ARCHITECTURAL STRUCTURES:
FORM, BEHAVIOR, AND DESIGN
ARCH 331
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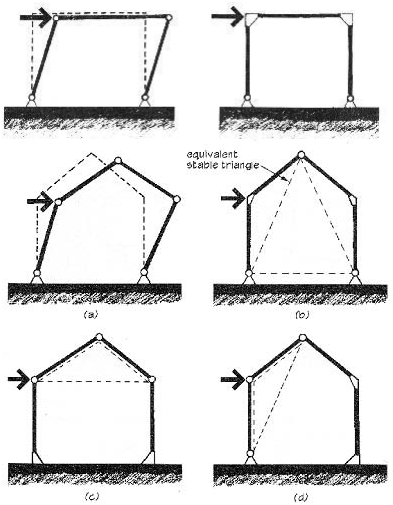
SUMMER 2013

lecture
ten

rigid frames: compression & buckling

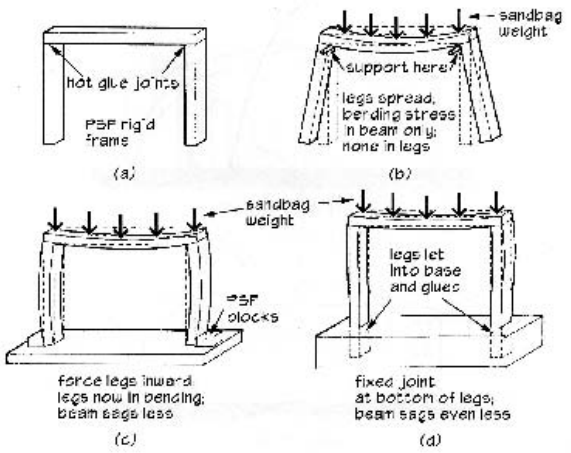
Rigid Frames

- *rigid frames have no pins*
- *frame is all one body*
- *joints transfer moments and shear*
- *typically statically indeterminate*
- *types*
  - *portal*
  - *gable*



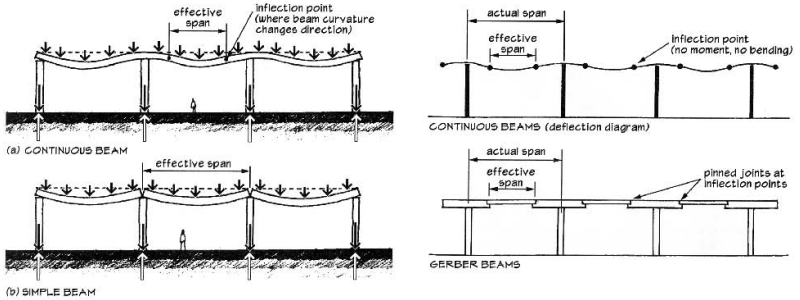
Rigid Frames

- *behavior*



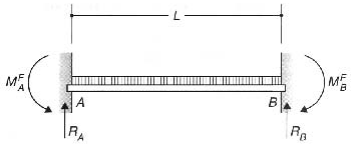
Rigid Frames

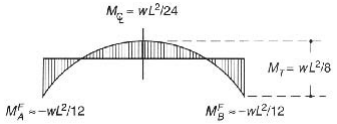
- *moments get redistributed*
- *deflections are smaller*
- *effective column lengths are shorter*
- *very sensitive to settling*



Moment Redistribution

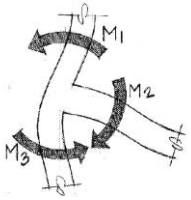
- *continuous slabs & beams with uniform loading*
  - *joints similar to fixed ends, but can rotate*
- *change in moment to center =* $\frac{wL^2}{8}$
  - *M_{max} for simply supported beam*





Rigid Frames

- *resists lateral loadings*
- *shape depends on stiffness of beams and columns*
- *90° maintained*



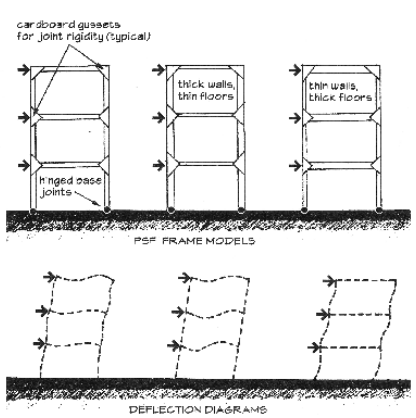
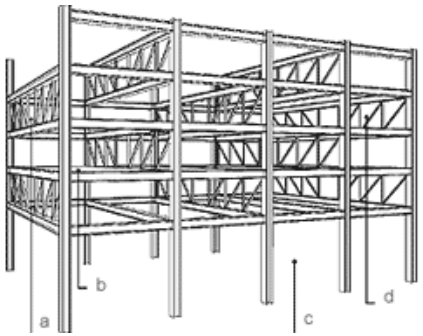


Figure 9.19: Model demonstration of the effects of varying the stiffness of beams and columns when a building frame is subjected to lateral loads.

