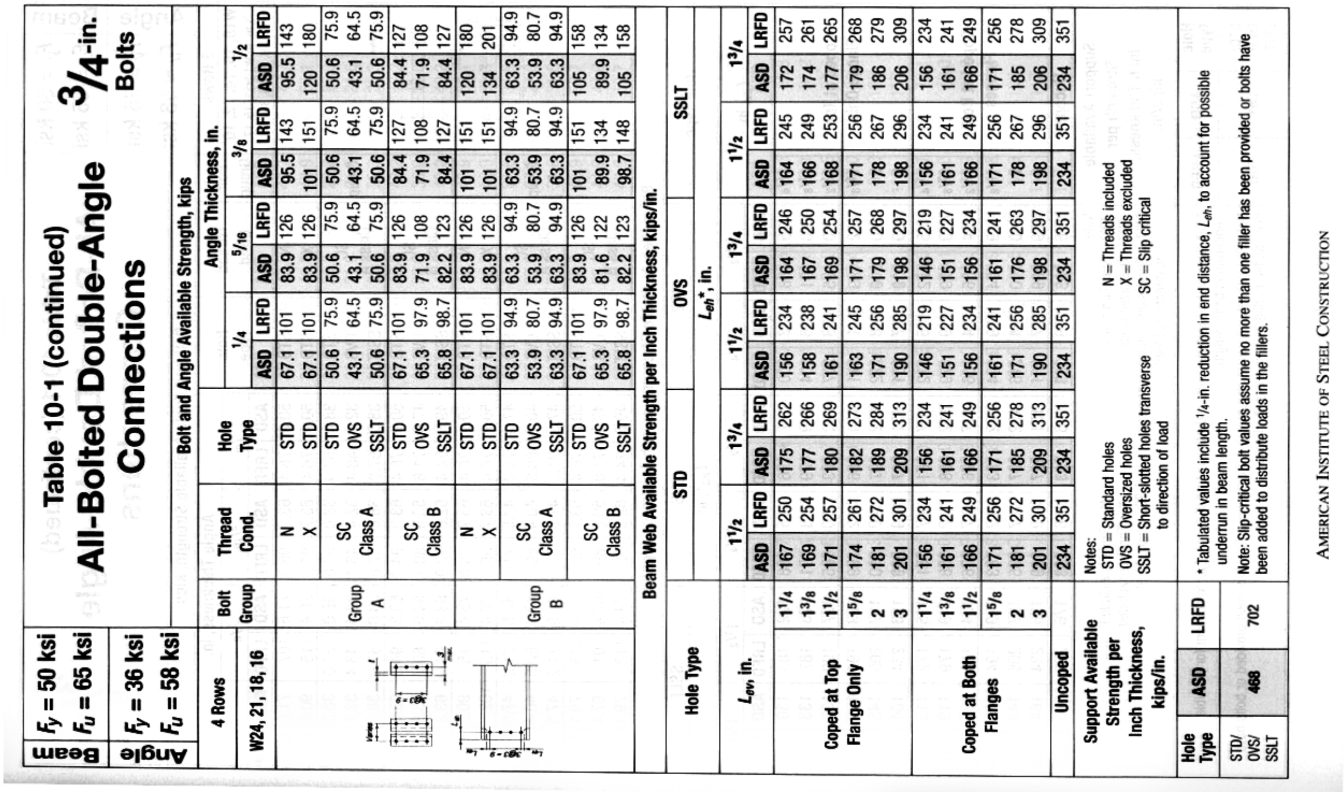
AISC provides tables that give bolt and angle available strength knowing number of bolts, bolt type, bolt diameter, angle leg thickness, hole type and coping, *and* the wide flange beam being connected. For the connections the limit-state of bolt shear, bolts bearing on the angles, shear yielding of the angles, shear rupture of the angles, and block shear rupture of the angles, and bolt bearing on the beam web are considered.

Group A bolts include A325, while Group B includes A490.

There are also tables for bolted/welded double-angle connections and all-welded double-angle connections.



Sample AISC Table for Bolt and Angle Available Strength in All-Bolted Double-Angle Connections



Beam F_y = 50 ksi, F_u = 65 ksi
Angle F_y = 36 ksi, F_u = 58 ksi

Table 10-1 (continued) All-Bolted Double-Angle Connections

3/4-in. Bolts

Bolt and Angle Available Strength, kips

4 Rows	Bolt Group	Thread Cond.	Hole Type	Angle Thickness, in. 1/4 ASD	1/4 LRFD	5/16 ASD	5/16 LRFD	3/8 ASD	3/8 LRFD	1/2 ASD	1/2 LRFD
W24, 21, 18, 16	Group A	N	STD	67.1	101	83.9	126	95.5	143	95.5	143
		X	STD	67.1	101	83.9	126	101	151	120	180
		SC Class A	STD	50.6	75.9	50.6	75.9	50.6	75.9	50.6	75.9
			OVS	43.1	64.5	43.1	64.5	43.1	64.5	43.1	64.5
			SSLT	50.6	75.9	50.6	75.9	50.6	75.9	50.6	75.9
		SC Class B	STD	67.1	101	83.9	126	84.4	127	84.4	127
			OVS	65.3	97.9	71.9	108	71.9	108	71.9	108
			SSLT	65.8	98.7	82.2	123	84.4	127	84.4	127
	Group B	N	STD	67.1	101	83.9	126	101	151	120	180
		X	STD	67.1	101	83.9	126	101	151	134	201
		SC Class A	STD	63.3	94.9	63.3	94.9	63.3	94.9	63.3	94.9
			OVS	53.9	80.7	53.9	80.7	53.9	80.7	53.9	80.7
			SSLT	63.3	94.9	63.3	94.9	63.3	94.9	63.3	94.9
		SC Class B	STD	67.1	101	83.9	126	101	151	105	158
			OVS	65.3	97.9	81.6	122	89.9	134	89.9	134
			SSLT	65.8	98.7	82.2	123	98.7	148	105	158

Beam Web Available Strength per Inch Thickness, kips/in.

Hole Type		STD				OVS				SSLT			
		L_{eh}*, in.											
L_{ev}, in.		1½		1¾		1½		1¾		1½		1¾	
		ASD	LRFD	ASD	LRFD	ASD	LRFD	ASD	LRFD	ASD	LRFD	ASD	LRFD
Coped at Top Flange Only	1¼	167	250	175	262	156	234	164	246	164	245	172	257
	1⅜	169	254	177	266	158	238	167	250	166	249	174	261
	1½	171	257	180	269	161	241	169	254	168	253	177	265
	1⅝	174	261	182	273	163	245	171	257	171	256	179	268
	2	181	272	189	284	171	256	179	268	178	267	186	279
	3	201	301	209	313	190	285	198	297	198	296	206	309
Coped at Both Flanges	1¼	156	234	156	234	146	219	146	219	156	234	156	234
	1⅜	161	241	161	241	151	227	151	227	161	241	161	241
	1½	166	249	166	249	156	234	156	234	166	249	166	249
	1⅝	171	256	171	256	161	241	161	241	171	256	171	256
	2	181	272	185	278	171	256	176	263	178	267	185	278
	3	201	301	209	313	190	285	198	297	198	296	206	309
Uncoped		234	351	234	351	234	351	234	351	234	351	234	351

Support Available Strength per Inch Thickness, kips/in.

Hole Type	ASD	LRFD
STD/ OVS/ SSLT	468	702

Notes:
STD = Standard holes
OVS = Oversized holes
SSLT = Short-slotted holes transverse to direction of load
N = Threads included
X = Threads excluded
SC = Slip critical

* Tabulated values include 1/4-in. reduction in end distance, L_{eh}, to account for possible underrun in beam length.

Note: Slip-critical bolt values assume no more than one filler has been provided or bolts have been added to distribute loads in the fillers.

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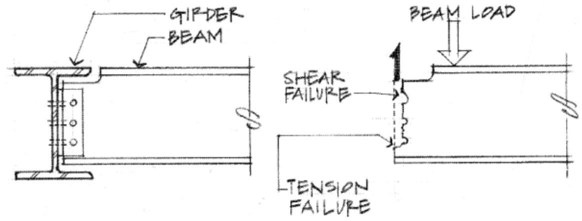
Limiting Strength or Stability States

In addition to resisting shear and tension in bolts and shear in welds, the connected materials may be subjected to shear, bearing, tension, flexure and even prying action. Coping can significantly reduce design strengths and may require web reinforcement. All the following must be considered:

- shear yielding
- shear rupture
- block shear rupture -
  failure of a block at a beam as a result of shear and tension
- tension yielding
- tension rupture
- local web buckling
- lateral torsional buckling



Block Shear Strength (or Rupture): $R_a \leq R_n / \Omega$ or $R_u \leq \phi R_n$

where $R_u = \Sigma \gamma_i R_i$

$$R_n = 0.6F_u A_{nv} + U_{bs} F_u A_{nt} \leq 0.6F_y A_{gv} + U_{bs} F_u A_{nt}$$

ϕ = 0.75 (LRFD) Ω = 2.00 (ASD) where:

A_{nv} is the net area subjected to shear
A_{nt} is the net area subjected to tension
A_{gv} is the gross area subjected to shear
U_{bs} = 1.0 when the tensile stress is uniform (most cases)
= 0.5 when the tensile stress is non-uniform

Gusset Plates

Gusset plates are used for truss member connections where the geometry prevents the members from coming together at the joint "point". Members being joined are typically double angles.

Decking

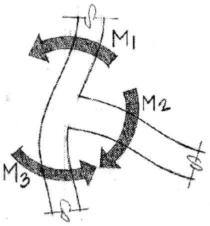
Shaped, thin sheet-steel panels that span several joists or evenly spaced support behave as continuous beams. Design tables consider a "1 unit" wide strip across the supports and determine maximum bending moment and deflections in order to provide allowable loads depending on the depth of the material.

The other structural use of decking is to construct what is called a *diaphragm,* which is a horizontal unit tying the decking to the joists that resists forces parallel to the surface of the diaphragm.

When decking supports a concrete topping or floor, the steel-concrete construction is called *composite.*

Frame Columns

Because joints can rotate in frames, the effective length of the column in a frame is harder to determine. The stiffness (EI/L) of each member in a joint determines how rigid or flexible it is. To find k, the relative stiffness, G or Ψ, must be found for both ends, plotted on the alignment charts, and connected by a line for braced and unbraced fames.

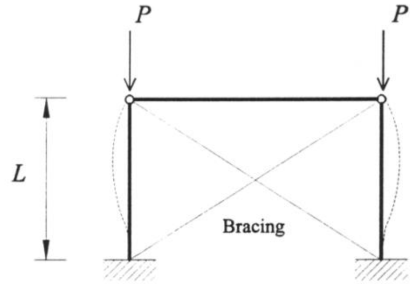


$$G = \Psi = \frac{\Sigma EI/l_c}{\Sigma EI/l_b}$$

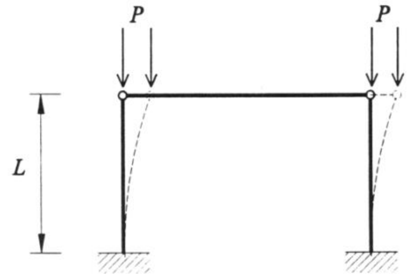
where

E = modulus of elasticity for a member
I = moment of inertia of for a member
l_c = length of the column from center to center
l_b = length of the beam from center to center

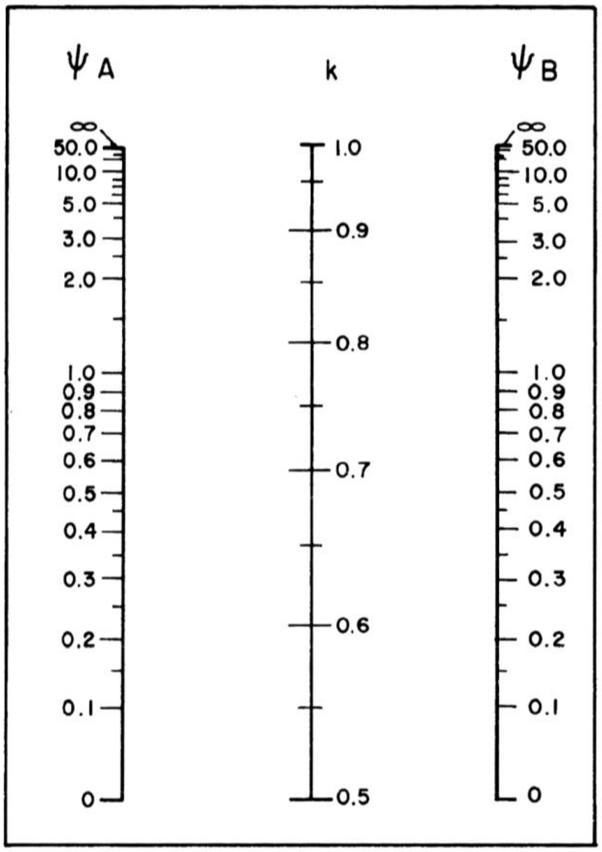
- For pinned connections we typically use a value of 10 for Ψ.
- For fixed connections we typically use a value of 1 for Ψ.



Braced – non-sway frame

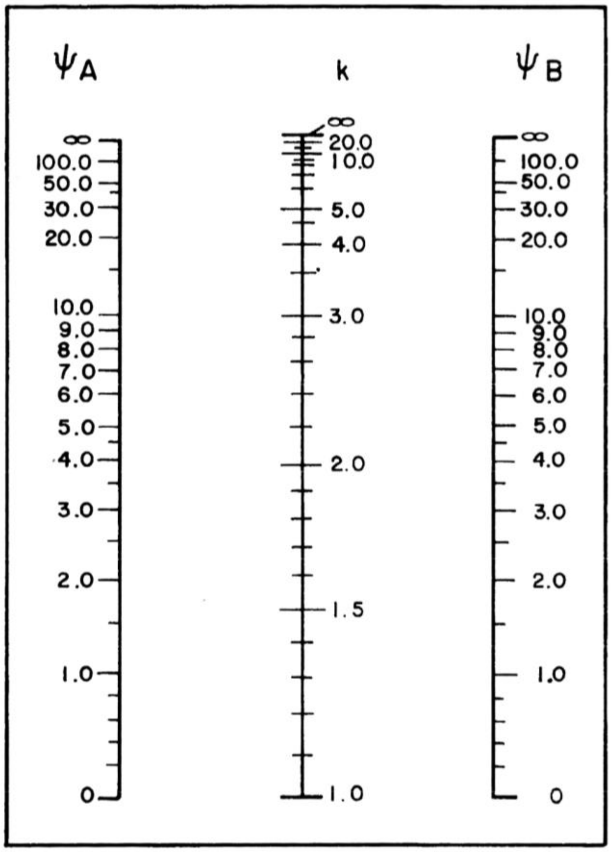


Unbraced – sway frame



(a)

Nonsway Frames



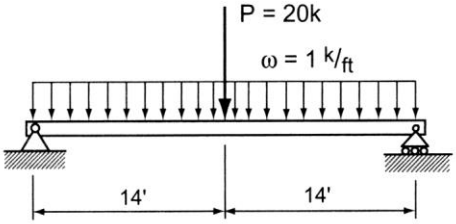
(b)

Sway Frames

Example 1 (pg 330)

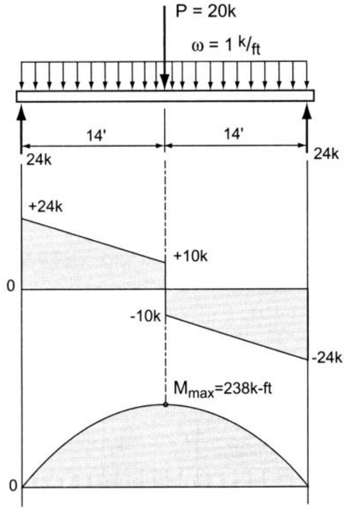
**Hypothetically determine the size of section required when the deflection criteria is NOT met*

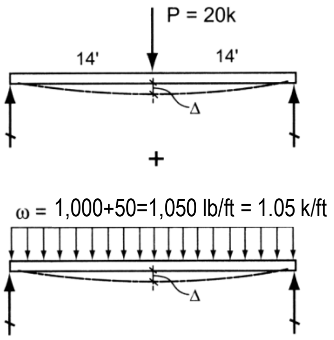
Example Problem 9.16 (Figures 9.76 to 9.78)



A steel beam (A572/50) is loaded as shown. Assuming a deflection requirement of $\Delta_{total} = L/240$ and a depth restriction of 18" nominal, select the most economical section. **(unified ASD)**

$F_b = 30$ ksi; $F_v = 20$ ksi; $E = 30 \times 10^3$ ksi $F_y = 50$ ksi

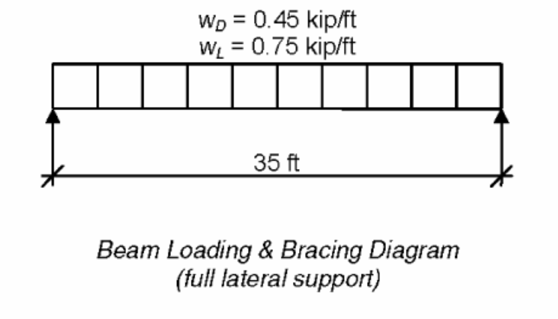




Example 2

Given:

Select an ASTM A992 W-shape beam with a simple span of 35 feet. Limit the member to a maximum nominal depth of 18 in. Limit the live load deflection to *L*/360. The nominal loads are a uniform dead load of 0.45 kip/ft and a uniform live load of 0.75 kip/ft. Assume the beam is continuously braced. Use ASD of the Unified Design method.



Beam Loading & Bracing Diagram
(full lateral support)

Solution:

Material Properties:

ASTM A992 $F_y = 50$ ksi $F_u = 65$ ksi

1. The unbraced length is 0 because it says it is fully braced.
2. Find the maximum shear and moment from unfactored loads: w_a = 0.450 k/ft + 0.750 k/ft = 1.20 k/ft

   V_a = 1.20 k/ft(35 ft)/2 = 21 k

   M_a = 1.20 k/ft(35 ft)^2/8 = 184 k-ft

   If $M_a \leq M_n/\Omega$, the maxmimum moment for design is $M_a\Omega$: M_{max} = 184 k-ft
3. Find $Z_{req'd}$:

   $Z_{req'd} \geq M_{max}/F_b = M_{max}(\Omega)/F_y$ = 184 k-ft(1.67)(12 in/ft)/50 ksi = 73.75 in^3 (F_y is the limit stress when fully braced)
4. Choose a trial section, and also limit the depth to 18 in as instructed:

   W18 x 40 has a plastic section modulus of 78.4 in^3 and is the most light weight (as indicated by the bold text) in Table 9.1

   Include the self weight in the maximum values: $w^*_{a\text{-}adjusted}$ = 1.20 k/ft + 0.04 k/ft

   $V^*_{a\text{-}adjusted}$ = 1.24 k/ft(35 ft)/2 = 21.7 k

   $M^*_{a\text{-}adjusted}$ = 1.24 k/ft(35 ft)^3/8 = 189.9 k

   $Z_{req'd} \geq$ 189.9 k-ft(1.67)(12 in/ft)/50 ksi = 76.11 in^3 And the Z we have (78.4) is larger than the Z we need (76.11), so OK.
6. Evaluate shear (is $V_a \leq V_n/\Omega$): $A_w = dt_w$ so look up section properties for W18 x 40: d = 17.90 in and t_w = 0.315 in

   $V_n/\Omega = 0.6F_{yw}A_w/\Omega$ = 0.6(50 ksi)(17.90 in)(0.315 in)/1.5 = 112.8 k which is much larger than 21.7 k, so OK.
9. Evaluate the deflection with respect to the limit stated of L/360 for the live load. (If we knew the **total** load limit we would check that as well). The moment of inertia for the W18 x 40 is needed. I_x = 612 in^4

   $\Delta_{\text{live load limit}}$ = 35 ft(12 in/ft)/360 = 1.17 in

   $\Delta = 5wL^4/384EI$ = 5(0.75 k/ft)(35 ft)^4(12 in/ft)^3/384(29 x 10^3 ksi)(612 in^4) = 1.42 in! This is TOO BIG (not less than the limit.