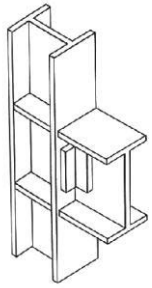
Rigid Frames

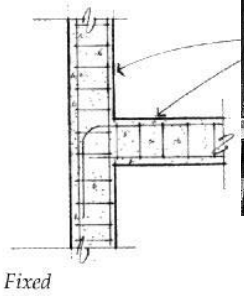
- *staggered truss*
  - *rigidity*
  - *clear stories*



Rigid Frames

- *connections*
  - *steel*
  - *concrete*





http:// nisee.berkeley.edu/godden

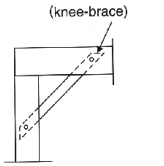
Braced Frames

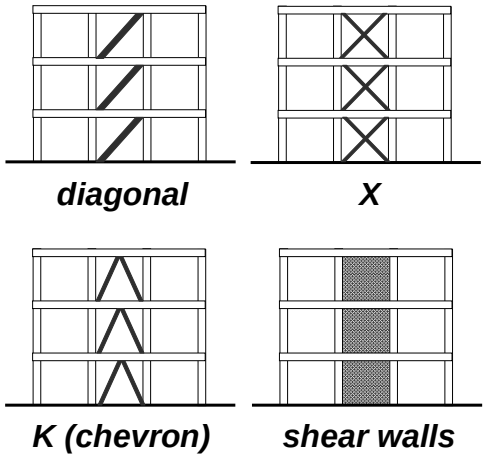
- *pin connections*
- *bracing to prevent lateral movements*

http:// nisee.berkeley.edu/godden

Braced Frames

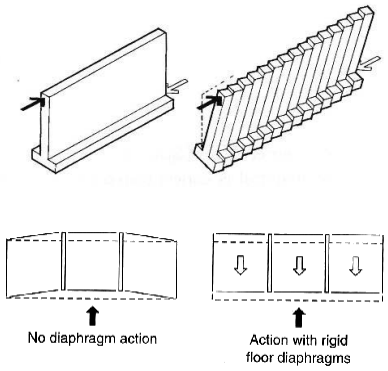
- *types of bracing*
  - *knee-bracing*
  - *diagonal*
  - *X*
  - *K or chevron*
  - *shear walls*

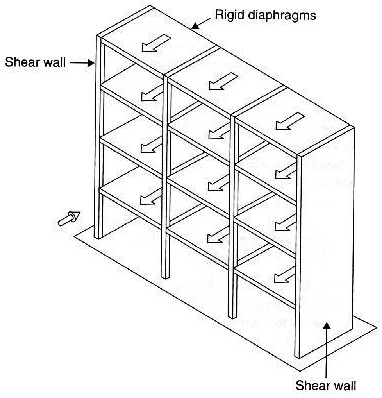




Shear Walls

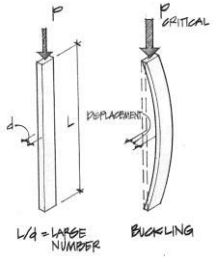
- *resist lateral load in plane with wall*





Compression Members

- *designed for strength & stresses*
- *designed for serviceability & deflection*
- *need to design for <u>stability</u>*
  - *ability to support a specified load without sudden or unacceptable deformations*



Column Buckling

- *axially loaded columns*
- *long & slender*
  - *unstable equilibrium = buckling*
  - *sudden and not good*

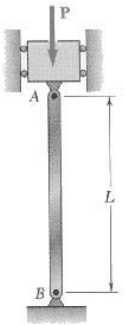
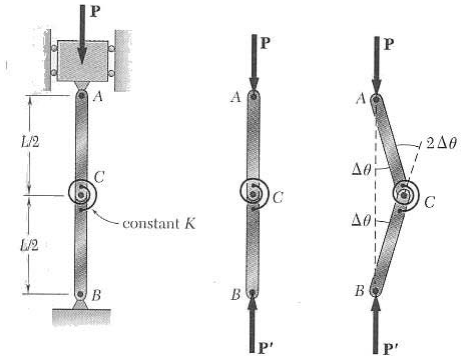