   Find the moment of inertia needed:

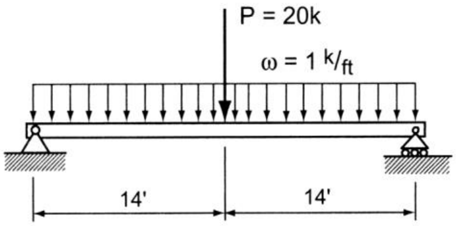
   $I_{req'd} \geq \Delta_{\text{too big}}(I_{trial})/\Delta_{limit}$ = 1.42 in(612 in^4)/(1.17 in) = 742.8 in^4

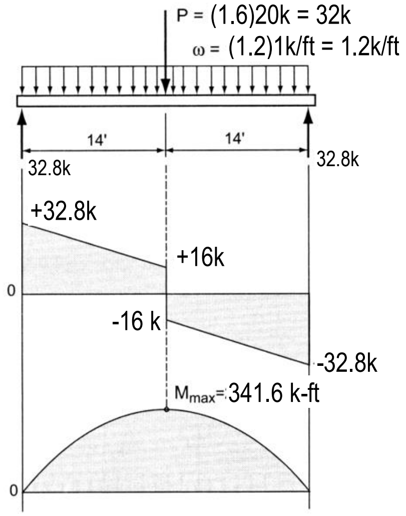
From Table 9.1, a W16 x 45 is larger (by Z), but not the most light weight (efficient), as is W10 x 68, W14 x 53, W18 x 46, (W21 x 44 is too deep) and W18 x 50 is bolded (efficient). (Now look up I's). (In order: I_x = 586, 394, 541, 712 and 800 in^4)

Choose a W18 x 50

Example 3

For the same beam and loading of Example 1, select the most economical beam using Load and Resistance Factor Design (LRFD) with the 18" depth restriction. Assume the distributed load is dead load, and the point load is live load. F_y = 50 ksi and E = 30x10^3 ksi





1. To find V$_{u\text{-max}}$ and M$_{u\text{-max}}$, factor the loads, construct a *new* load diagram, shear diagram and bending moment diagram.

2. To satisfy $M_u \le \phi_b M_n$, we find $M_n = \frac{M_u}{\phi_b} = \frac{341.6^{k-ft}}{0.9} = 379.6^{k-ft}$ and

   solve for Z needed: $Z = \frac{M_n}{F_y} = \frac{379.6^{k-ft}(12\, ^{in}\!/_{ft})}{50ksi} = 91.1in^3$

   Choose a *trial* section from the Listing of W Shapes in Descending Order of Z by selecting the **bold** section at the top of the grouping satisfying our Z and depth requirement – W18 x 50 is the *lightest* with Z = 101 in^3. (W22 x 44 is the lightest without the depth requirement.) Include the additional self weight (dead load) and find the maximum shear and bending moment:

$$V^*_{u-adjusted} = 32.8k + \frac{1.2(50\, ^{lb}\!/_{ft})28\,ft}{2(1000\, ^{lb}\!/_{k})} = 33.64k$$

$$M^*_{u-adjusted} = 341.6^{k-ft} + \frac{1.2(50\, ^{lb}\!/_{ft})(28\,ft)^2}{8(1000\, ^{lb}\!/_{k})} = 347.5^{k-ft}$$

$$Z^*_{req'd} \ge \frac{M_u}{\phi_b F_y} = \frac{347.5^{k-ft}(12\, ^{in}\!/_{ft})}{0.9(50ksi)} = 92.7in^3$$, so Z (have) of 101 in^3 is greater than the Z (needed).

3. Check the shear capacity to satisfy $V_u \le \phi_v V_n$: $A_{web} = dt_w$ and d=17.99 in., t$_w$ = 0.355 in. for the W18x50

   $\phi_v V_n = \phi_v 0.6 F_{yw} A_w = 1.0(0.6)50ksi(17.99in)0.355in = 191.6k$ So 33.64k ≤ 191.6 k OK

4. Calculate the deflection from the ***unfactored*** loads, including the self-weight now because it is known, and satisfy the deflection criteria of $\Delta_{LL} \le \Delta_{LL\text{-limit}}$ and $\Delta_{total} \le \Delta_{total\text{-limit}}$. (This is identical to what is done in Example 1.) I$_x$ =800 in^3 for the W18x50

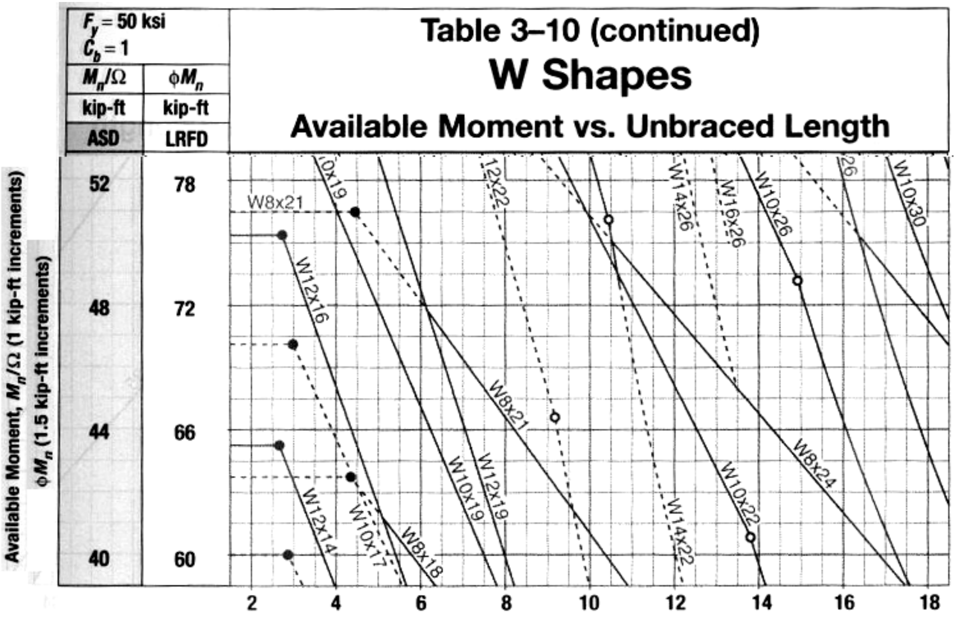
   $\Delta_{total\text{-limit}}$ = L/240 = 1.4 in., say Δ_{LL} = L/360 = 0.93 in

$$\Delta_{total} = \frac{PL^3}{48EI} + \frac{5wL^4}{384EI} = \frac{20k(28\,ft)^3(12\, ^{in}\!/_{ft})^3}{48(30x10^3\,ksi)800in^4} + \frac{5(1.050\, ^{k}\!/_{ft})(28\,ft)^4(12\, ^{in}\!/_{ft})^3}{384(30x10^3\,ksi)800in^4} = 0.658 + 0.605 = 1.26in$$

So 1.26 in. ≤ 1.4 in., and 0.658 in. ≤ 0.93 in. OK ∴ **FINAL SELECTION IS W18x50**

Example 4

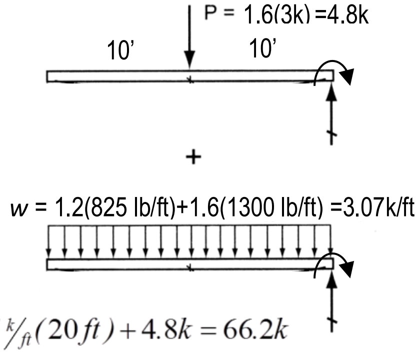
A steel beam with a 20 ft span is designed to be simply supported at the ends on columns and to carry a floor system made with open-web steel joists at 4 ft on center. The joists span 28 feet and frame into the beam from *one side only* and have a self weight of 8.5 lb/ft. Use A992 (grade 50) steel and select the most economical wide-flange section for the beam with LRFD design. Floor loads are 50 psf LL and 14.5 psf DL.



Example 5

Select a A992 W shape flexural member (F_y = 50 ksi, F_u = 65 ksi) for a beam with distributed loads of 825 lb/ft (dead) and 1300 lb/ft (live) and a live point load at midspan of 3 k using the Available Moment tables. The beam is simply supported, 20 feet long, and braced at the ends and midpoint only (L_b = 10 ft.) The beam is a roof beam for an institution without plaster ceilings. (LRFD)

SOLUTION:



To use the Available Moment tables, the maximum moment required is plotted against the unbraced length. The first solid line with capacity or unbraced length *above* what is needed is the most economical.

DESIGN LOADS (load factors applied on figure):

$$M_u = \frac{wl^2}{2} + Pb = \frac{3.07\,{}^{k}\!/_{ft}(20ft)^2}{2} + 4.8k(10ft) = 662^{k-ft} \quad V_u = wl + P = 3.07\,{}^{k}\!/_{ft}(20ft) + 4.8k = 66.2k$$

Plotting 662 k-ft vs. 10 ft lands just on the capacity of the W21x83, but it is dashed (and not the most economical) AND we need to consider the contribution of self weight to the total moment. Choose a *trial* section of W24 x 76. Include the new dead load:

$$M^*_{u-adjusted} = 662^{k-ft} + \frac{1.2(76\,{}^{lb}\!/_{ft})(20ft)^2}{2(1000\,{}^{lb}\!/_{k})} 680.2^{k-ft} \qquad V^*_{u-adjusted} = 66.2k + 1.2(0.076\,{}^{k}\!/_{ft})(20ft) = 68.0k$$

Replot 680.2 k-ft vs. 10ft, which lands *above* the capacity of the W21x83. We can't look up because the chart ends, but we can look for that capacity with a longer unbraced length. This leads us to a **W24 x 84** as the most economical. (With the additional self weight of 84 - 76 lb/ft = 8 lb/ft, the increase in the *factored* moment is only 1.92 k-ft; therefore, it is still OK.)

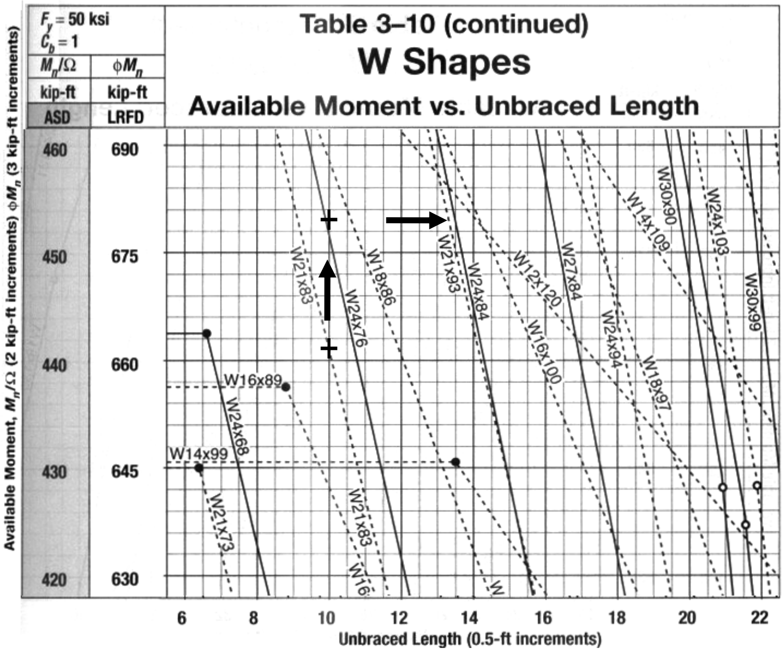
Evaluate the shear capacity:

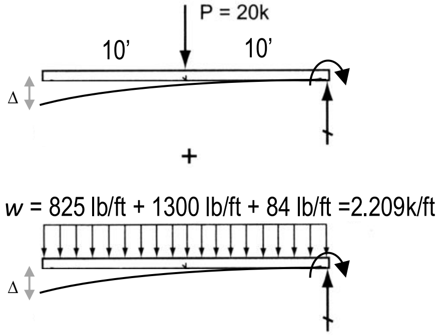
$$\phi_v V_n = \phi_v 0.6 F_{yw} A_w = 1.0(0.6)50ksi(24.10in)0.47in = 338.4k$$ so yes, 68 k ≤ 338.4k OK

Evaluate the deflection with respect to the limits of L/240 for live (*unfactored)* load and L/180 for total (*unfactored)* load:

L/240 = 1 in. and L/180 = 1.33 in.

$$\Delta_{total} = \frac{Pb^2(3l-b)}{6EI} + \frac{wL^4}{24EI} = \frac{3k(10ft)^2(3\cdot 20-10ft)(12\,{}^{in}\!/_{ft})^3}{6(30x10^3ksi)2370in^4} + \frac{(2.209^{k/ft})(20ft)^4(12\,{}^{in}\!/_{ft})^3}{24(30x10^3ksi)2370in^4} = 0.06 + 0.36 = 0.42in$$





So, $\Delta_{LL} \le \Delta_{LL-limit}$ and $\Delta_{total} \le \Delta_{total-limit}$:

0.06 in. ≤ 1 in. and 0.42 in. ≤ 1.33 in.

(This section is so big to accommodate the large bending moment at the cantilever support that it deflects very little.)

∴ FINAL SELECTION IS W24x84

Example 6

Select the most economical joist for the 40 ft grid structure with floors and a flat roof. The roof loads are 10 lb/ft^2 dead load and 20 lb/ft^2 live load. The floor loads are 30 lb/ft^2 dead load 100 lb/ft^2 live load. (Live load deflection limit for the roof is L/240, while the floor is L/360). Use the (LRFD) K and LH series charts provided.

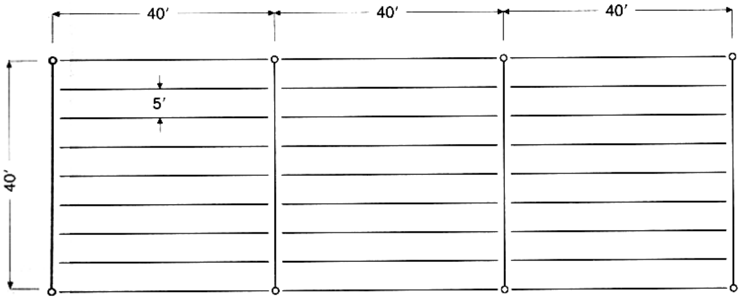
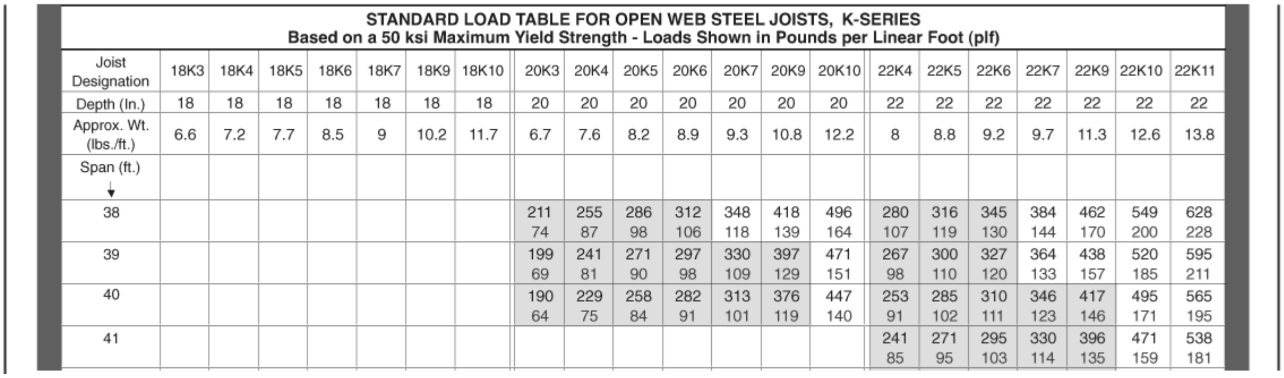


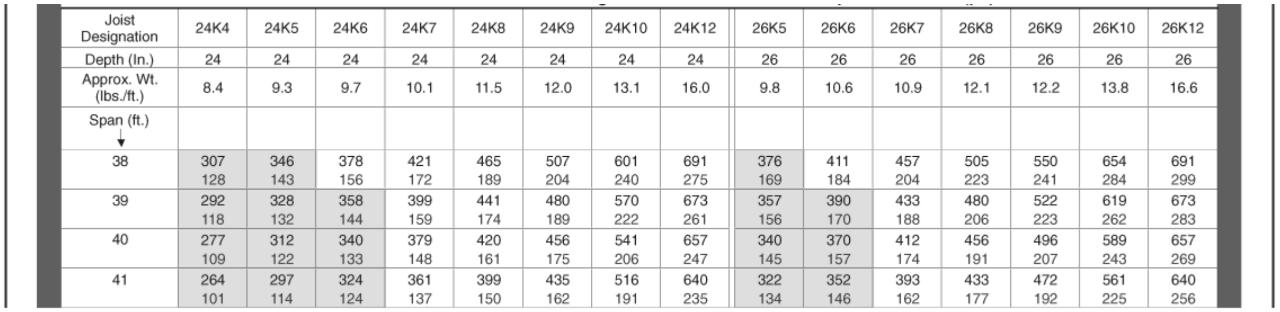
Figure 7.218 Framing plan for joists, girders, and columns on 40 ft × 40 ft grid.

(Top values are maximum total factored load in lb/ft, while the lower (lighter) values are maximum (unfactored) live load for a deflection of L/360)

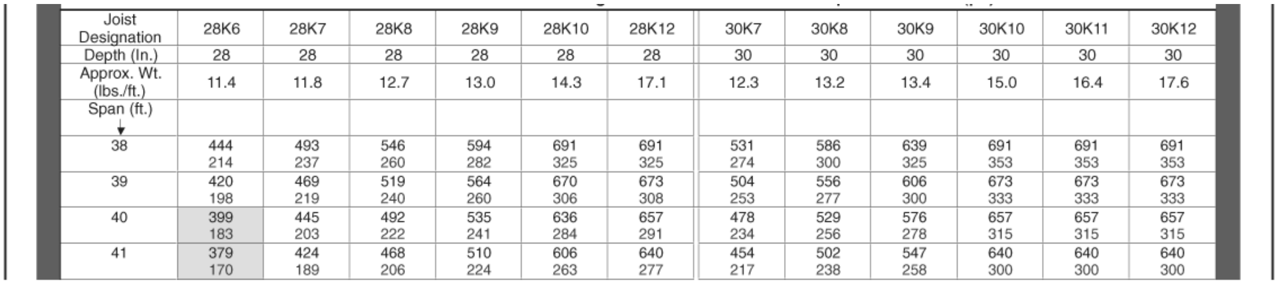


STANDARD LOAD TABLE FOR OPEN WEB STEEL JOISTS, K-SERIES
Based on a 50 ksi Maximum Yield Strength - Loads Shown in Pounds per Linear Foot (plf)

Joist Designation	18K3	18K4	18K5	18K6	18K7	18K9	18K10	20K3	20K4	20K5	20K6	20K7	20K9	20K10	22K4	22K5	22K6	22K7	22K9	22K10	22K11
Depth (In.)	18	18	18	18	18	18	18	20	20	20	20	20	20	20	22	22	22	22	22	22	22
Approx. Wt. (lbs./ft.)	6.6	7.2	7.7	8.5	9	10.2	11.7	6.7	7.6	8.2	8.9	9.3	10.8	12.2	8	8.8	9.2	9.7	11.3	12.6	13.8
Span (ft.) ↓																					
38								211 74	255 87	286 98	312 106	348 118	418 139	496 164	280 107	316 119	345 130	384 144	462 170	549 200	628 228
39								199 69	241 81	271 90	297 98	330 109	397 129	471 151	267 98	300 110	327 120	364 133	438 157	520 185	595 211
40								190 64	229 75	258 84	282 91	313 101	376 119	447 140	253 91	285 102	310 111	346 123	417 146	495 171	565 195
41															241 85	271 95	295 103	330 114	396 135	471 159	538 181



Joist Designation	24K4	24K5	24K6	24K7	24K8	24K9	24K10	24K12	26K5	26K6	26K7	26K8	26K9	26K10	26K12
Depth (In.)	24	24	24	24	24	24	24	24	26	26	26	26	26	26	26
Approx. Wt. (lbs./ft.)	8.4	9.3	9.7	10.1	11.5	12.0	13.1	16.0	9.8	10.6	10.9	12.1	12.2	13.8	16.6
Span (ft.) ↓															
38	307 128	346 143	378 156	421 172	465 189	507 204	601 240	691 275	376 169	411 184	457 204	505 223	550 241	654 284	691 299
39	292 118	328 132	358 144	399 159	441 174	480 189	570 222	673 261	357 156	390 170	433 188	480 206	522 223	619 262	673 283
40	277 109	312 122	340 133	379 148	420 161	456 175	541 206	657 247	340 145	370 157	412 174	456 191	496 207	589 243	657 269
41	264 101	297 114	324 124	361 137	399 150	435 162	516 191	640 235	322 134	352 146	393 162	433 177	472 192	561 225	640 256