Fig. 10.1

Fig. 10.2

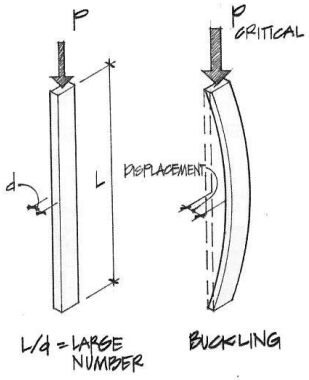
Modeling

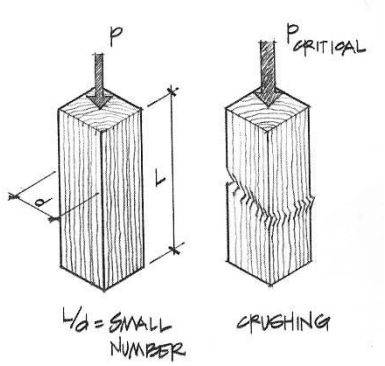
- *can be modeled with a spring at mid-height*
- *when moment from deflection exceeds the spring capacity ... "boing"*
- *critical load P*



Effect of Length

- *long & slender*
- *short & stubby*





Buckling Load

- *related to deflected shape (PΔ)*
- *shape of sine wave*
- *Euler's Formula*
- *smallest I governs*

$$P_{critical} = \frac{\pi^2 EI}{(L)^2}$$

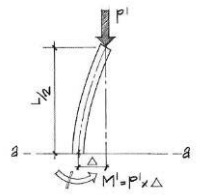


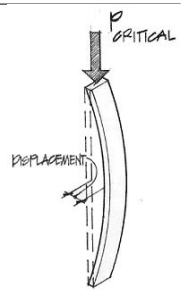

Figure 9.3 Leonhard Euler (1707–1783).

Critical Stress

- *short columns*

$$f_{critical} = \frac{P_{actual}}{A} < F_a$$

- *slenderness ratio = L_e/r (L/d)*
- *radius of gyration =* $r = \sqrt{\frac{I}{A}}$



weak axis

$$f_{critical} = \frac{P_{critical}}{A} = \frac{\pi^2 EAr^2}{A(L_e)^2} = \frac{\pi^2 E}{\left(L_e/r\right)^2} \qquad P_{critical} = \frac{\pi^2 EA}{\left(L_e/r\right)^2}$$

Critical Stresses

- *when a column gets stubby, F_y will limit the load*
- *real world has loads with eccentricity*
- *C_c for steel and allowable stress*

$$L_e/r > C_c = \sqrt{\frac{2\pi^2 E}{F_y}}$$

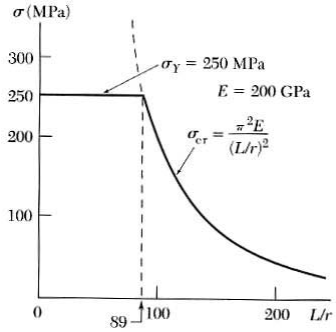
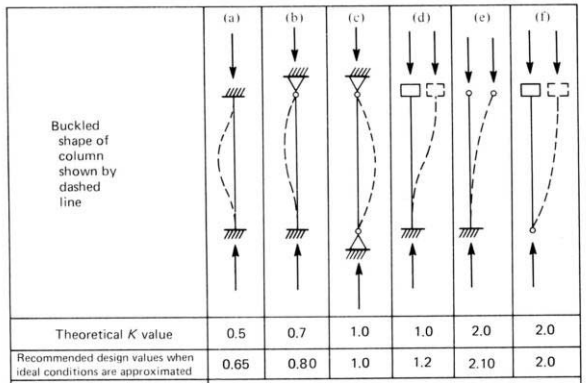


Fig. 10.9

Effective Length

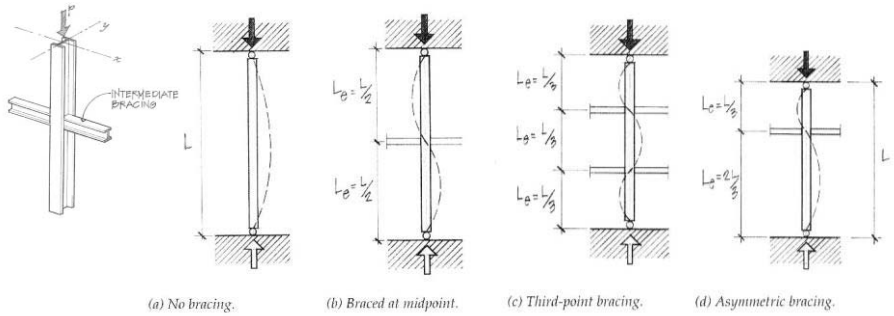
- *end conditions affect shape*
- *effective length factor, K* $L_e = K \cdot L$



Buckled shape of column shown by dashed line	(a)	(b)	(c)	(d)	(e)	(f)
Theoretical K value	0.5	0.7	1.0	1.0	2.0	2.0
Recommended design values when ideal conditions are approximated	0.65	0.80	1.0	1.2	2.10	2.0

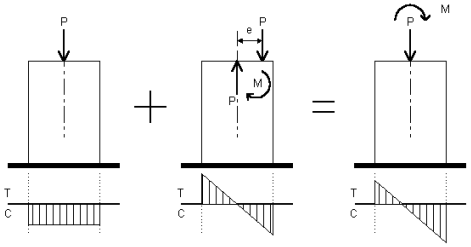
Bracing

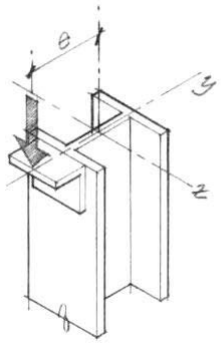
- *bracing affects shape of buckle in one direction*
- *both should be checked!*



Centric & Eccentric Loading

- *centric*
  - *allowable stress from strength or buckling*
- *eccentric*
  - *combined stresses*



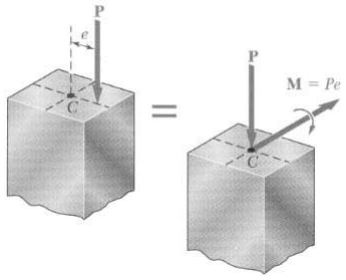


Combined Stresses

- *axial + bending*

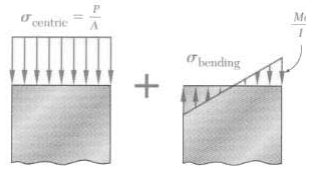
$$f_{\max} = \frac{P}{A} + \frac{Mc}{I}$$

$$M = P \cdot e$$



- *design*

$$f_{\max} \le F_{cr} = \frac{f_{cr}}{F.S.}$$



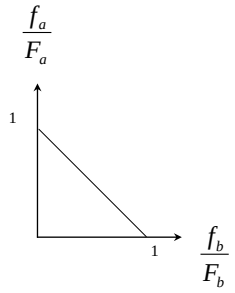
Stress Limit Conditions

- *ASD interaction formula*

$$\frac{f_a}{F_a} + \frac{f_b}{F_b} \le 1.0$$

- *with biaxial bending*

$$\frac{f_a}{F_a} + \frac{f_{bx}}{F_{bx}} + \frac{f_{by}}{F_{by}} \le 1.0$$

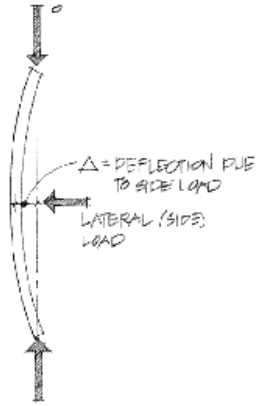


interaction diagram

Stress Limit Conditions

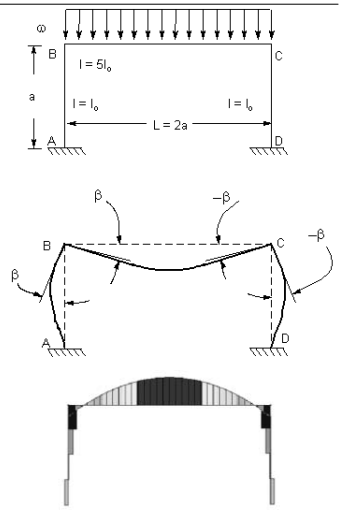
- *in reality, as the column flexes, the moment increases*
- *P-Δ effect*

$$\frac{f_a}{F_a} + \frac{f_b \times (Magnification\ \ factor)}{F_{bx}} \le 1.0$$