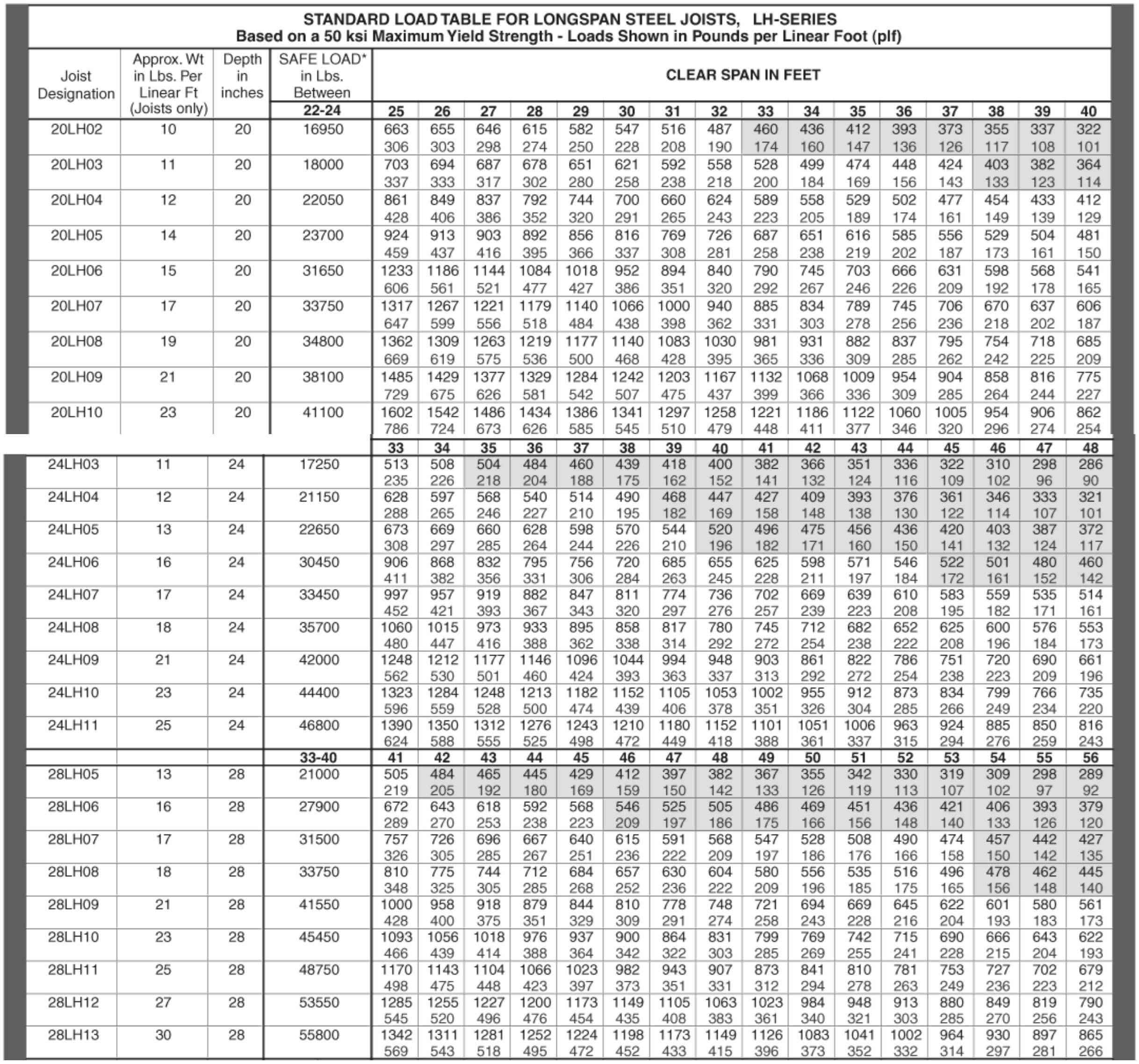


Joist Designation	28K6	28K7	28K8	28K9	28K10	28K12	30K7	30K8	30K9	30K10	30K11	30K12
Depth (In.)	28	28	28	28	28	28	30	30	30	30	30	30
Approx. Wt. (lbs./ft.)	11.4	11.8	12.7	13.0	14.3	17.1	12.3	13.2	13.4	15.0	16.4	17.6
Span (ft.) ↓												
38	444 214	493 237	546 260	594 282	691 325	691 325	531 274	586 300	639 325	691 353	691 353	691 353
39	420 198	469 219	519 240	564 260	670 306	673 308	504 253	556 277	606 300	673 333	673 333	673 333
40	399 183	445 203	492 222	535 241	636 284	657 291	478 234	529 256	576 278	657 315	657 315	657 315
41	379 170	424 189	468 206	510 224	606 263	640 277	454 217	502 238	547 258	640 300	640 300	640 300

Shaded areas indicate the bridging requirements.

Example 6 (continued)

(Top values are maximum total factored load in lb/ft, while the lower (lighter) values
are maximum (unfactored) live load for a deflection of L/360)



STANDARD LOAD TABLE FOR LONGSPAN STEEL JOISTS, LH-SERIES
Based on a 50 ksi Maximum Yield Strength - Loads Shown in Pounds per Linear Foot (plf)

Joist Designation	Approx. Wt in Lbs. Per Linear Ft (Joists only)	Depth in inches	SAFE LOAD* in Lbs. Between	CLEAR SPAN IN FEET															
			22-24	**25**	**26**	**27**	**28**	**29**	**30**	**31**	**32**	**33**	**34**	**35**	**36**	**37**	**38**	**39**	**40**
20LH02	10	20	16950	663	655	646	615	582	547	516	487	460	436	412	393	373	355	337	322
				306	303	298	274	250	228	208	190	174	160	147	136	126	117	108	101
20LH03	11	20	18000	703	694	687	678	651	621	592	558	528	499	474	448	424	403	382	364
				337	333	317	302	280	258	238	218	200	184	169	156	143	133	123	114
20LH04	12	20	22050	861	849	837	792	744	700	660	624	589	558	529	502	477	454	433	412
				428	406	386	352	320	291	265	243	223	205	189	174	161	149	139	129
20LH05	14	20	23700	924	913	903	892	856	816	769	726	687	651	616	585	556	529	504	481
				459	437	416	395	366	337	308	281	258	238	219	202	187	173	161	150
20LH06	15	20	31650	1233	1186	1144	1084	1018	952	894	840	790	745	703	666	631	598	568	541
				606	561	521	477	427	386	351	320	292	267	246	226	209	192	178	165
20LH07	17	20	33750	1317	1267	1221	1179	1140	1066	1000	940	885	834	789	745	706	670	637	606
				647	599	556	518	484	438	398	362	331	303	278	256	236	218	202	187
20LH08	19	20	34800	1362	1309	1263	1219	1177	1140	1083	1030	981	931	882	837	795	754	718	685
				669	619	575	536	500	468	428	395	365	336	309	285	262	242	225	209
20LH09	21	20	38100	1485	1429	1377	1329	1284	1242	1203	1167	1132	1068	1009	954	904	858	816	775
				729	675	626	581	542	507	475	437	399	366	336	309	285	264	244	227
20LH10	23	20	41100	1602	1542	1486	1434	1386	1341	1297	1258	1221	1186	1122	1060	1005	954	906	862
				786	724	673	626	585	545	510	479	448	411	377	346	320	296	274	254
				33	**34**	**35**	**36**	**37**	**38**	**39**	**40**	**41**	**42**	**43**	**44**	**45**	**46**	**47**	**48**
24LH03	11	24	17250	513	508	504	484	460	439	418	400	382	366	351	336	322	310	298	286
				235	226	218	204	188	175	162	152	141	132	124	116	109	102	96	90
24LH04	12	24	21150	628	597	568	540	514	490	468	447	427	409	393	376	361	346	333	321
				288	265	246	227	210	195	182	169	158	148	138	130	122	114	107	101
24LH05	13	24	22650	673	669	660	628	598	570	544	520	496	475	456	436	420	403	387	372
				308	297	285	264	244	226	210	196	182	171	160	150	141	132	124	117
24LH06	16	24	30450	906	868	832	795	756	720	685	655	625	598	571	546	522	501	480	460
				411	382	356	331	306	284	263	245	228	211	197	184	172	161	152	142
24LH07	17	24	33450	997	957	919	882	847	811	774	736	702	669	639	610	583	559	535	514
				452	421	393	367	343	320	297	276	257	239	223	208	195	182	171	161
24LH08	18	24	35700	1060	1015	973	933	895	858	817	780	745	712	682	652	625	600	576	553
				480	447	416	388	362	338	314	292	272	254	238	222	208	196	184	173
24LH09	21	24	42000	1248	1212	1177	1146	1096	1044	994	948	903	861	822	786	751	720	690	661
				562	530	501	460	424	393	363	337	313	292	272	254	238	223	209	196
24LH10	23	24	44400	1323	1284	1248	1213	1182	1152	1105	1053	1002	955	912	873	834	799	766	735
				596	559	528	500	474	439	406	378	351	326	304	285	266	249	234	220
24LH11	25	24	46800	1390	1350	1312	1276	1243	1210	1180	1152	1101	1051	1006	963	924	885	850	816
				624	588	555	525	498	472	449	418	388	361	337	315	294	276	259	243
			33-40	**41**	**42**	**43**	**44**	**45**	**46**	**47**	**48**	**49**	**50**	**51**	**52**	**53**	**54**	**55**	**56**
28LH05	13	28	21000	505	484	465	445	429	412	397	382	367	355	342	330	319	309	298	289
				219	205	192	180	169	159	150	142	133	126	119	113	107	102	97	92
28LH06	16	28	27900	672	643	618	592	568	546	525	505	486	469	451	436	421	406	393	379
				289	270	253	238	223	209	197	186	175	166	156	148	140	133	126	120
28LH07	17	28	31500	757	726	696	667	640	615	591	568	547	528	508	490	474	457	442	427
				326	305	285	267	251	236	222	209	197	186	176	166	158	150	142	135
28LH08	18	28	33750	810	775	744	712	684	657	630	604	580	556	535	516	496	478	462	445
				348	325	305	285	268	252	236	222	209	196	185	175	165	156	148	140
28LH09	21	28	41550	1000	958	918	879	844	810	778	748	721	694	669	645	622	601	580	561
				428	400	375	351	329	309	291	274	258	243	228	216	204	193	183	173
28LH10	23	28	45450	1093	1056	1018	976	937	900	864	831	799	769	742	715	690	666	643	622
				466	439	414	388	364	342	322	303	285	269	255	241	228	215	204	193
28LH11	25	28	48750	1170	1143	1104	1066	1023	982	943	907	873	841	810	781	753	727	702	679
				498	475	448	423	397	373	351	331	312	294	278	263	249	236	223	212
28LH12	27	28	53550	1285	1255	1227	1200	1173	1149	1105	1063	1023	984	948	913	880	849	819	790
				545	520	496	476	454	435	408	383	361	340	321	303	285	270	256	243
28LH13	30	28	55800	1342	1311	1281	1252	1224	1198	1173	1149	1126	1083	1041	1002	964	930	897	865
				569	543	518	495	472	452	433	415	396	373	352	332	314	297	281	266

Shaded areas indicate the bridging requirements.

Example 7 (LRFD)

EXAMPLE 5.1 Open-Web Steel Joist Design

A fully exposed roof system for a commercial building, spanning 35 ft, located in Muncie, Indiana, in an urban environment.

IBC specifies a **20 psf snow live load** for Muncie, Indiana, home of Ball State University. Table 1.3 indicates the snow exposure factor: $C_e = 0.9$. Table 1.4 indicates the snow thermal factor: $C_t = 1.0$. Table 1.7 indicates an occupancy importance factor (for Category II): $I_S = 1.0$. Fig. 1.2 indicates the ground snow load: $p_g = 20$ psf

$$P_S = 0.7(0.9)1.0(1.0)20 \text{ psf} = 13.9 \text{ psf}$$

A typical roof construction might consist of:

Membrane roofing	1.0 psf
4 in. average tapered rigid insulation	6.0 psf
Steel deck (2–4 ft span)	1.0 psf
Estimated joist weight:	
35 ft span would be a minimum 18 in. joist	
An average 18 in. joist weight = 9.0 plf	
Spaced @ 4 ft-0 in. o.c. 9.0 plf/4 ft	2.3 psf
Ceiling suspension system	1.0 psf
$^1/_2$ in. gypsum ceiling	2.0 psf

Mechanical system estimates should also be included; the heavy sprinkler/drain piping running parallel to a joist or pair of joists is especially critical.

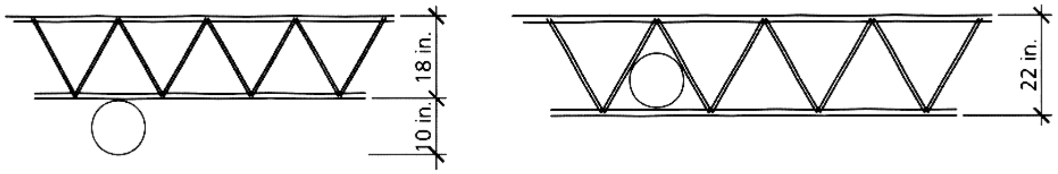
Miscellaneous ductwork/electrical	1.0 psf
Total dead load	14.3 psf × 4 ft o.c. = 57.2 plf
Total live load	13.9 psf X 4 ft o.c. = 55.6 plf

Total factored live snow load + dead load = 1.2(55.6) + 1.6 (57.2) = 158.2 plf

Use joist load tables to select the best section:

At 35 ft, 18K3 joists carry 237 plf TFL and 84 plf LL
LL: deflection controls and the weight is 6.4 plf.

At least on the surface, this is the best choice, but depending upon the need to integrate mechanical systems into the joist space, a 20K3 at 6.5 plf or even a 22K4 at 7.3 plf which is both deeper and heavier than the previous selection may be best:



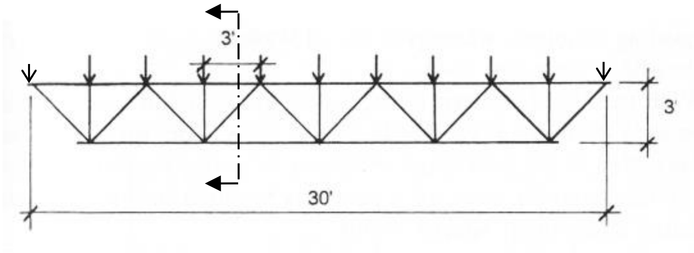
LRFD

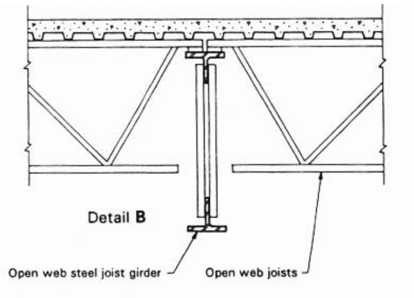
STANDARD LOAD TABLE FOR OPEN WEB STEEL JOISTS, K-SERIES
Based On A 50 ksi Maximum Yield Strength - Loads Shown In Pounds Per Linear Foot (plf)

Joist Designation	18K3	18K4	18K5	18K6	18K7	18K9	18K10	20K3	20K4	20K5	20K6	20K7	20K9	20K10	22K4	22K5	22K6	22K7	22K9	22K10	22K11
Depth (In.)	18	18	18	18	18	18	18	20	20	20	20	20	20	20	22	22	22	22	22	22	22
Approx. Wt. (lbs./ft.)	6.4	7.2	7.7	8.4	8.9	10.1	11.6	6.5	7.2	7.7	8.4	8.9	10.1	11.6	7.3	7.7	8.5	9.0	10.2	11.7	11.9
Span (ft.) ↓																					
34	237 84	285 98	321 110	349 120	390 132	468 156	555 184	264 105	318 122	358 137	391 149	435 165	523 195	621 229	352 149	397 167	432 182	481 202	579 239	687 280	774 314
35	223 77	268 90	303 101	330 110	367 121	441 143	523 168	249 96	300 112	339 126	369 137	411 151	493 179	585 210	331 137	373 153	408 167	454 185	546 219	648 257	741 292

Example 8

A floor with multiple bays is to be supported by open-web steel joists spaced at 3 ft. on center and spanning 30 ft. having a dead load of 70 lb/ft^2 and a live load of 100 lb/ft^2. The joists are supported on joist girders spanning 30 ft. with 3 ft.-long panel points (shown). Determine the member forces at the location shown in a horizontal chord and the maximum force in a web member for an interior girder. Use factored loads. *Assume a self weight for the open-web joists of 12 lb/ft, and the self weight for the joist girder of 35 lb/ft.*





Example 9

A floor is to be supported by trusses spaced at 5 ft. on center and spanning 60 ft. having a dead load of 53 lb/ft^2 and a live load of 100 lb/ft^2. With 3 ft.-long panel points, the depth is assumed to be 3 ft with a span-to-depth ratio of 20. With 6 ft.-long panel points, the depth is assumed to be 6 ft with a span-to-depth ratio of 10. Determine the maximum force in a horizontal chord and the maximum force in a web member. Use factored loads. *Assume a self weight of 40 lb/ft.*

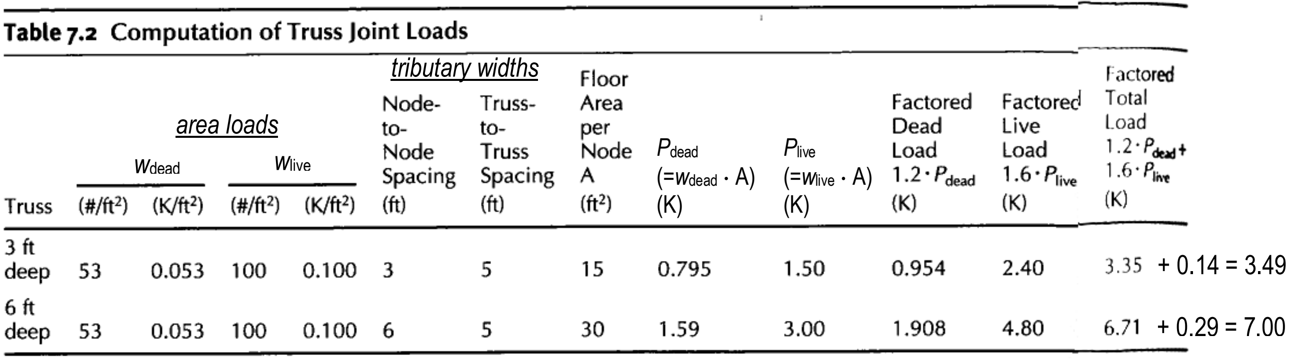


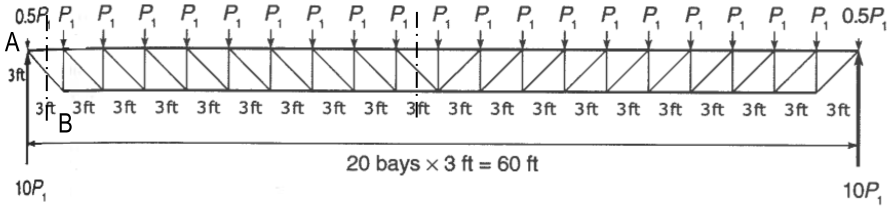
Table 7.2 Computation of Truss Joint Loads

	area loads				tributary widths							
	w_{dead}		w_{live}									
Truss	(#/ft²)	(K/ft²)	(#/ft²)	(K/ft²)	Node-to-Node Spacing (ft)	Truss-to-Truss Spacing (ft)	Floor Area per Node A (ft²)	P_{dead} (=$w_{dead}\cdot$ A) (K)	P_{live} (=$w_{live}\cdot$ A) (K)	Factored Dead Load $1.2\cdot P_{dead}$ (K)	Factored Live Load $1.6\cdot P_{live}$ (K)	Factored Total Load $1.2\cdot P_{dead}+1.6\cdot P_{live}$ (K)
3 ft deep	53	0.053	100	0.100	3	5	15	0.795	1.50	0.954	2.40	3.35 + 0.14 = 3.49
6 ft deep	53	0.053	100	0.100	6	5	30	1.59	3.00	1.908	4.80	6.71 + 0.29 = 7.00

self weight 0.04 k/ft (distributed) 3 $1.2P_{dead} = 1.2w_{dead}\cdot$ *tributary width* = 0.14 K

6 $1.2P_{dead} = 1.2w_{dead}\cdot$ *tributary width* = 0.29 K

NOTE – end panels only have *half* the tributary width of interior panels

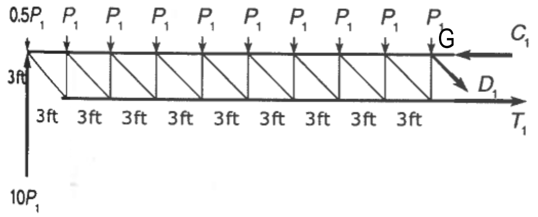


***FBD 1** for 3 ft deep truss*

FBD 3: Maximum web force will be in the end diagonal (just like maximum shear in a beam)

$\Sigma F_y = 10P_1 - 0.5P_1 - F_{AB}\cdot\sin 45° = 0$

$F_{AB} = 9.5P_1/\sin 45° = 9.5(3.49\ k)/0.707 = \underline{46.9\ k}$



***FBD 2** of cut just to the left of midspan*

***FBD 3** of cut just to right of left support*

FBD 2: Maximum chord force (top or bottom) will be at midspan

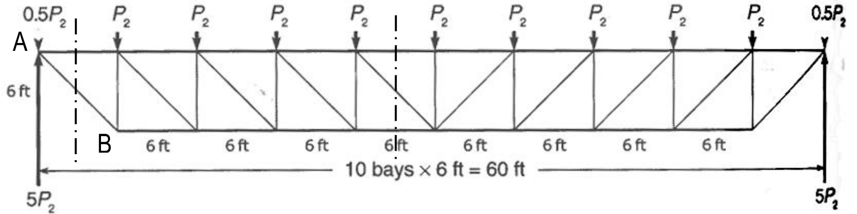
$$\Sigma M_G = -9.5P_1(27^{ft}) + P_1(24^{ft}) + P_1(21^{ft}) + P_1(18^{ft}) + P_1(15^{ft}) + P_1(12^{ft}) + P_1(9^{ft}) + P_1(6^{ft}) + P_1(3^{ft}) + T_1(3^{ft}) = 0$$

$$T_1 = P_1(148.5^{ft})/3^{ft} = (3.49\ k)(49.5) = 172.8\ k$$

$\Sigma F_y = 10P_1 - 9.5P_1 - D_1\cdot\sin 45° = 0$

$D_1 = 0.5(3.49\ k)/0.707 = 2.5\ k$ *(minimum near midspan)*

$\Sigma F_x = -C_1 + T_1 + D_1\cdot\cos 45° = 0$ $\underline{C_1 = 174.5\ k}$

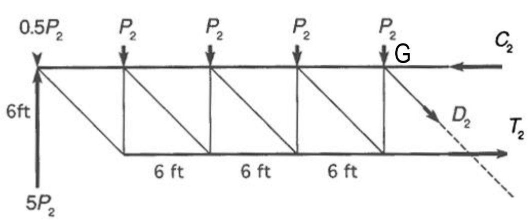


***FBD 4** for 6 ft deep truss*

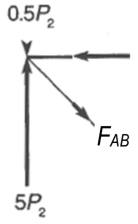
FBD 6: Maximum web force will be in the end diagonal

$\Sigma F_y = 5P_2 - 0.5P_2 - F_{AB}\cdot\sin 45° = 0$

$F_{AB} = 4.5P_2/\sin 45° = 4.5(7\ k)/0.707 = \underline{44.5\ k}$



***FBD 5** of cut just to the left of midspan*



***FBD 6** of cut just to right of left support*

FBD 5: Maximum chord (top or bottom) force will be at midspan

$\Sigma M_G = -4.5P_2(24^{ft}) + P_2(18^{ft}) + P_2(12^{ft}) + P_2(6^{ft}) + T_2(6^{ft}) = 0$

$T_2 = P_2(72^{ft})/6^{ft} = (7\ k)(12) = 84\ k$

$\Sigma F_y = 5P_2 - 4.5P_1 - D_s\cdot\sin 45° = 0$

$D_2 = 0.5(7\ k)/0.707 = 4.9\ k$ *(minimum near midspan)*

$\Sigma F_x = -C_2 + T_2 + D_2\cdot\cos 45° = 0$ $\underline{C_2 = 87.5\ k}$

Example 10 (pg 367) + LRFD

Example Problem 10.10 (Figure 10.41)

A 24-ft.-tall, A572 grade 50, steel column (W14×82) with an $F_y = 50$ ksi has pins at both ends. Its weak axis is braced at midheight, but the column is free to buckle the full 24 ft. in the strong direction. Determine the safe load capacity for this column. using ASD and LRFD.

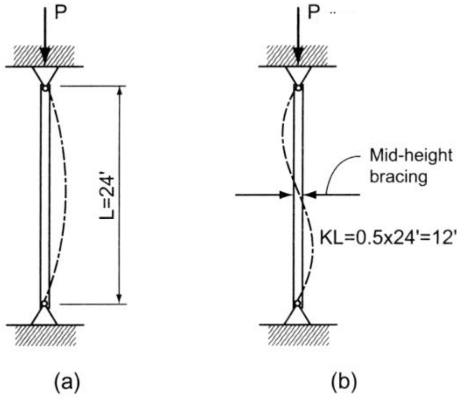


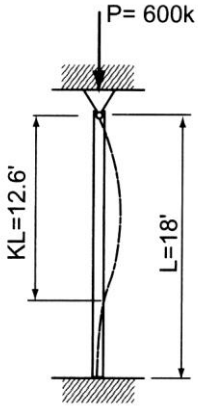
Figure 10.41 (a) Strong axis buckling. (b) Weak axis buckling.

Example 11 (pg 371) + chart method

Example Problem 10.14: Design of Steel Columns (Figure 10.48)

Select the most economical W12 × column 18' in height to support an axial load of 600 kips using A572 grade 50 steel. Assume that the column is hinged at the top but fixed at the base. Use LRFD assuming that the load is a dead load (factor of 1.4)

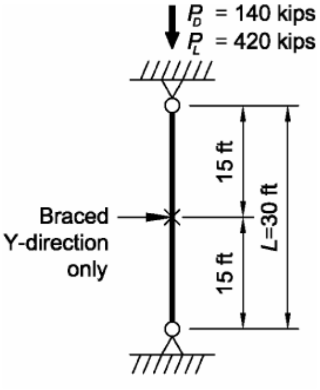
ALSO: Select the W12 column using the Available Strength charts.



Example 12

Given:

Redesign the column from Example E.1a assuming the column is laterally braced about the y-y axis and torsionally braced at the midpoint. Use both ASD and LRFD. F_y = 50 ksi. (Not using Available Strength charts)



Solution:

ASD:

1. P_a = 140 k + 420 k = 560 k
2. The effective length in the weak (y-y) axis is 15 ft, while the effective length in the strong (x-x) axis is 30 ft. (K = 1, KL = 1×30 ft). To find kL/r_x and kL/r_y we can assume or choose values from the wide flange charts. r_y's range from 1 to 3 in., while r_x's range from 3 to 14 inches. Let's try r_y = 2 in and r_x = 9 in. (something in the W21 range, say.)

   $kL/r_y \cong$ 15 ft(12 in/ft)/2 in. = 90 $\Leftarrow$ GOVERNS (is larger)

   $kL/r_x \cong$ 30 ft(12 in/ft)/9 in. = 40
3. Find a section with sufficient area (which then will give us "real" values for r_x and r_y):

   If $P_a \leq P_n/\Omega$, and $P_n = F_{cr} A$, we can find $A \geq P_a\Omega/F_{cr}$ with Ω = 1.67

   The tables provided have $\underline{\phi F_{cr}}$, so we can get F_{cr} by dividing by ϕ = 0.9

   ϕF_{cr} for 90 is 24.9 ksi, F_{cr} = 24.9 ksi/0.9 = 27.67 ksi so $A \geq$ 560 k(1.67)/27.67 ksi = 33.8 in^2
4. Choose a trial section, and find the effective lengths and associated available strength, F_{cr} :

   Looking from the smallest sections, the W14's are the first with a big enough area:

   Try a W14 x 120 (A = 35.3 in^2) with r_y = 3.74 in and r_x = 6.24 in.: kL/r_y = 48.1 and $\underline{kL/r_x = 57.7}$ (GOVERNS)

   ϕF_{cr} for 58 is 35.2 ksi, F_{cr} = 39.1 ksi so $A \geq$ 560 k(1.67)/39.1 ksi = 23.9 in^2

Choose a W14 x 90 (Choosing a W14 x 82 would make kL/r_x = 59.5, and $A_{req'd}$ = 24.3 in^2, which is more than 24.1 in^2!)

LRFD:

1. P_u = 1.2(140 k) + 1.6(420 k) = 840 k
2. The effective length in the weak (y-y) axis is 15 ft, while the effective length in the strong (x-x) axis is 30 ft. (K = 1, KL = 1×30 ft). To find kL/r_x and kL/r_y we can assume or choose values from the wide flange charts. r_y's range from 1 to 3 in., while r_x's range from 3 to 14 inches. Let's try r_y = 2 in and r_x = 9 in. (something in the W21 range, say.)

   $kL/r_y \cong$ 15 ft(12 in/ft)/2 in. = 90 $\Leftarrow$ GOVERNS (is larger)

   $kL/r_x \cong$ 30 ft(12 in/ft)/9 in. = 40
3. Find a section with sufficient area (which then will give us "real" values for r_x and r_y):

   If $P_u \leq \phi P_n$, and $\phi P_n = \phi F_{cr} A$, we can find $A \geq P_u/\phi F_{cr}$ with ϕ = 0.9

   ϕF_{cr} for 90 is 24.9 ksi, so $A \geq$ 840 k/24.9 ksi = 33.7 in^2
4. Choose a trial section, and find the effective lengths and associated available strength, ϕF_{cr} :

   Looking from the smallest sections, the W14's are the first with a big enough area:

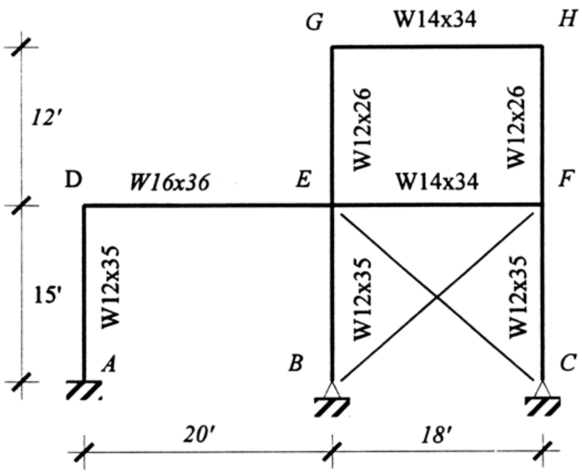
   Try a W14 x 120 (A = 35.3 in^2) with r_y = 3.74 in and r_x = 6.24 in.: kL/r_y = 48.1 and $\underline{kL/r_x = 57.7}$ (GOVERNS)

   ϕF_{cr} for 58 is 35.2 ksi, so $A \geq$ 840 k/35.2 ksi = 23.9 in^2

Choose a W14 x 90 (Choosing a W14 x 82 would make kL/r_x = 59.5, and $A_{req'd}$ = 24.3 in^2, which is more than 24.1 in^2!)

Example 13

Example 6-1: For the building frame shown in Fig. 6-20, determine the effective column length factor, K, the slenderness ratio, KL/r for each column. Assume the columns buckle and the beams bend about their strong axis.



W12x26:

$I_x = 204$ in.^{4}
$r_x = 5.17$ in.^{4}

W12x35:

$I_x = 285$ in.^{4}
$r_x = 5.25$ in.^{4}

W14x34:

$I_x = 340$ in.^{4}

W16x36:

$I_x = 448$ in.^{4}

Figure 6-20: Building frame for Example 6-1.

Solution:

Note: The diagonal bracing prevents sidesway of the first story columns only.

$G_A =$ 1.0 (fixed support) $G_B = G_C =$ 10.0 (pinned support)

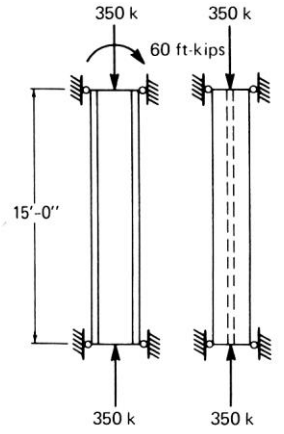
$$G_D = \frac{\frac{285}{15}}{\frac{448}{20}} = 0.85 \qquad G_E = \frac{\frac{285}{15} + \frac{204}{12}}{\frac{448}{20} + \frac{340}{18}} = 0.87$$

$$G_F = \frac{\frac{285}{15} + \frac{204}{12}}{\frac{340}{18}} = 1.91 \qquad G_G = G_H = \frac{\frac{204}{12}}{\frac{340}{18}} = 0.90$$

Column	G_{Top}	G_{Bot}	K		KL/r
AD	0.85	1.0	0.76	Braced	0.76(15)(12)/5.25 = 26.1
BE	0.87	10.0	0.85	Braced	0.85(15)(12)/5.25 = 29.1
CF	1.91	10.0	0.90	Braced	0.90(15)(12)/5.25 = 30.9
EG	0.90	0.87	1.29	Unbraced	1.29(12)(12)/5.17 = 35.9
FH	0.90	1.91	1.43	Unbraced	1.43(12)(12)/5.17 = 39.8

Table 6-1: Column effective length factors and slenderness ratios for Example 6-1.

Example 14



Investigate the accepatbility of a W16 x 67 used as a beam-column under the unfactored loading shown in the figure. It is A992 steel (F_y = 50 ksi). Assume 25% of the load is dead load with 75% live load.

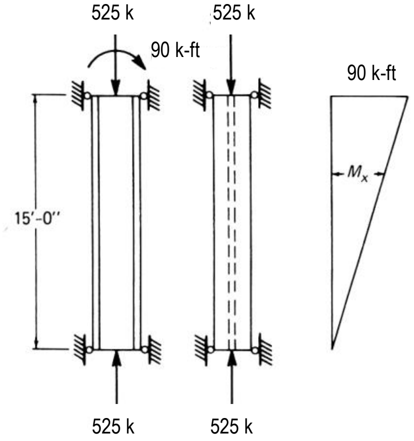
SOLUTION:

DESIGN LOADS (shown on figure):

Axial load = 1.2(0.25)(350k)+1.6(0.75)(350k)=525k

Moment at joint = 1.2(0.25)(60 $^{k\text{-}ft}$) + 1.6(0.75)(60 $^{k\text{-}ft}$) = 90 $^{k\text{-}ft}$

Determine column capacity and fraction to choose the appropriate interaction equation:



$\frac{kL}{r_x} = \frac{15ft(12^{in}/_{ft})}{6.96in} = 25.9$ and $\frac{kL}{r_y} = \frac{15ft(12^{in}/_{ft})}{2.46in} = 73$ (governs)

$$P_c = \phi_c P_n = \phi_c F_{cr} A_g = (30.5ksi)19.7in^2 = 600.85k$$

$\frac{P_r}{P_c} = \frac{525k}{600.85k} = 0.87 > 0.2$ so use $\frac{P_u}{\phi_c P_n} + \frac{8}{9}\left(\frac{M_{ux}}{\phi_b M_{nx}} + \frac{M_{uy}}{\phi_b M_{ny}}\right) \le 1.0$

There is no bending about the y axis, so that term will not have any values.

Determine the bending moment capacity in the x direction:

The unbraced length to use the full plastic moment (*L_p*) is listed as 8.69 ft, and we are over that so of we don't want to determine it from formula, we can find the beam in the Available Moment vs. Unbraced Length tables. The value of ϕM_n at *L_b* =15 ft is 422 k-ft.

Determine the magnification factor when M_1 = 0, M_2 = 90 k-ft:

$C_m = 0.6 - 0.4\frac{M_1}{M_2} = 0.6 - \frac{0^{k-ft}}{90^{k-ft}} = 0.6 \le 1.0$ $\qquad$ $P_{e1} = \frac{\pi^2 EA}{\left(Kl/_r\right)^2} = \frac{\pi^2(30x10^3ksi)19.7in^2}{(25.9)^2} = 8{,}695.4k$

$B_1 = \frac{C_m}{1-(P_u/P_{e1})} = \frac{0.6}{1-(525k/8695.4k)} = 0.64 \ngeq 1.0$ USE 1.0 $\qquad$ M_u = (1)90 k-ft

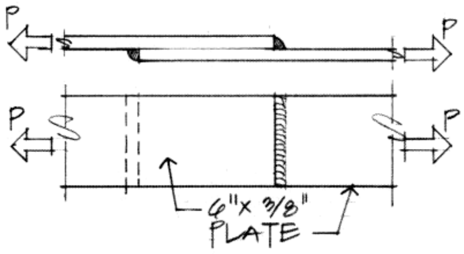
Finally, determine the interaction value:

$$\frac{P_u}{\phi_c P_n} + \frac{8}{9}\left(\frac{M_{ux}}{\phi_b M_{nx}} + \frac{M_{uy}}{\phi_b M_{ny}}\right) = 0.87 + \frac{8}{9}\left(\frac{90^{k-ft}}{422^{k-ft}}\right) = 1.06 \nleq 1.0$$

This is **NOT OK.** (and outside error tolerance). The section should be larger.

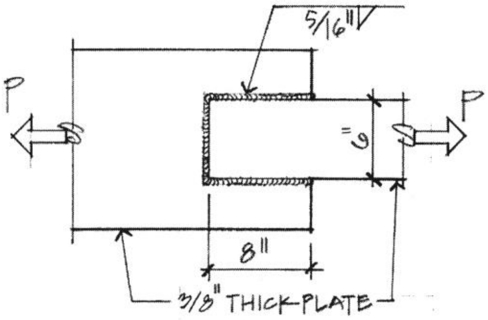
Example 15

10.9 Determine the maximum load carrying capacity of this lap joint., assuming A36 steel with E60XX electrodes.



Example 16

10.7 Determine the capacity of the connection in Figure 10.44 assuming A36 steel with E70XX electrodes.



Solution:

Capacity of weld:

For a 5⁄16″ fillet weld, $\phi S = 6.96$ k/in

Weld length = 8 in + 6 in + 8 in = 22 in.

Weld capacity = 22″ × 6.96 k/in = 153.1 k

Capacity of plate:

$\phi P_n = \phi F_y A_g \quad \phi = 0.9$

Plate capacity = 0.9 x 36 k/in^2 x 3/8″ x 6″= 72.9 k

∴ Plate capacity governs, P_{allow} = 72.9 k

The weld size used is obviously too strong. What size, then, can the weld be reduced to so that the weld strength is more compatible to the plate capacity? To make the weld capacity ≈ plate capacity:

22″ × (weld capacity per in.) = 72.9 k

Weld capacity per inch = $\dfrac{72.9\text{ k}}{22\text{ in.}}$ = 3.31 k/in.

From Available Strength table, use 3/16″ weld ($\phi S = 4.18$ k/in.)

Minimum size fillet = 3⁄16″ based on a 3⁄8″ thick plate.

Example 17

10.5 Using the AISC framed beam connection bolt shear in Table 7-1, determine the shear adequacy of the connection shown in Figure 10.28. What thickness and angle length are required? Also determine the bearing capacity of the wide flange sections.

Factored end beam reaction = 90 k.