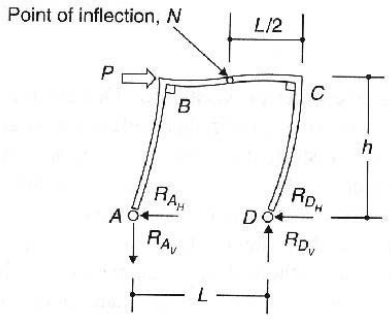
Rigid Frame Analysis

- *members see*
  - *shear*
  - *axial force*
  - *bending*
- *V & M diagrams*
  - *plot on "outside"*



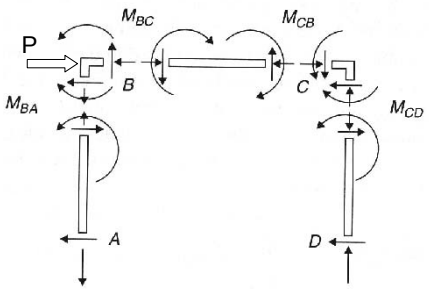
Rigid Frame Analysis

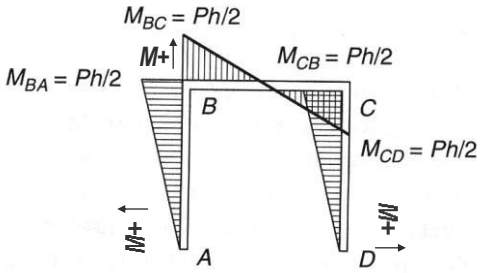
- *need support reactions*
- *free body diagram each member*
- *end reactions are <u>equal and opposite</u> on next member*
- *"turn" member like beam*
- *draw V & M*



Rigid Frame Analysis

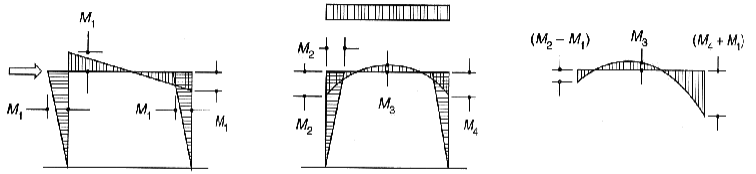
- *FBD & M*
  - *opposite end reactions at joints*





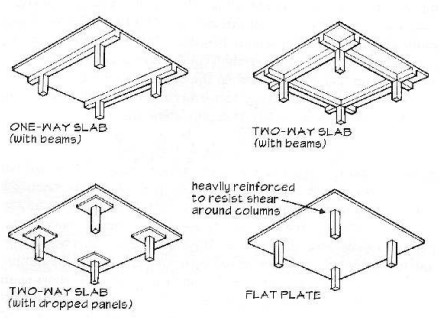
Rigid Frame Design

- *loads and combinations*
  - *usually uniformly distributed gravity loads*
  - *worst case for largest moments...*
  - *wind direction can increase moments*



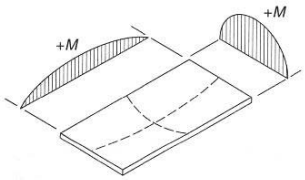
Rigid Frame Design

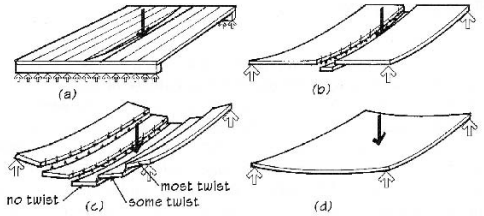
- *frames & floors*
  - *rigid frame can have slab floors or slab with connecting beams*
- *other*
  - *slabs or plates on columns*



Rigid Frame Design

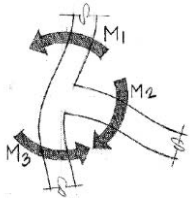
- *floors – plates & slabs*
  - *one-way behavior*
    - *side ratio > 1.5*
    - *"strip" beam*
  - *two-way behavior*
    - *more complex*





Rigid Frame Design

- *columns in frames*
  - *ends can be "flexible"*
  - *stiffness affected by beams <u>and</u> column = EI/L*