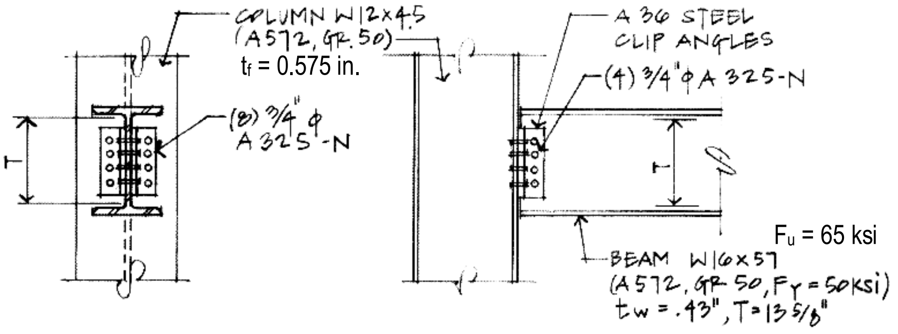
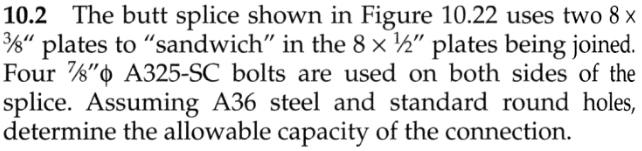
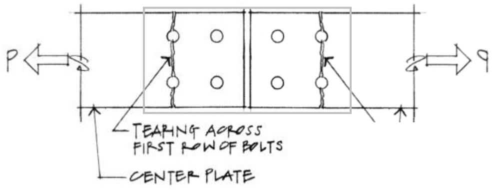


Figure 10.28 Typical beam–column connection.

Example 18

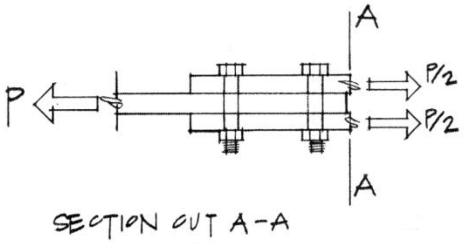


10.2 The butt splice shown in Figure 10.22 uses two 8 × ⅜" plates to "sandwich" in the 8 × ½" plates being joined. Four ⅞"ϕ A325-SC bolts are used on both sides of the splice. Assuming A36 steel and standard round holes, determine the allowable capacity of the connection.



SOLUTION:

Shear, bearing and net tension will be checked to determine the critical conditions that governs the capacity of the connection.



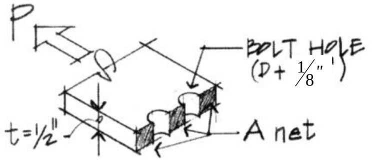
Shear: Using the AISC available shear in Table 7-3 (Group A):

ϕR_n = 26.4 k/bolt x 4 bolts = 105.6 k

Bearing: Using the AISC available bearing in Table 7-4:

There are 4 bolts bearing on the center (1/2") plate, while there are 4 bolts bearing on a total width of two sandwich plates (3/4" total). The thinner bearing width will govern. Assume 3 in. spacing (center to center) of bolts. For A36 steel, F_u = 58 ksi.

ϕR_n = 91.4 k/bolt/in. x 0.5 in. x 4 bolts = 182.8 k (Table 7-4)

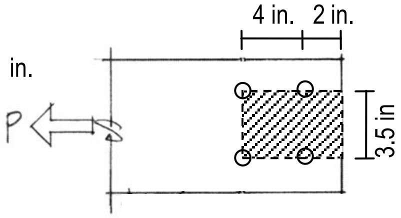


With the edge distance of 2 in., the bearing capacity might be smaller from Table 7-5 which says the distance should be 2 ¼ in for full bearing (and we have 2 in.).

ϕR_n = 79.9 k/bolt/in. x 0.5 in. x 4 bolts = 159.8 k

Tension: The center plate is critical, again, because its thickness is less than the combined thicknesses of the two outer plates. We must consider tension yielding and tension rupture:

$\phi R_n = \phi F_y A_g$ and $\phi R_n = \phi F_u A_e$ where $A_e = A_{net} U$



A_g = 8 in. x ½ in. = 4 in^2

The holes are considered 1/8 in. larger than the bolt hole diameter = (7/8 + 1/8) = 1.0 in.

A_n = (8 in. – 2 holes x 1.0 in.) x ½ in. = 3.0 in^2

The whole cross section sees tension, so the shear lag factor U = 1

$\phi F_y A_g$ = 0.9 x 36 ksi x 4 in^2 = 129.6 k

$\phi F_u A_e$ = 0.75 x 58 ksi x (1) x 3.0 in^2 = 130.5 k

The maximum connection capacity (*smallest value*) **so far** is governed by bolt shear: $\underline{\phi R_n = 105.6 \text{ k}}$

Block Shear Rupture: It is possible for the center plate to rip away from the sandwich plates leaving the block (shown hatched) behind:

$\phi R_n = \phi(0.6F_uA_{nv} + U_{bs}F_uA_{nt}) \leq \phi(0.6F_yA_{gv} + U_{bs}F_uA_{nt})$

where A_{nv} is the area resisting shear, A_{nt} is the area resisting tension, A_{gv} is the gross area resisting shear, and U_{bs} = 1 when the tensile stress is uniform.

A_{gv} = 2 x (4 + 2 in.) x ½ in. = 6 in^2

$A_{nv} = A_{gv}$ – 1 ½ holes areas = 6 in^2 – 1.5 x 1 in. x ½ in. = 5.25 in^2

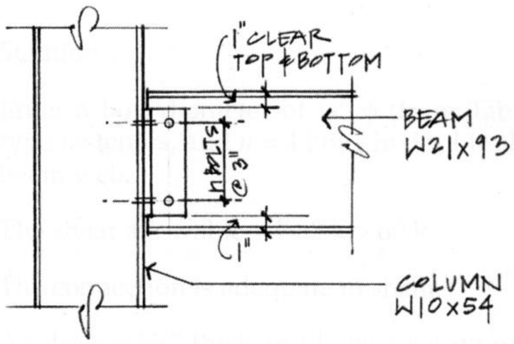
A_{nt} = 3.5 in. x t – 2(½ hole areas) = 3.5 in. x ½ in – 1 x 1 in. x ½ in. = 1.25 in^2

$\phi(0.6F_uA_{nv} + U_{bs}F_uA_{nt})$ = 0.75 x (0.6 x 58 ksi x 5.25 in^2 + 1 x 58 ksi x 1.25 in^2) = 191.4 k

$\phi(0.6F_yA_{gv} + U_{bs}F_uA_{nt})$ = 0.75 x (0.6 x 36 ksi x 6 in^2 + 1 x 58 ksi x 1.25 in^2) = 151.6 k

The maximum connection capacity (*smallest value*) is governed by block shear rupture: $\underline{\phi R_n = 151.6 \text{ k}}$

Example 19



The steel used in the connection and beams is A992 with F_y = 50 ksi, and F_u = 65 ksi. Using A490-N bolt material, determine the maximum capacity of the connection based on shear in the bolts, bearing in all materials and pick the number of bolts and angle length (not staggered). Use A36 steel for the angles.

W21x93: d = 21.62 in, t_w = 0.58 in, t_f = 0.93 in
W10x54: t_f = 0.615 in

SOLUTION:

The maximum length the angles can be depends on how it fits between the top and bottom flange with some clearance allowed for the fillet to the flange, and getting an air wrench in to tighten the bolts. This example uses 1" of clearance:

Available length = beam depth – both flange thicknesses – 1" clearance at top & 1" at bottom

= 21.62 in – 2(0.93 in) – 2(1 in) = 17.76 in.

With the spaced at 3 in. and 1 ¼ in. end lengths (each end), the maximum number of bolts can be determined:

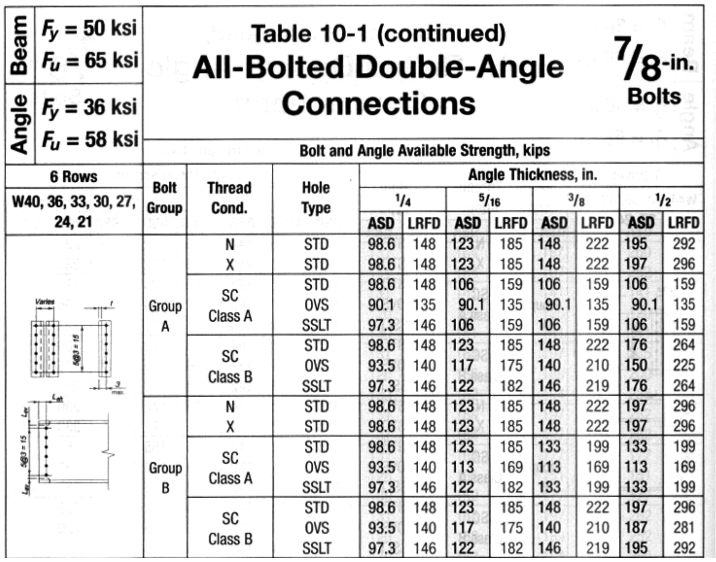
Available length ≥ 1.25 in. + 1.25 in. + 3 in. x (number of bolts – 1)

number of bolts ≤ (17.76 in – 2.5 in. - (-3 in.))/3 in. = 6.1, so 6 bolts.

It is helpful to have the All-bolted Double-Angle Connection Tables 10-1. They are available for ¾", 7/8", and 1" bolt diameters and list angle thicknesses of ¼", 5/16", 3/8", and ½". Increasing the angle thickness is likely to increase the angle strength, although the limit states include shear yielding of the angles, shear rupture of the angles, and block shear rupture of the angles.

For these diameters, the available **shear** (double) from Table 7-1 for 6 bolts is (6)45.1 k/bolt = 270.6 kips, (6)61.3 k/bolt = 367.8 kips, and (6)80.1 k/bolt = 480.6 kips.

Tables 10-1 (not all provided here) list a bolt and angle available strength of 271 kips for the ¾" bolts, 296 kips for the 7/8" bolts, and 281 kips for the 1" bolts. It appears that increasing the bolt diameter to 1" will not gain additional load. Use 7/8" bolts.



Beam F_y = 50 ksi F_u = 65 ksi
Angle F_y = 36 ksi F_u = 58 ksi

Table 10-1 (continued)
All-Bolted Double-Angle Connections
7/8-in. Bolts

Bolt and Angle Available Strength, kips

6 Rows W40, 36, 33, 30, 27, 24, 21	Bolt Group	Thread Cond.	Hole Type	Angle Thickness, in.							
				1/4		5/16		3/8		1/2	
				ASD	LRFD	ASD	LRFD	ASD	LRFD	ASD	LRFD
	Group A	N	STD	98.6	148	123	185	148	222	195	292
		X	STD	98.6	148	123	185	148	222	197	296
		SC Class A	STD	98.6	148	106	159	106	159	106	159
			OVS	90.1	135	90.1	135	90.1	135	90.1	135
			SSLT	97.3	146	106	159	106	159	106	159
		SC Class B	STD	98.6	148	123	185	148	222	176	264
			OVS	93.5	140	117	175	140	210	150	225
			SSLT	97.3	146	122	182	146	219	176	264
	Group B	N	STD	98.6	148	123	185	148	222	197	296
		X	STD	98.6	148	123	185	148	222	197	296
		SC Class A	STD	98.6	148	123	185	133	199	133	199
			OVS	93.5	140	113	169	113	169	113	169
			SSLT	97.3	146	122	182	133	199	133	199
		SC Class B	STD	98.6	148	123	185	148	222	197	296
			OVS	93.5	140	117	175	140	210	187	281
			SSLT	97.3	146	122	182	146	219	195	292

ϕR_n = 367.8 kips for double shear of 7/8" bolts ϕR_n = 296 kips for limit state in angles

We also need to evaluate **bearing** of bolts on the beam web, and column flange where there are bolt holes. Table 7-4 provides available bearing strength for the material type, bolt diameter, hole type, and spacing per inch of material thicknesses.

a) Bearing for beam web: There are *6* bolt holes through the beam web. This is typically the critical bearing limit value because there are two angle legs that resist bolt bearing and twice as many bolt holes to the column. The material is A992 (F_u = 65 ksi), 0.58" thick, with 7/8" bolt diameters at 3 in. spacing.

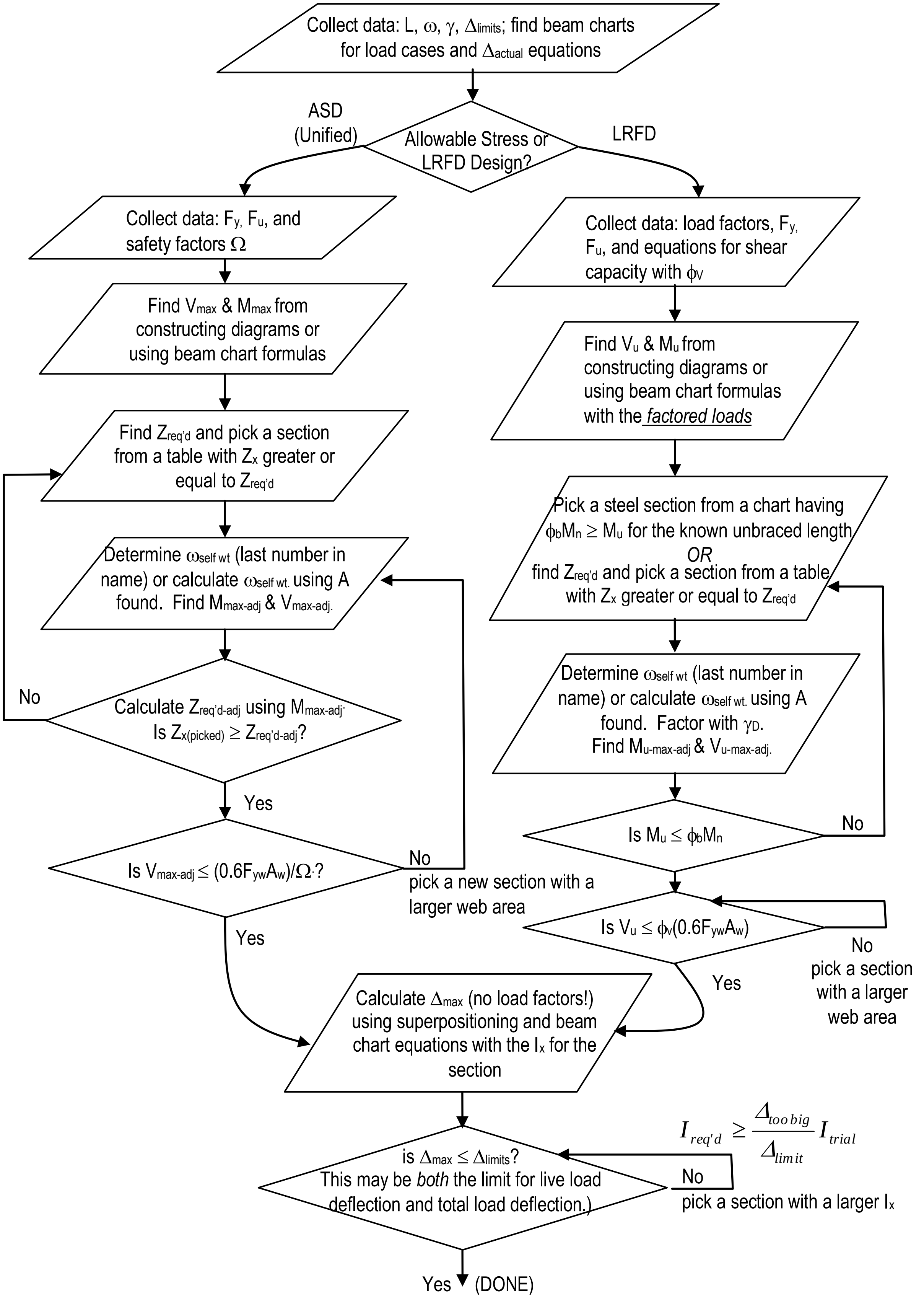
ϕR_n = 6 bolts·(102 k/bolt/inch)·(0.58 in) = 355.0 kips

b) Bearing for column flange: There are 12 bolt holes through the column. The material is A992 (F_u = 65 ksi), 0.615" thick, with 1" bolt diameters.

ϕR_n = 12 bolts·(102 k/bolt/inch)·(0.615 in) = 752.8 kips

Although, the bearing in the beam web is the smallest at 355 kips, with the shear on the bolts even smaller at 324.6 kips, *the maximum capacity for the simple-shear connector is 296 kips* limited by the critical capacity of the angles.

Beam Design Flow Chart



Listing of W Shapes in Descending order of Z_x for Beam Design

Z_x – US (in.^{3})	I_x – US (in.^{4})	Section	I_x – SI (10^{6}mm.^{4})	Z_x – SI (10^{3}mm.3)
514	**7450**	**W33X141**	**3100**	**8420**
511	5680	W24X176	2360	8370
509	**7800**	**W36X135**	**3250**	**8340**
500	6680	W30X148	2780	8190
490	4330	W18X211	1800	8030
487	3400	W14X257	1420	7980
481	3110	W12X279	1290	7880
476	4730	W21X182	1970	7800
468	5170	W24X162	2150	7670
467	**6710**	**W33X130**	**2790**	**7650**
464	5660	W27X146	2360	7600
442	3870	W18X192	1610	7240
437	5770	W30X132	2400	7160
436	3010	W14X233	1250	7140
432	4280	W21X166	1780	7080
428	2720	W12X252	1130	7010
418	4580	W24X146	1910	6850
415	**5900**	**W33X118**	**2460**	**6800**
408	5360	W30X124	2230	6690
398	3450	W18X175	1440	6520
395	4760	W27X129	1980	6470
390	2660	W14X211	1110	6390
386	2420	W12X230	1010	6330
378	**4930**	**W30X116**	**2050**	**6190**
373	3630	W21X147	1510	6110
370	4020	W24X131	1670	6060
356	3060	W18X158	1270	5830
355	2400	W14X193	999	5820
348	2140	W12X210	891	5700
346	**4470**	**W30X108**	**1860**	**5670**
343	4080	W27X114	1700	5620
333	3220	W21X132	1340	5460
327	3540	W24X117	1470	5360
322	2750	W18X143	1140	5280
320	2140	W14X176	891	5240
312	**3990**	**W30X99**	**1660**	**5110**
311	1890	W12X190	787	5100
307	2960	W21X122	1230	5030
305	3620	W27X102	1510	5000
290	2460	W18X130	1020	4750
289	3100	W24X104	1290	4740
287	1900	W14X159	791	4700
283	**3610**	**W30X90**	**1500**	**4640**
280	3000	W24X103	1250	4590
279	2670	W21X111	1110	4570
278	3270	W27X94	1360	4560
275	1650	W12X170	687	4510
262	2190	W18X119	912	4290
260	1710	W14X145	712	4260
254	2700	W24X94	1120	4160
253	2420	W21X101	1010	4150
244	**2850**	**W27X84**	**1190**	**4000**
243	1430	W12X152	595	3980
234	1530	W14X132	637	3830
230	1910	W18X106	795	3770
224	**2370**	**W24X84**	**986**	**3670**
221	2070	W21X93	862	3620
214	1240	W12X136	516	3510
212	1380	W14X120	574	3470
211	1750	W18X97	728	3460
200	**2100**	**W24X76**	**874**	**3280**
198	1490	W16X100	620	3240
196	1830	W21X83	762	3210
192	1240	W14X109	516	3150
186	1530	W18X86	637	3050
186	1070	W12X120	445	3050
177	**1830**	**W24X68**	**762**	**2900**
175	1300	W16X89	541	2870
173	1110	W14X99	462	2830
172	1600	W21X73	666	2820
164	933	W12X106	388	2690
163	1330	W18X76	554	2670
160	**1480**	**W21X68**	**616**	**2620**
157	999	W14X90	416	2570
153	**1550**	**W24X62**	**645**	**2510**
150	1110	W16X77	462	2460
147	833	W12X96	347	2410
147	716	W10X112	298	2410
146	1170	W18X71	487	2390

(continued)

Listing of W Shapes in Descending order of Z_x for Beam Design (Continued)