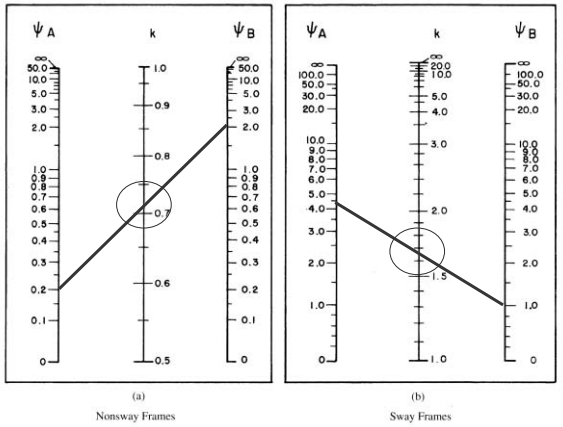


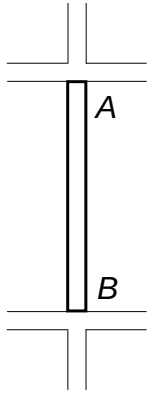
$$G = \Psi = \frac{\Sigma EI/l_c}{\Sigma EI/l_b}$$

  - *for the joint*
    - *l_c is the column length of each column*
    - *l_b is the beam length of each beam*
    - *measured center to center*

Rigid Frame Design

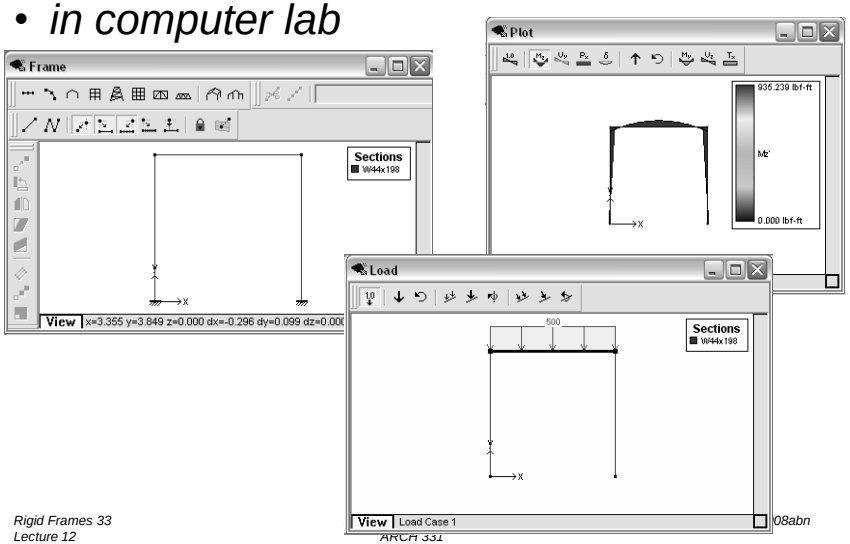
- *column effective length, k*





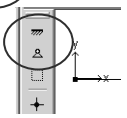
Tools – Multiframe

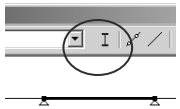
- *in computer lab*

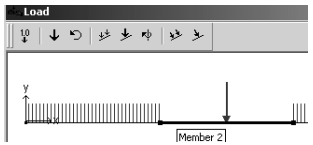


Tools – Multiframe

- *frame window*
  - *define frame members*
    - *or pre-defined frame*
  - *select points, assign supports*
  - *select members, assign <u>section</u>*
  - *load window*
  - *select point or member, add point or distributed loads*

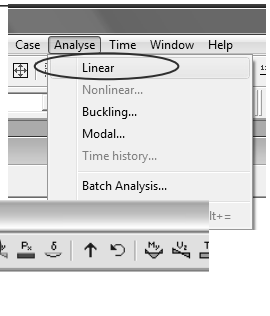


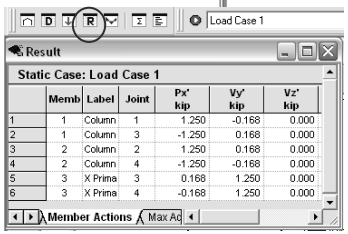




Tools – Multiframe

- *to run analysis choose*
  - *Analyze menu*
    - *Linear*
- *plot*
  - *choose options*
- *results*
  - *choose options*





	Memb	Label	Joint	Px' kip	Vy' kip	Vz' kip
1	1	Column	1	1.250	-0.168	0.000
2	1	Column	3	-1.250	0.168	0.000
3	2	Column	2	1.250	0.168	0.000
4	2	Column	4	-1.250	-0.168	0.000
5	3	X Prima	3	0.168	1.250	0.000
6	3	X Prima	4	-0.168	1.250	0.000