Z_x – US (in.^{3})	I_x – US (in.^{4})	Section	I_x – SI (10^{6}mm.^{4})	Z_x – SI (10^{3}mm.3)	Z_x – US (in.^{3})	I_x – US (in.^{4})	Section	I_x – SI (10^{6}mm.^{4})	Z_x – SI (10^{3}mm.3)
144	**1330**	**W21X62**	**554**	**2360**	**66.5**	**510**	**W18X35**	**212**	**1090**
139	881	W14X82	367	2280	64.2	348	W12X45	145	1050
134	**1350**	**W24X55**	**562**	**2200**	64.0	448	W16X36	186	1050
133	1070	W18X65	445	2180	61.5	385	W14X38	160	1010
132	740	W12X87	308	2160	60.4	272	W10X49	113	990
130	954	W16X67	397	2130	59.8	228	W8X58	94.9	980
130	623	W10X100	259	2130	57.0	307	W12X40	128	934
129	1170	W21X57	487	2110	54.9	248	W10X45	103	900
126	**1140**	**W21X55**	**475**	**2060**	**54.6**	**340**	**W14X34**	**142**	**895**
126	795	W14X74	331	2060	**54.0**	**375**	**W16X31**	**156**	**885**
123	984	W18X60	410	2020	51.2	285	W12X35	119	839
119	662	W12X79	276	1950	49.0	184	W8X48	76.6	803
115	722	W14X68	301	1880	**47.3**	**291**	**W14X30**	**121**	**775**
113	534	W10X88	222	1850	46.8	209	W10X39	87.0	767
112	**890**	**W18X55**	**370**	**1840**	**44.2**	**301**	**W16X26**	**125**	**724**
110	**984**	**W21X50**	**410**	**1800**	43.1	238	W12X30	99.1	706
108	597	W12X72	248	1770	**40.2**	**245**	**W14X26**	**102**	**659**
107	**959**	**W21X48**	**399**	**1750**	39.8	146	W8X40	60.8	652
105	758	W16X57	316	1720	38.8	171	W10X33	71.2	636
102	640	W14X61	266	1670	**37.2**	**204**	**W12X26**	**84.9**	**610**
101	800	W18X50	333	1660	36.6	170	W10X30	70.8	600
97.6	455	W10X77	189	1600	34.7	127	W8X35	52.9	569
96.8	533	W12X65	222	1590	**33.2**	**199**	**W14X22**	**82.8**	**544**
95.4	**843**	**W21X44**	**351**	**1560**	31.3	144	W10X26	59.9	513
92.0	659	W16X50	274	1510	30.4	110	W8X31	45.8	498
90.7	712	W18X46	296	1490	**29.3**	**156**	**W12X22**	**64.9**	**480**
87.1	541	W14X53	225	1430	27.2	98.0	W8X28	40.8	446
86.4	475	W12X58	198	1420	**26.0**	**118**	**W10X22**	**49.1**	**426**
85.3	394	W10X68	164	1400	**24.7**	**130**	**W12X19**	**54.1**	**405**
82.3	586	W16X45	244	1350	23.1	82.7	W8X24	34.4	379
78.4	**612**	**W18X40**	**255**	**1280**	**21.6**	**96.3**	**W10X19**	**40.1**	**354**
78.4	484	W14X48	201	1280	20.4	75.3	W8X21	31.3	334
77.9	425	W12X53	177	1280	**20.1**	**103**	**W12x16**	**42.9**	**329**
74.6	341	W10X60	142	1220	18.7	81.9	W10X17	34.1	306
73.0	**518**	**W16X40**	**216**	**1200**	**17.4**	**88.6**	**W12X14**	**36.9**	**285**
71.9	391	W12X50	163	1180	17.0	61.9	W8X18	25.8	279
70.1	272	W8X67	113	1150	16.0	68.9	W10X15	28.7	262
69.6	428	W14X43	178	1140	13.6	48.0	W8X15	20.0	223
66.6	303	W10X54	126	1090	**12.6**	**53.8**	**W10X12**	**22.4**	**206**
					11.4	39.6	W8X13	16.5	187
					8.87	**30.8**	**W8X10**	**12.8**	**145**

Available Critical Stress, $\phi_c F_{cr}$, for Compression Members, ksi (F_y = 36 ksi and ϕ_c = 0.90)

KL/r	$\phi_c\ F_{cr}$	KL/r	$\phi_c\ F_{cr}$	KL/r	$\phi_c\ F_{cr}$	KL/r	$\phi_c\ F_{cr}$	KL/r	$\phi_c\ F_{cr}$
1	32.4	41	29.7	81	22.9	121	15.0	161	8.72
2	32.4	42	29.5	82	22.7	122	14.8	162	8.61
3	32.4	43	29.4	83	22.5	123	14.6	163	8.50
4	32.4	44	29.3	84	22.3	124	14.4	164	8.40
5	32.4	45	29.1	85	22.1	125	14.2	165	8.30
6	32.3	46	29.0	86	22.0	126	14.0	166	8.20
7	32.3	47	28.8	87	21.8	127	13.9	167	8.10
8	32.3	48	28.7	88	21.6	128	13.7	168	8.00
9	32.3	49	28.6	89	21.4	129	13.5	169	7.91
10	32.2	50	28.4	90	21.2	130	13.3	170	7.82
11	32.2	51	28.3	91	21.0	131	13.1	171	7.73
12	32.2	52	28.1	92	20.8	132	12.9	172	7.64
13	32.1	53	27.9	93	20.5	133	12.8	173	7.55
14	32.1	54	27.8	94	20.3	134	12.6	174	7.46
15	32.0	55	27.6	95	20.1	135	12.4	175	7.38
16	32.0	56	27.5	96	19.9	136	12.2	176	7.29
17	31.9	57	27.3	97	19.7	137	12.0	177	7.21
18	31.9	58	27.1	98	19.5	138	11.9	178	7.13
19	31.8	59	27.0	99	19.3	139	11.7	179	7.05
20	31.7	60	26.8	100	19.1	140	11.5	180	6.97
21	31.7	61	26.6	101	18.9	141	11.4	181	6.90
22	31.6	62	26.5	102	18.7	142	11.2	182	6.82
23	31.5	63	26.3	103	18.5	143	11.0	183	6.75
24	31.4	64	26.1	104	18.3	144	10.9	184	6.67
25	31.4	65	25.9	105	18.1	145	10.7	185	6.60
26	31.3	66	25.8	106	17.9	146	10.6	186	6.53
27	31.2	67	25.6	107	17.7	147	10.5	187	6.46
28	31.1	68	25.4	108	17.5	148	10.3	188	6.39
29	31.0	69	25.2	109	17.3	149	10.2	189	6.32
30	30.9	70	25.0	110	17.1	150	10.0	190	6.26
31	30.8	71	24.8	111	16.9	151	9.91	191	6.19
32	30.7	72	24.7	112	16.7	152	9.78	192	6.13
33	30.6	73	24.5	113	16.5	153	9.65	193	6.06
34	30.5	74	24.3	114	16.3	154	9.53	194	6.00
35	30.4	75	24.1	115	16.2	155	9.40	195	5.94
36	30.3	76	23.9	116	16.0	156	9.28	196	5.88
37	30.1	77	23.7	117	15.8	157	9.17	197	5.82
38	30.0	78	23.5	118	15.6	158	9.05	198	5.76
39	29.9	79	23.3	119	15.4	159	8.94	199	5.70
40	29.8	80	23.1	120	15.2	160	8.82	200	5.65

Available Critical Stress, $\phi_c F_{cr}$, for Compression Members, ksi (F_y = 50 ksi and ϕ_c = 0.90)

KL/r	$\phi_c F_{cr}$	*KL/r*	$\phi_c F_{cr}$	*KL/r*	$\phi_c F_{cr}$	*KL/r*	$\phi_c F_{cr}$	*KL/r*	$\phi_c F_{cr}$
1	45.0	41	39.8	81	27.9	121	15.4	161	8.72
2	45.0	42	39.6	82	27.5	122	15.2	162	8.61
3	45.0	43	39.3	83	27.2	123	14.9	163	8.50
4	44.9	44	39.1	84	26.9	124	14.7	164	8.40
5	44.9	45	38.8	85	26.5	125	14.5	165	8.30
6	44.9	46	38.5	86	26.2	126	14.2	166	8.20
7	44.8	47	38.3	87	25.9	127	14.0	167	8.10
8	44.8	48	38.0	88	25.5	128	13.8	168	8.00
9	44.7	49	37.8	89	25.2	129	13.6	169	7.91
10	44.7	50	37.5	90	24.9	130	13.4	170	7.82
11	44.6	51	37.2	91	24.6	131	13.2	171	7.73
12	44.5	52	36.9	92	24.2	132	13.0	172	7.64
13	44.4	53	36.6	93	23.9	133	12.8	173	7.55
14	44.4	54	36.4	94	23.6	134	12.6	174	7.46
15	44.3	55	36.1	95	23.3	135	12.4	175	7.38
16	44.2	56	35.8	96	22.9	136	12.2	176	7.29
17	44.1	57	35.5	97	22.6	137	12.0	177	7.21
18	43.9	58	35.2	98	22.3	138	11.9	178	7.13
19	43.8	59	34.9	99	22.0	139	11.7	179	7.05
20	43.7	60	34.6	100	21.7	140	11.5	180	6.97
21	43.6	61	34.3	101	21.3	141	11.4	181	6.90
22	43.4	62	34.0	102	21.0	142	11.2	182	6.82
23	43.3	63	33.7	103	20.7	143	11.0	183	6.75
24	43.1	64	33.4	104	20.4	144	10.9	184	6.67
25	43.0	65	33.0	105	20.1	145	10.7	185	6.60
26	42.8	66	32.7	106	19.8	146	10.6	186	6.53
27	42.7	67	32.4	107	19.5	147	10.5	187	6.46
28	42.5	68	32.1	108	19.2	148	10.3	188	6.39
29	42.3	69	31.8	109	18.9	149	10.2	189	6.32
30	42.1	70	31.4	110	18.6	150	10.0	190	6.26
31	41.9	71	31.1	111	18.3	151	9.91	191	6.19
32	41.8	72	30.8	112	18.0	152	9.78	192	6.13
33	41.6	73	30.5	113	17.7	153	9.65	193	6.06
34	41.4	74	30.2	114	17.4	154	9.53	194	6.00
35	41.1	75	29.8	115	17.1	155	9.40	195	5.94
36	40.9	76	29.5	116	16.8	156	9.28	196	5.88
37	40.7	77	29.2	117	16.5	157	9.17	197	5.82
38	40.5	78	28.8	118	16.2	158	9.05	198	5.76
39	40.3	79	28.5	119	16.0	159	8.94	199	5.70
40	40.0	80	28.2	120	15.7	160	8.82	200	5.65

Bolt Strength Tables

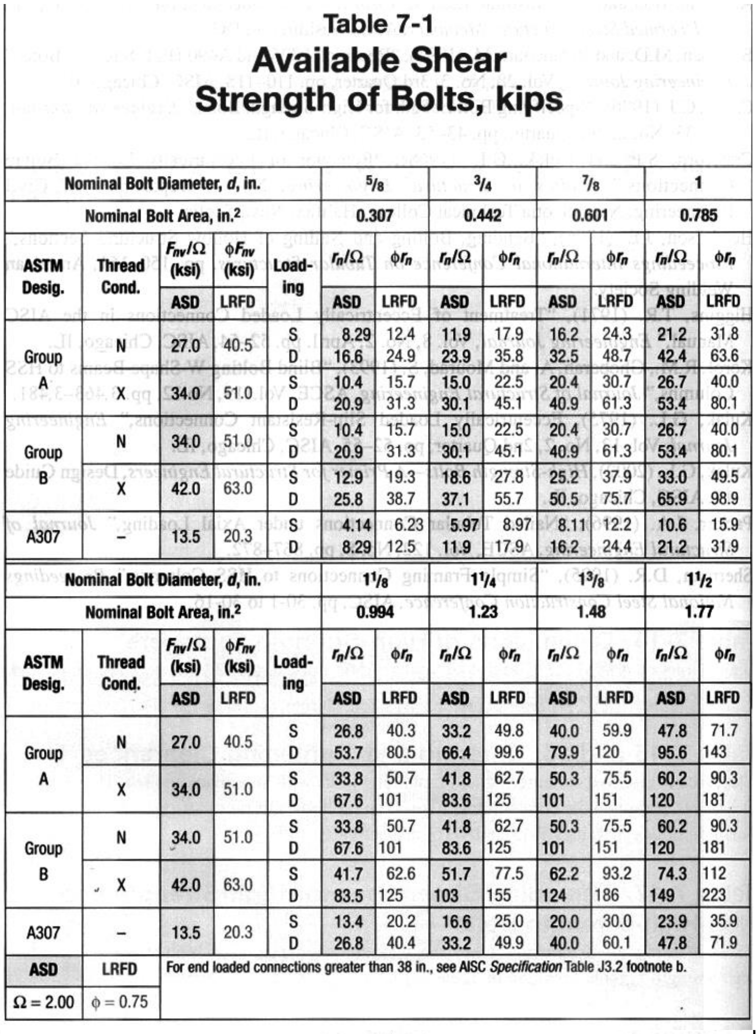


Table 7-1
Available Shear Strength of Bolts, kips

Nominal Bolt Diameter, *d*, in.					5/8		3/4		7/8		1	
Nominal Bolt Area, in.^{2}					0.307		0.442		0.601		0.785	
ASTM Desig.	Thread Cond.	F_{nv}/Ω (ksi)	ϕF_{nv} (ksi)	Load-ing	r_n/Ω	ϕr_n	r_n/Ω	ϕr_n	r_n/Ω	ϕr_n	r_n/Ω	ϕr_n
		ASD	LRFD		ASD	LRFD	ASD	LRFD	ASD	LRFD	ASD	LRFD
Group A	N	27.0	40.5	S	8.29	12.4	11.9	17.9	16.2	24.3	21.2	31.8
				D	16.6	24.9	23.9	35.8	32.5	48.7	42.4	63.6
	X	34.0	51.0	S	10.4	15.7	15.0	22.5	20.4	30.7	26.7	40.0
				D	20.9	31.3	30.1	45.1	40.9	61.3	53.4	80.1
Group B	N	34.0	51.0	S	10.4	15.7	15.0	22.5	20.4	30.7	26.7	40.0
				D	20.9	31.3	30.1	45.1	40.9	61.3	53.4	80.1
	X	42.0	63.0	S	12.9	19.3	18.6	27.8	25.2	37.9	33.0	49.5
				D	25.8	38.7	37.1	55.7	50.5	75.7	65.9	98.9
A307	–	13.5	20.3	S	4.14	6.23	5.97	8.97	8.11	12.2	10.6	15.9
				D	8.29	12.5	11.9	17.9	16.2	24.4	21.2	31.9

Nominal Bolt Diameter, *d*, in.					1 1/8		1 1/4		1 3/8		1 1/2	
Nominal Bolt Area, in.^{2}					0.994		1.23		1.48		1.77	
ASTM Desig.	Thread Cond.	F_{nv}/Ω (ksi)	ϕF_{nv} (ksi)	Load-ing	r_n/Ω	ϕr_n	r_n/Ω	ϕr_n	r_n/Ω	ϕr_n	r_n/Ω	ϕr_n
		ASD	LRFD		ASD	LRFD	ASD	LRFD	ASD	LRFD	ASD	LRFD
Group A	N	27.0	40.5	S	26.8	40.3	33.2	49.8	40.0	59.9	47.8	71.7
				D	53.7	80.5	66.4	99.6	79.9	120	95.6	143
	X	34.0	51.0	S	33.8	50.7	41.8	62.7	50.3	75.5	60.2	90.3
				D	67.6	101	83.6	125	101	151	120	181
Group B	N	34.0	51.0	S	33.8	50.7	41.8	62.7	50.3	75.5	60.2	90.3
				D	67.6	101	83.6	125	101	151	120	181
	X	42.0	63.0	S	41.7	62.6	51.7	77.5	62.2	93.2	74.3	112
				D	83.5	125	103	155	124	186	149	223
A307	–	13.5	20.3	S	13.4	20.2	16.6	25.0	20.0	30.0	23.9	35.9
				D	26.8	40.4	33.2	49.9	40.0	60.1	47.8	71.9

ASD	LRFD	For end loaded connections greater than 38 in., see AISC *Specification* Table J3.2 footnote b.
$\Omega = 2.00$	$\phi = 0.75$	

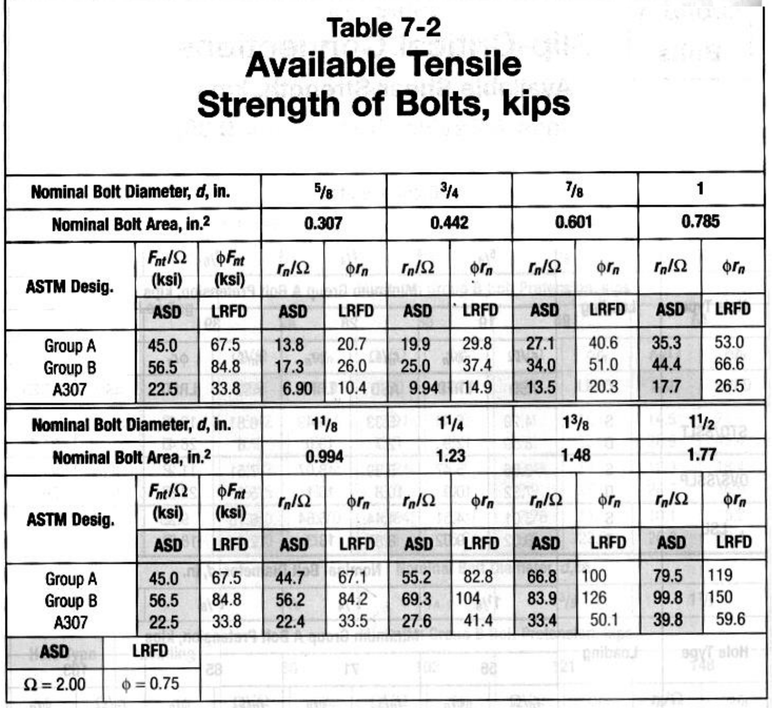
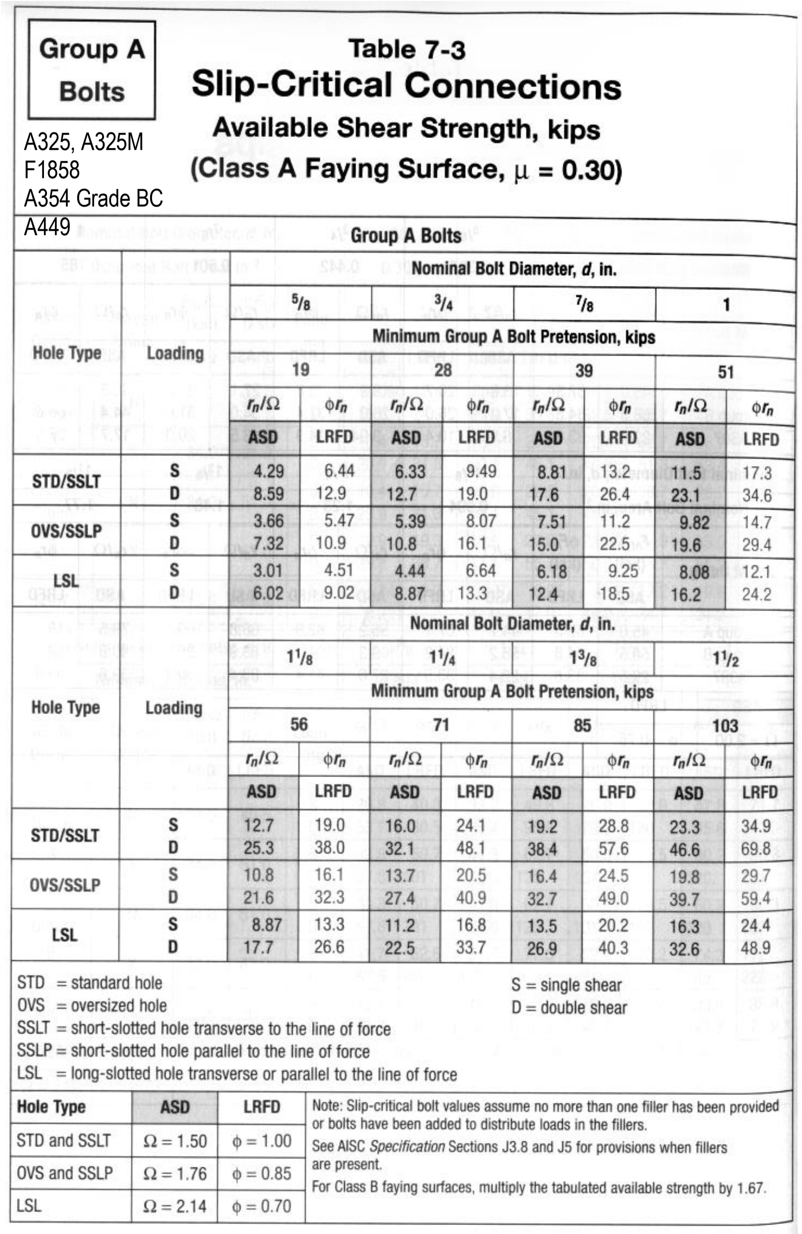


Table 7-2
Available Tensile Strength of Bolts, kips

Nominal Bolt Diameter, *d*, in.			5/8		3/4		7/8		1	
Nominal Bolt Area, in.^{2}			0.307		0.442		0.601		0.785	
ASTM Desig.	F_{nt}/Ω (ksi)	ϕF_{nt} (ksi)	r_n/Ω	ϕr_n	r_n/Ω	ϕr_n	r_n/Ω	ϕr_n	r_n/Ω	ϕr_n
	ASD	LRFD	ASD	LRFD	ASD	LRFD	ASD	LRFD	ASD	LRFD
Group A	45.0	67.5	13.8	20.7	19.9	29.8	27.1	40.6	35.3	53.0
Group B	56.5	84.8	17.3	26.0	25.0	37.4	34.0	51.0	44.4	66.6
A307	22.5	33.8	6.90	10.4	9.94	14.9	13.5	20.3	17.7	26.5

Nominal Bolt Diameter, *d*, in.			1 1/8		1 1/4		1 3/8		1 1/2	
Nominal Bolt Area, in.^{2}			0.994		1.23		1.48		1.77	
ASTM Desig.	F_{nt}/Ω (ksi)	ϕF_{nt} (ksi)	r_n/Ω	ϕr_n	r_n/Ω	ϕr_n	r_n/Ω	ϕr_n	r_n/Ω	ϕr_n
	ASD	LRFD	ASD	LRFD	ASD	LRFD	ASD	LRFD	ASD	LRFD
Group A	45.0	67.5	44.7	67.1	55.2	82.8	66.8	100	79.5	119
Group B	56.5	84.8	56.2	84.2	69.3	104	83.9	126	99.8	150
A307	22.5	33.8	22.4	33.5	27.6	41.4	33.4	50.1	39.8	59.6

ASD	LRFD
$\Omega = 2.00$	$\phi = 0.75$



Group A Bolts

A325, A325M
F1858
A354 Grade BC
A449

Table 7-3
Slip-Critical Connections
Available Shear Strength, kips
(Class A Faying Surface, $\mu = 0.30$)

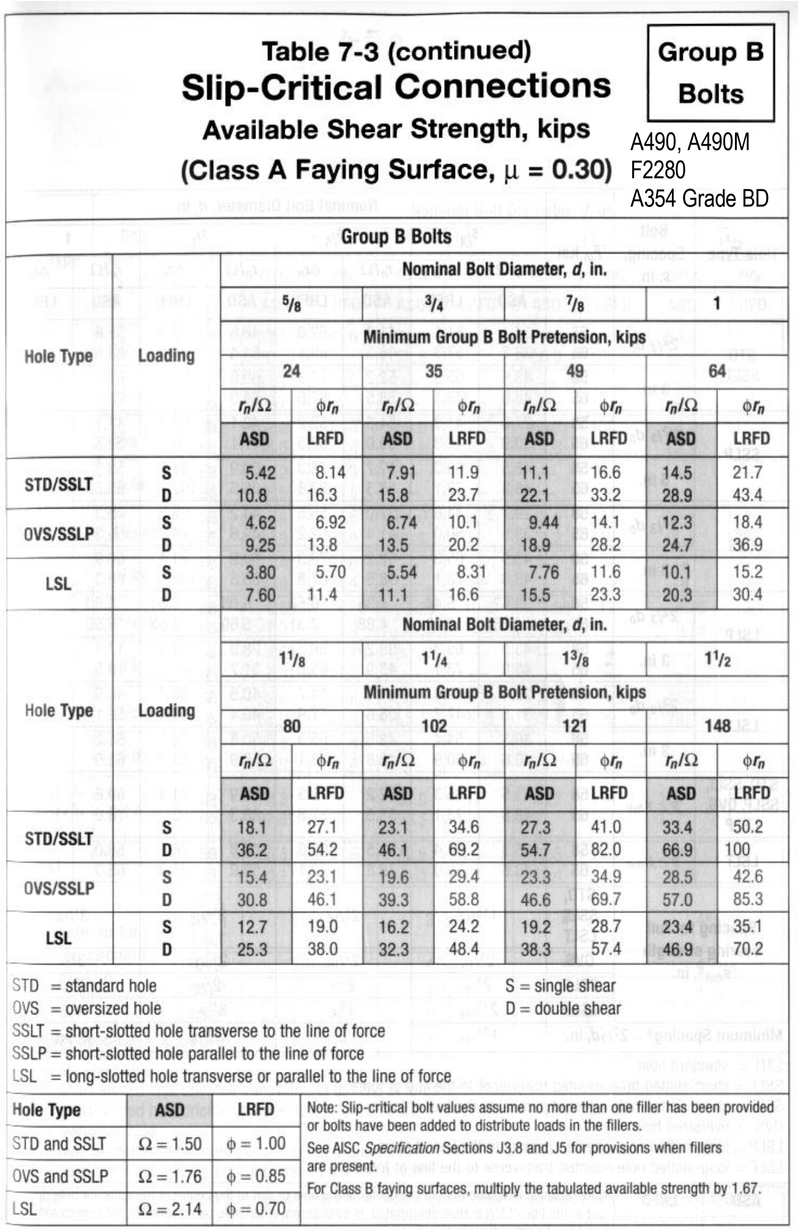
Group A Bolts									
		Nominal Bolt Diameter, *d*, in.							
		5/8		3/4		7/8		1	
		Minimum Group A Bolt Pretension, kips							
Hole Type	Loading	19		28		39		51	
		r_n/Ω	ϕr_n	r_n/Ω	ϕr_n	r_n/Ω	ϕr_n	r_n/Ω	ϕr_n
		ASD	LRFD	ASD	LRFD	ASD	LRFD	ASD	LRFD
STD/SSLT	S	4.29	6.44	6.33	9.49	8.81	13.2	11.5	17.3
	D	8.59	12.9	12.7	19.0	17.6	26.4	23.1	34.6
OVS/SSLP	S	3.66	5.47	5.39	8.07	7.51	11.2	9.82	14.7
	D	7.32	10.9	10.8	16.1	15.0	22.5	19.6	29.4
LSL	S	3.01	4.51	4.44	6.64	6.18	9.25	8.08	12.1
	D	6.02	9.02	8.87	13.3	12.4	18.5	16.2	24.2
		Nominal Bolt Diameter, *d*, in.							
		1 1/8		1 1/4		1 3/8		1 1/2	
		Minimum Group A Bolt Pretension, kips							
Hole Type	Loading	56		71		85		103	
		r_n/Ω	ϕr_n	r_n/Ω	ϕr_n	r_n/Ω	ϕr_n	r_n/Ω	ϕr_n
		ASD	LRFD	ASD	LRFD	ASD	LRFD	ASD	LRFD
STD/SSLT	S	12.7	19.0	16.0	24.1	19.2	28.8	23.3	34.9
	D	25.3	38.0	32.1	48.1	38.4	57.6	46.6	69.8
OVS/SSLP	S	10.8	16.1	13.7	20.5	16.4	24.5	19.8	29.7
	D	21.6	32.3	27.4	40.9	32.7	49.0	39.7	59.4
LSL	S	8.87	13.3	11.2	16.8	13.5	20.2	16.3	24.4
	D	17.7	26.6	22.5	33.7	26.9	40.3	32.6	48.9

STD = standard hole
OVS = oversized hole
SSLT = short-slotted hole transverse to the line of force
SSLP = short-slotted hole parallel to the line of force
LSL = long-slotted hole transverse or parallel to the line of force

S = single shear
D = double shear

Hole Type	ASD	LRFD
STD and SSLT	$\Omega = 1.50$	$\phi = 1.00$
OVS and SSLP	$\Omega = 1.76$	$\phi = 0.85$
LSL	$\Omega = 2.14$	$\phi = 0.70$

Note: Slip-critical bolt values assume no more than one filler has been provided or bolts have been added to distribute loads in the fillers.
See AISC *Specification* Sections J3.8 and J5 for provisions when fillers are present.
For Class B faying surfaces, multiply the tabulated available strength by 1.67.



Group B Bolts

A490, A490M
F2280
A354 Grade BD

Table 7-3 (continued)
Slip-Critical Connections
Available Shear Strength, kips
(Class A Faying Surface, $\mu = 0.30$)

Group B Bolts									
		Nominal Bolt Diameter, *d*, in.							
		5/8		3/4		7/8		1	
		Minimum Group B Bolt Pretension, kips							
Hole Type	Loading	24		35		49		64	
		r_n/Ω	ϕr_n	r_n/Ω	ϕr_n	r_n/Ω	ϕr_n	r_n/Ω	ϕr_n
		ASD	LRFD	ASD	LRFD	ASD	LRFD	ASD	LRFD
STD/SSLT	S	5.42	8.14	7.91	11.9	11.1	16.6	14.5	21.7
	D	10.8	16.3	15.8	23.7	22.1	33.2	28.9	43.4
OVS/SSLP	S	4.62	6.92	6.74	10.1	9.44	14.1	12.3	18.4
	D	9.25	13.8	13.5	20.2	18.9	28.2	24.7	36.9
LSL	S	3.80	5.70	5.54	8.31	7.76	11.6	10.1	15.2
	D	7.60	11.4	11.1	16.6	15.5	23.3	20.3	30.4
		Nominal Bolt Diameter, *d*, in.							
		1 1/8		1 1/4		1 3/8		1 1/2	
		Minimum Group B Bolt Pretension, kips							
Hole Type	Loading	80		102		121		148	
		r_n/Ω	ϕr_n	r_n/Ω	ϕr_n	r_n/Ω	ϕr_n	r_n/Ω	ϕr_n
		ASD	LRFD	ASD	LRFD	ASD	LRFD	ASD	LRFD
STD/SSLT	S	18.1	27.1	23.1	34.6	27.3	41.0	33.4	50.2
	D	36.2	54.2	46.1	69.2	54.7	82.0	66.9	100
OVS/SSLP	S	15.4	23.1	19.6	29.4	23.3	34.9	28.5	42.6
	D	30.8	46.1	39.3	58.8	46.6	69.7	57.0	85.3
LSL	S	12.7	19.0	16.2	24.2	19.2	28.7	23.4	35.1
	D	25.3	38.0	32.3	48.4	38.3	57.4	46.9	70.2

STD = standard hole
OVS = oversized hole
SSLT = short-slotted hole transverse to the line of force
SSLP = short-slotted hole parallel to the line of force
LSL = long-slotted hole transverse or parallel to the line of force

S = single shear
D = double shear

Hole Type	ASD	LRFD
STD and SSLT	$\Omega = 1.50$	$\phi = 1.00$
OVS and SSLP	$\Omega = 1.76$	$\phi = 0.85$
LSL	$\Omega = 2.14$	$\phi = 0.70$

Note: Slip-critical bolt values assume no more than one filler has been provided or bolts have been added to distribute loads in the fillers.
See AISC *Specification* Sections J3.8 and J5 for provisions when fillers are present.
For Class B faying surfaces, multiply the tabulated available strength by 1.67.

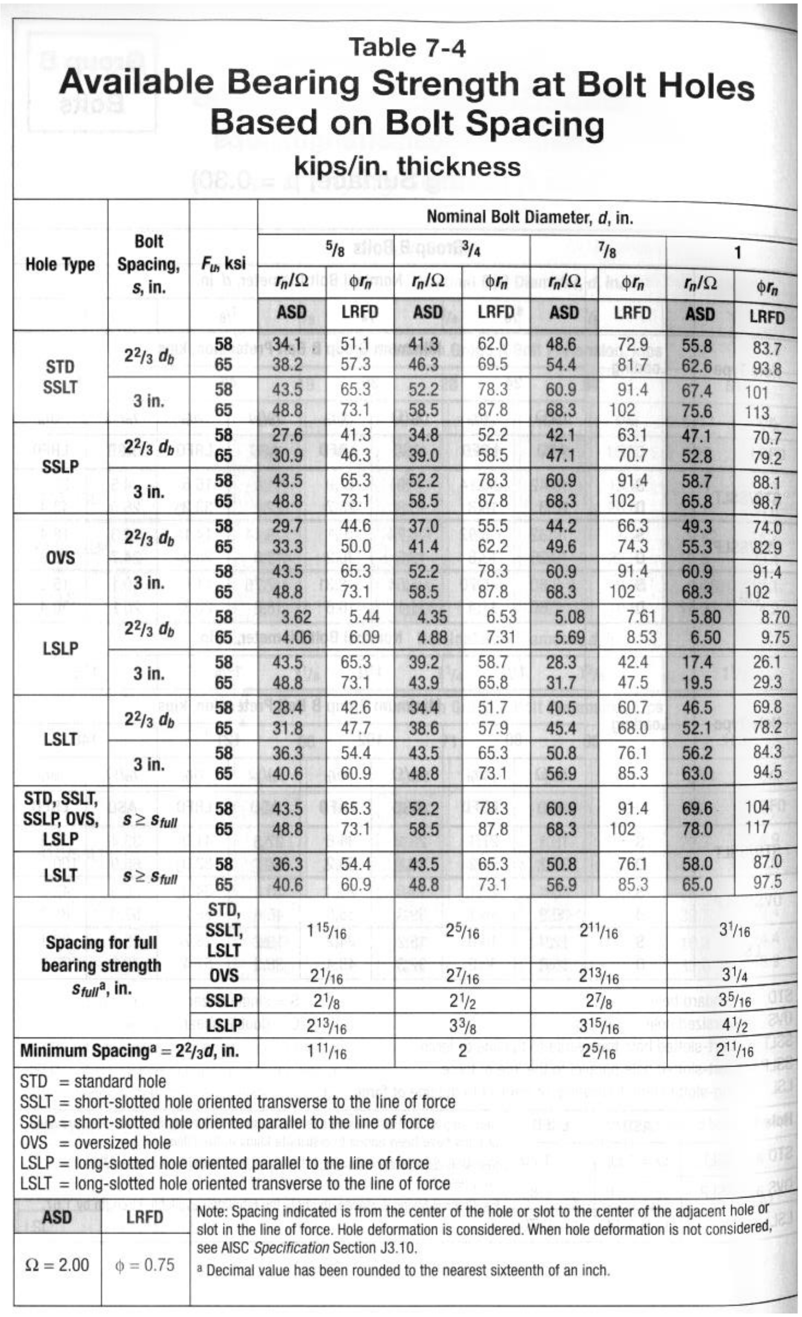


Table 7-4
Available Bearing Strength at Bolt Holes Based on Bolt Spacing
kips/in. thickness

Hole Type	Bolt Spacing, s, in.	F_u, ksi	Nominal Bolt Diameter, d, in.							
			5/8		3/4		7/8		1	
			r_n/Ω	ϕr_n	r_n/Ω	ϕr_n	r_n/Ω	ϕr_n	r_n/Ω	ϕr_n
			ASD	LRFD	ASD	LRFD	ASD	LRFD	ASD	LRFD
STD SSLT	$2^2/_3\ d_b$	58	34.1	51.1	41.3	62.0	48.6	72.9	55.8	83.7
		65	38.2	57.3	46.3	69.5	54.4	81.7	62.6	93.8
	3 in.	58	43.5	65.3	52.2	78.3	60.9	91.4	67.4	101
		65	48.8	73.1	58.5	87.8	68.3	102	75.6	113
SSLP	$2^2/_3\ d_b$	58	27.6	41.3	34.8	52.2	42.1	63.1	47.1	70.7
		65	30.9	46.3	39.0	58.5	47.1	70.7	52.8	79.2
	3 in.	58	43.5	65.3	52.2	78.3	60.9	91.4	58.7	88.1
		65	48.8	73.1	58.5	87.8	68.3	102	65.8	98.7
OVS	$2^2/_3\ d_b$	58	29.7	44.6	37.0	55.5	44.2	66.3	49.3	74.0
		65	33.3	50.0	41.4	62.2	49.6	74.3	55.3	82.9
	3 in.	58	43.5	65.3	52.2	78.3	60.9	91.4	60.9	91.4
		65	48.8	73.1	58.5	87.8	68.3	102	68.3	102
LSLP	$2^2/_3\ d_b$	58	3.62	5.44	4.35	6.53	5.08	7.61	5.80	8.70
		65	4.06	6.09	4.88	7.31	5.69	8.53	6.50	9.75
	3 in.	58	43.5	65.3	39.2	58.7	28.3	42.4	17.4	26.1
		65	48.8	73.1	43.9	65.8	31.7	47.5	19.5	29.3
LSLT	$2^2/_3\ d_b$	58	28.4	42.6	34.4	51.7	40.5	60.7	46.5	69.8
		65	31.8	47.7	38.6	57.9	45.4	68.0	52.1	78.2
	3 in.	58	36.3	54.4	43.5	65.3	50.8	76.1	56.2	84.3
		65	40.6	60.9	48.8	73.1	56.9	85.3	63.0	94.5
STD, SSLT, SSLP, OVS, LSLP	$s \geq s_{full}$	58	43.5	65.3	52.2	78.3	60.9	91.4	69.6	104
		65	48.8	73.1	58.5	87.8	68.3	102	78.0	117
LSLT	$s \geq s_{full}$	58	36.3	54.4	43.5	65.3	50.8	76.1	58.0	87.0
		65	40.6	60.9	48.8	73.1	56.9	85.3	65.0	97.5
Spacing for full bearing strength s_{full}[a], in.		STD, SSLT, LSLT	$1^{15}/_{16}$		$2^5/_{16}$		$2^{11}/_{16}$		$3^1/_{16}$	
		OVS	$2^1/_{16}$		$2^7/_{16}$		$2^{13}/_{16}$		$3^1/_4$	
		SSLP	$2^1/_8$		$2^1/_2$		$2^7/_8$		$3^5/_{16}$	
		LSLP	$2^{13}/_{16}$		$3^3/_8$		$3^{15}/_{16}$		$4^1/_2$	
Minimum Spacing[a] = $2^2/_3 d$, in.			$1^{11}/_{16}$		2		$2^5/_{16}$		$2^{11}/_{16}$	

STD = standard hole
SSLT = short-slotted hole oriented transverse to the line of force
SSLP = short-slotted hole oriented parallel to the line of force
OVS = oversized hole
LSLP = long-slotted hole oriented parallel to the line of force
LSLT = long-slotted hole oriented transverse to the line of force

ASD	LRFD	Note: Spacing indicated is from the center of the hole or slot to the center of the adjacent hole or slot in the line of force. Hole deformation is considered. When hole deformation is not considered, see AISC *Specification* Section J3.10. [a] Decimal value has been rounded to the nearest sixteenth of an inch.
$\Omega = 2.00$	$\phi = 0.75$	

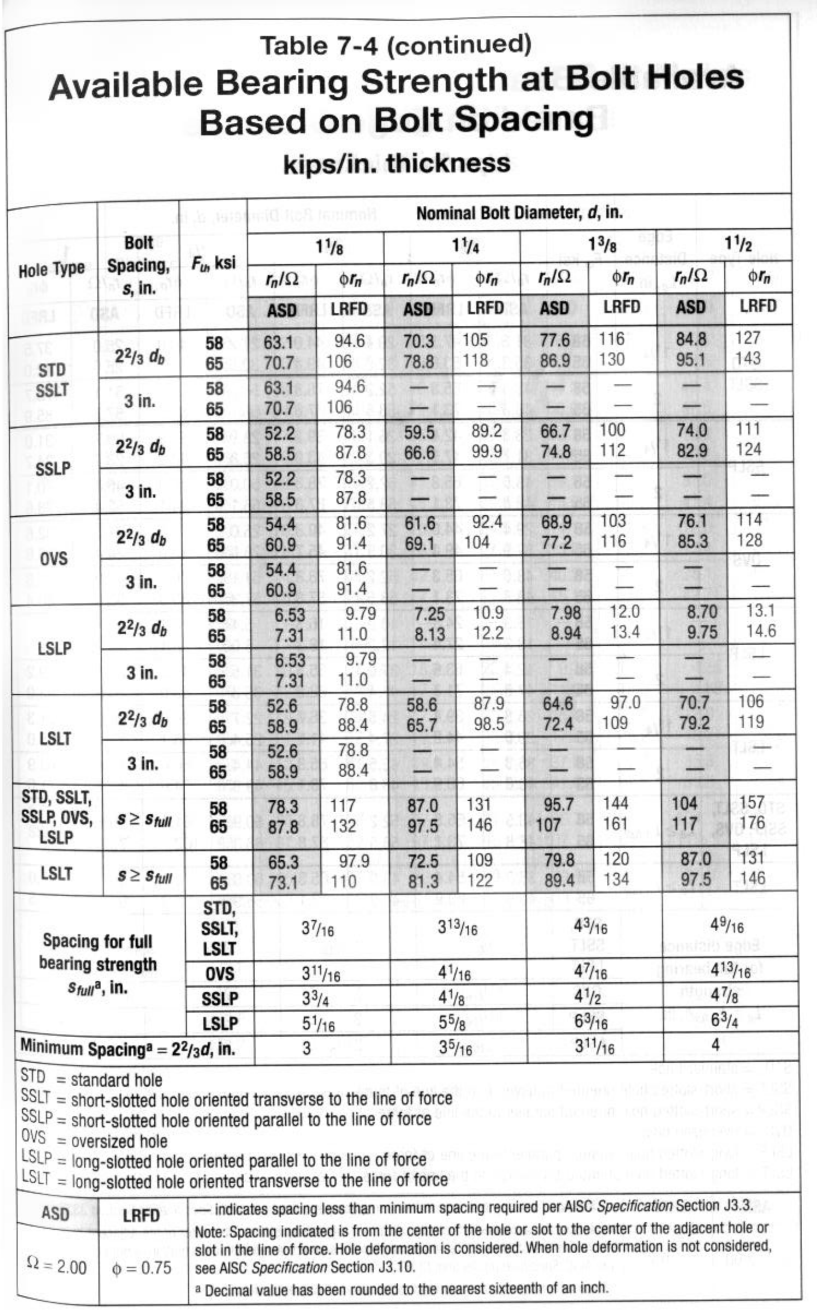


Table 7-4 (continued)
Available Bearing Strength at Bolt Holes Based on Bolt Spacing
kips/in. thickness

Hole Type	Bolt Spacing, s, in.	F_u, ksi	Nominal Bolt Diameter, d, in.							
			$1^1/_8$		$1^1/_4$		$1^3/_8$		$1^1/_2$	
			r_n/Ω	ϕr_n	r_n/Ω	ϕr_n	r_n/Ω	ϕr_n	r_n/Ω	ϕr_n
			ASD	LRFD	ASD	LRFD	ASD	LRFD	ASD	LRFD
STD SSLT	$2^2/_3\ d_b$	58	63.1	94.6	70.3	105	77.6	116	84.8	127
		65	70.7	106	78.8	118	86.9	130	95.1	143
	3 in.	58	63.1	94.6	—	—	—	—	—	—
		65	70.7	106	—	—	—	—	—	—
SSLP	$2^2/_3\ d_b$	58	52.2	78.3	59.5	89.2	66.7	100	74.0	111
		65	58.5	87.8	66.6	99.9	74.8	112	82.9	124
	3 in.	58	52.2	78.3	—	—	—	—	—	—
		65	58.5	87.8	—	—	—	—	—	—
OVS	$2^2/_3\ d_b$	58	54.4	81.6	61.6	92.4	68.9	103	76.1	114
		65	60.9	91.4	69.1	104	77.2	116	85.3	128
	3 in.	58	54.4	81.6	—	—	—	—	—	—
		65	60.9	91.4	—	—	—	—	—	—
LSLP	$2^2/_3\ d_b$	58	6.53	9.79	7.25	10.9	7.98	12.0	8.70	13.1
		65	7.31	11.0	8.13	12.2	8.94	13.4	9.75	14.6
	3 in.	58	6.53	9.79	—	—	—	—	—	—
		65	7.31	11.0	—	—	—	—	—	—
LSLT	$2^2/_3\ d_b$	58	52.6	78.8	58.6	87.9	64.6	97.0	70.7	106
		65	58.9	88.4	65.7	98.5	72.4	109	79.2	119
	3 in.	58	52.6	78.8	—	—	—	—	—	—
		65	58.9	88.4	—	—	—	—	—	—
STD, SSLT, SSLP, OVS, LSLP	$s \geq s_{full}$	58	78.3	117	87.0	131	95.7	144	104	157
		65	87.8	132	97.5	146	107	161	117	176
LSLT	$s \geq s_{full}$	58	65.3	97.9	72.5	109	79.8	120	87.0	131
		65	73.1	110	81.3	122	89.4	134	97.5	146
Spacing for full bearing strength s_{full}[a], in.		STD, SSLT, LSLT	$3^7/_{16}$		$3^{13}/_{16}$		$4^3/_{16}$		$4^9/_{16}$	
		OVS	$3^{11}/_{16}$		$4^1/_{16}$		$4^7/_{16}$		$4^{13}/_{16}$	
		SSLP	$3^3/_4$		$4^1/_8$		$4^1/_2$		$4^7/_8$	
		LSLP	$5^1/_{16}$		$5^5/_8$		$6^3/_{16}$		$6^3/_4$	
Minimum Spacing[a] = $2^2/_3 d$, in.			3		$3^5/_{16}$		$3^{11}/_{16}$		4	

STD = standard hole
SSLT = short-slotted hole oriented transverse to the line of force
SSLP = short-slotted hole oriented parallel to the line of force
OVS = oversized hole
LSLP = long-slotted hole oriented parallel to the line of force
LSLT = long-slotted hole oriented transverse to the line of force

ASD	LRFD	— indicates spacing less than minimum spacing required per AISC *Specification* Section J3.3. Note: Spacing indicated is from the center of the hole or slot to the center of the adjacent hole or slot in the line of force. Hole deformation is considered. When hole deformation is not considered, see AISC *Specification* Section J3.10. [a] Decimal value has been rounded to the nearest sixteenth of an inch.
$\Omega = 2.00$	$\phi = 0.75$	

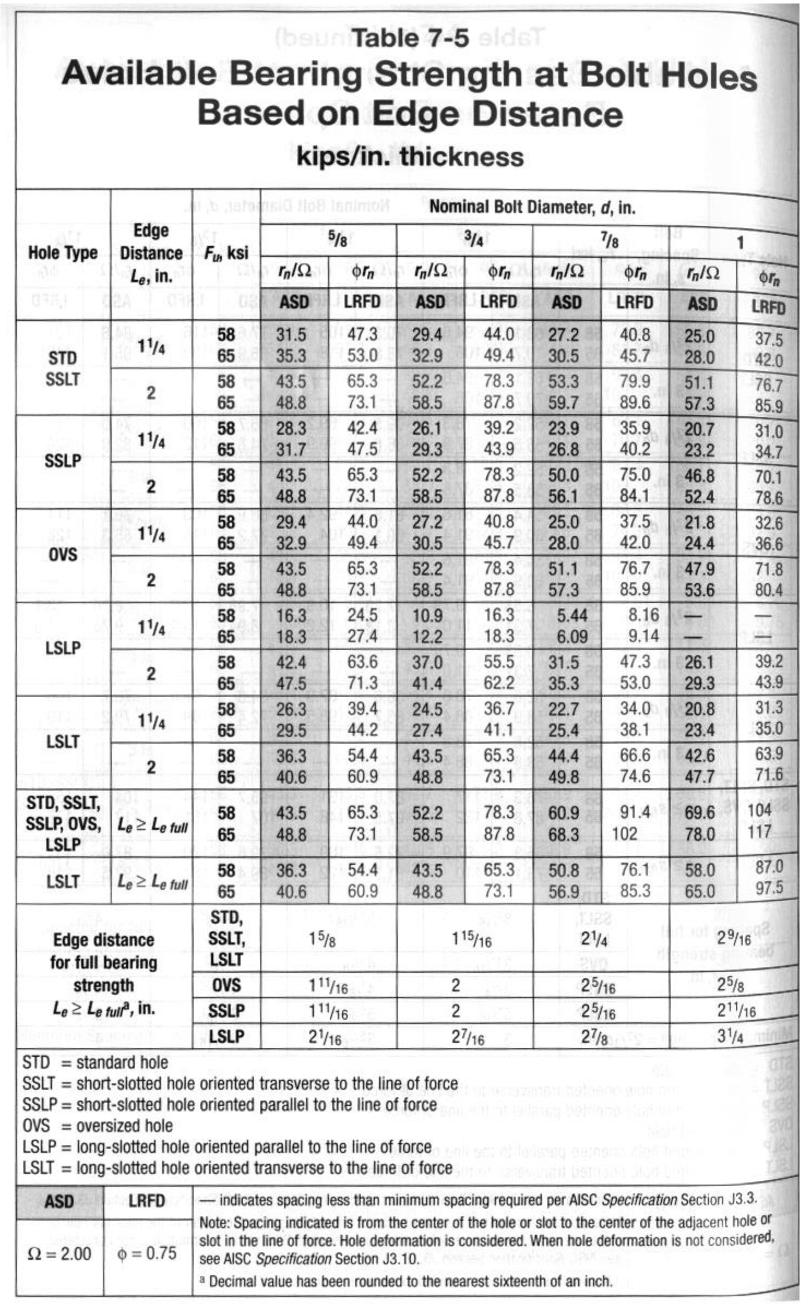


Table 7-5

Available Bearing Strength at Bolt Holes Based on Edge Distance

kips/in. thickness

Hole Type	Edge Distance L_e, in.	F_u, ksi	Nominal Bolt Diameter, d, in.							
			5/8		3/4		7/8		1	
			r_n/Ω	ϕr_n	r_n/Ω	ϕr_n	r_n/Ω	ϕr_n	r_n/Ω	ϕr_n
			ASD	LRFD	ASD	LRFD	ASD	LRFD	ASD	LRFD
STD SSLT	1 1/4	58	31.5	47.3	29.4	44.0	27.2	40.8	25.0	37.5
		65	35.3	53.0	32.9	49.4	30.5	45.7	28.0	42.0
	2	58	43.5	65.3	52.2	78.3	53.3	79.9	51.1	76.7
		65	48.8	73.1	58.5	87.8	59.7	89.6	57.3	85.9
SSLP	1 1/4	58	28.3	42.4	26.1	39.2	23.9	35.9	20.7	31.0
		65	31.7	47.5	29.3	43.9	26.8	40.2	23.2	34.7
	2	58	43.5	65.3	52.2	78.3	50.0	75.0	46.8	70.1
		65	48.8	73.1	58.5	87.8	56.1	84.1	52.4	78.6
OVS	1 1/4	58	29.4	44.0	27.2	40.8	25.0	37.5	21.8	32.6
		65	32.9	49.4	30.5	45.7	28.0	42.0	24.4	36.6
	2	58	43.5	65.3	52.2	78.3	51.1	76.7	47.9	71.8
		65	48.8	73.1	58.5	87.8	57.3	85.9	53.6	80.4
LSLP	1 1/4	58	16.3	24.5	10.9	16.3	5.44	8.16	—	—
		65	18.3	27.4	12.2	18.3	6.09	9.14	—	—
	2	58	42.4	63.6	37.0	55.5	31.5	47.3	26.1	39.2
		65	47.5	71.3	41.4	62.2	35.3	53.0	29.3	43.9
LSLT	1 1/4	58	26.3	39.4	24.5	36.7	22.7	34.0	20.8	31.3
		65	29.5	44.2	27.4	41.1	25.4	38.1	23.4	35.0
	2	58	36.3	54.4	43.5	65.3	44.4	66.6	42.6	63.9
		65	40.6	60.9	48.8	73.1	49.8	74.6	47.7	71.6
STD, SSLT, SSLP, OVS, LSLP	$L_e \geq L_{e\,full}$	58	43.5	65.3	52.2	78.3	60.9	91.4	69.6	104
		65	48.8	73.1	58.5	87.8	68.3	102	78.0	117
LSLT	$L_e \geq L_{e\,full}$	58	36.3	54.4	43.5	65.3	50.8	76.1	58.0	87.0
		65	40.6	60.9	48.8	73.1	56.9	85.3	65.0	97.5
Edge distance for full bearing strength $L_e \geq L_{e\,full}$[a], in.		STD, SSLT, LSLT	1 5/8		1 15/16		2 1/4		2 9/16	
		OVS	1 11/16		2		2 5/16		2 5/8	
		SSLP	1 11/16		2		2 5/16		2 11/16	
		LSLP	2 1/16		2 7/16		2 7/8		3 1/4	

STD = standard hole
SSLT = short-slotted hole oriented transverse to the line of force
SSLP = short-slotted hole oriented parallel to the line of force
OVS = oversized hole
LSLP = long-slotted hole oriented parallel to the line of force
LSLT = long-slotted hole oriented transverse to the line of force

ASD	LRFD	— indicates spacing less than minimum spacing required per AISC *Specification* Section J3.3.
$\Omega = 2.00$	$\phi = 0.75$	Note: Spacing indicated is from the center of the hole or slot to the center of the adjacent hole or slot in the line of force. Hole deformation is considered. When hole deformation is not considered, see AISC *Specification* Section J3.10. [a] Decimal value has been rounded to the nearest sixteenth of an inch.

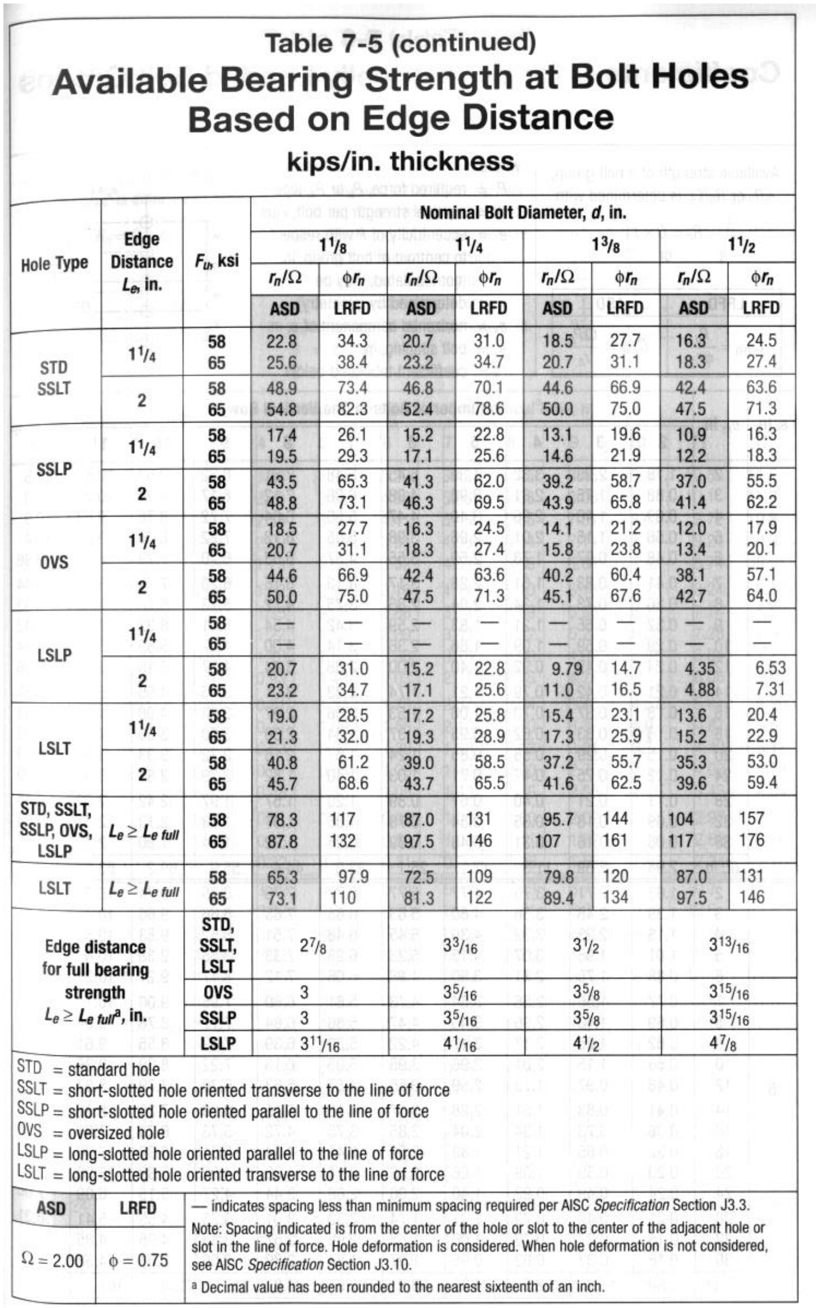


Table 7-5 (continued)

Available Bearing Strength at Bolt Holes Based on Edge Distance

kips/in. thickness

Hole Type	Edge Distance L_e, in.	F_u, ksi	Nominal Bolt Diameter, d, in.							
			1 1/8		1 1/4		1 3/8		1 1/2	
			r_n/Ω	ϕr_n	r_n/Ω	ϕr_n	r_n/Ω	ϕr_n	r_n/Ω	ϕr_n
			ASD	LRFD	ASD	LRFD	ASD	LRFD	ASD	LRFD
STD SSLT	1 1/4	58	22.8	34.3	20.7	31.0	18.5	27.7	16.3	24.5
		65	25.6	38.4	23.2	34.7	20.7	31.1	18.3	27.4
	2	58	48.9	73.4	46.8	70.1	44.6	66.9	42.4	63.6
		65	54.8	82.3	52.4	78.6	50.0	75.0	47.5	71.3
SSLP	1 1/4	58	17.4	26.1	15.2	22.8	13.1	19.6	10.9	16.3
		65	19.5	29.3	17.1	25.6	14.6	21.9	12.2	18.3
	2	58	43.5	65.3	41.3	62.0	39.2	58.7	37.0	55.5
		65	48.8	73.1	46.3	69.5	43.9	65.8	41.4	62.2
OVS	1 1/4	58	18.5	27.7	16.3	24.5	14.1	21.2	12.0	17.9
		65	20.7	31.1	18.3	27.4	15.8	23.8	13.4	20.1
	2	58	44.6	66.9	42.4	63.6	40.2	60.4	38.1	57.1
		65	50.0	75.0	47.5	71.3	45.1	67.6	42.7	64.0
LSLP	1 1/4	58	—	—	—	—	—	—	—	—
		65	—	—	—	—	—	—	—	—
	2	58	20.7	31.0	15.2	22.8	9.79	14.7	4.35	6.53
		65	23.2	34.7	17.1	25.6	11.0	16.5	4.88	7.31
LSLT	1 1/4	58	19.0	28.5	17.2	25.8	15.4	23.1	13.6	20.4
		65	21.3	32.0	19.3	28.9	17.3	25.9	15.2	22.9
	2	58	40.8	61.2	39.0	58.5	37.2	55.7	35.3	53.0
		65	45.7	68.6	43.7	65.5	41.6	62.5	39.6	59.4
STD, SSLT, SSLP, OVS, LSLP	$L_e \geq L_{e\,full}$	58	78.3	117	87.0	131	95.7	144	104	157
		65	87.8	132	97.5	146	107	161	117	176
LSLT	$L_e \geq L_{e\,full}$	58	65.3	97.9	72.5	109	79.8	120	87.0	131
		65	73.1	110	81.3	122	89.4	134	97.5	146
Edge distance for full bearing strength $L_e \geq L_{e\,full}$[a], in.		STD, SSLT, LSLT	2 7/8		3 3/16		3 1/2		3 13/16	
		OVS	3		3 5/16		3 5/8		3 15/16	
		SSLP	3		3 5/16		3 5/8		3 15/16	
		LSLP	3 11/16		4 1/16		4 1/2		4 7/8	

STD = standard hole
SSLT = short-slotted hole oriented transverse to the line of force
SSLP = short-slotted hole oriented parallel to the line of force
OVS = oversized hole
LSLP = long-slotted hole oriented parallel to the line of force
LSLT = long-slotted hole oriented transverse to the line of force

ASD	LRFD	— indicates spacing less than minimum spacing required per AISC *Specification* Section J3.3.
$\Omega = 2.00$	$\phi = 0.75$	Note: Spacing indicated is from the center of the hole or slot to the center of the adjacent hole or slot in the line of force. Hole deformation is considered. When hole deformation is not considered, see AISC *Specification* Section J3.10. [a] Decimal value has been rounded to the nearest sixteenth of an inch.