

lecture  
**twenty six**

## **concrete construction: columns & frames**

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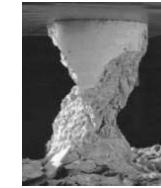
<http://www.building.co.uk>



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## **Concrete in Compression**

- crushing
- vertical cracking
  - tension
- diagonal cracking
  - shear
- $f'_c$



<http://www.bam.de>

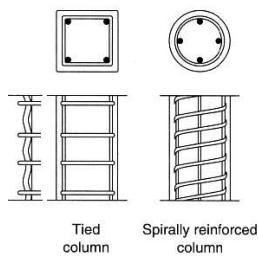
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## **Columns Reinforcement**

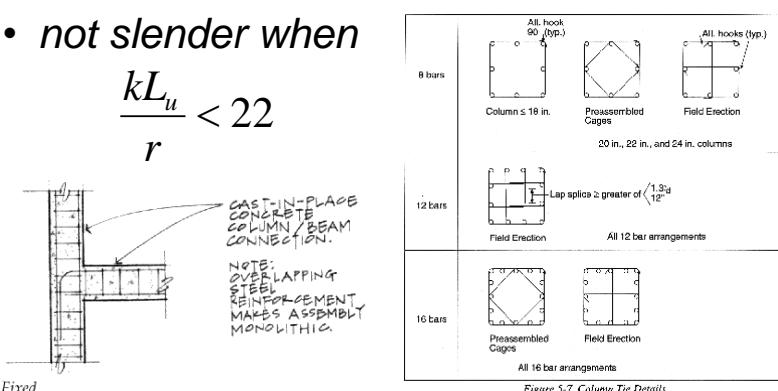
- columns require
  - ties or spiral reinforcement to “confine” concrete (#3 bars minimum)
  - minimum amount of longitudinal steel (#5 bars minimum: 4 with ties, 5 with spiral)



## **Slenderness**

- effective length in monolithic with respect to stiffness of joint:  $\Psi$  &  $k$
- not slender when

$$\frac{kL_u}{r} < 22$$



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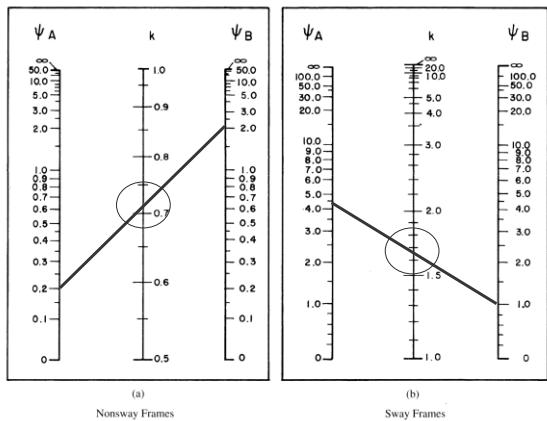
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## Effective Length (revisited)

- relative rotation



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$$\Psi = \frac{\sum EI/l_c}{\sum EI/l_b}$$

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## Column Behavior

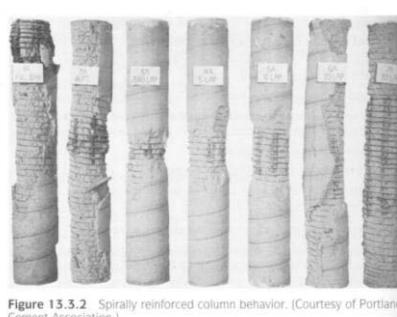


Figure 13.3.2 Spirally reinforced column behavior. (Courtesy of Portland Cement Association.)

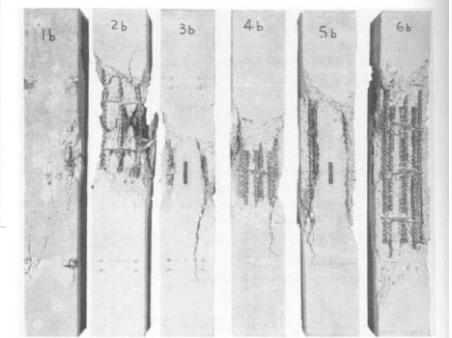


Figure 13.3.3 Tied column behavior. (Courtesy of Portland Cement Association.)

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## Column Design

- $\phi_c = 0.65$  for ties,  $\phi_c = 0.70$  for spirals
- $P_o$  – no bending

$$P_o = 0.85 f'_c (A_g - A_{st}) + f_y A_{st}$$

$$P_u \leq \phi_c P_n$$

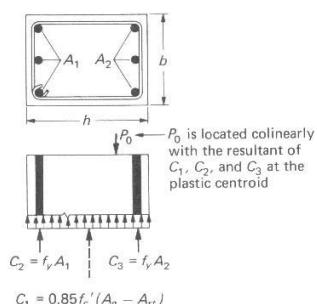
– ties:  $P_n = 0.8P_o$

– spiral:  $P_n = 0.85P_o$

- nominal axial capacity:

– presumes steel yields

– concrete at ultimate stress



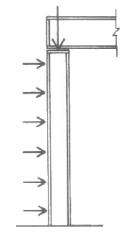
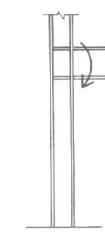
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## Columns with Bending

- eccentric loads can cause moments
- moments can change shape and induce more deflection ( $P-\Delta$ )



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Figure 10.6 Considerations for development of bending in steel columns: (a) bending induced by eccentric load, (b) bending transferred to column in a rigid frame, and (c) combined loading condition, separately producing axial compression and bending.

## Columns with Bending

- for ultimate strength behavior, ultimate strains can't be exceeded
  - concrete 0.003
  - steel  $\frac{f_y}{E_s}$
- $P$  reduces with  $M$

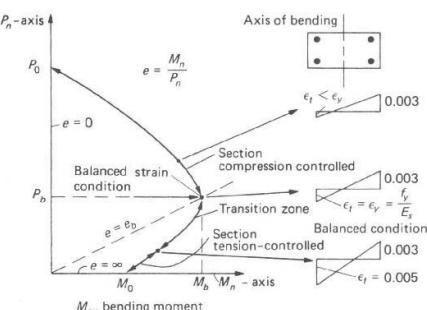


Figure 13.6.1 Typical strength interaction diagram for axial compression and bending moment about one axis. Transition zone is where  $e_y \leq e_t \leq 0.003$ .

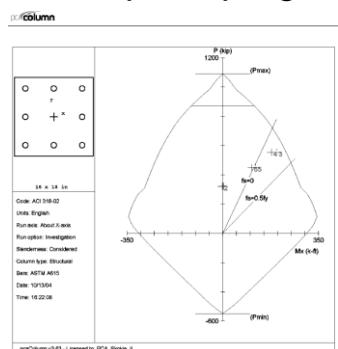
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## Design Methods

- calculation intensive
  - handbook charts
  - computer programs



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## Columns with Bending

- need to consider combined stresses
- linear strain
- steel stress at or below  $f_y$
- plot interaction diagram

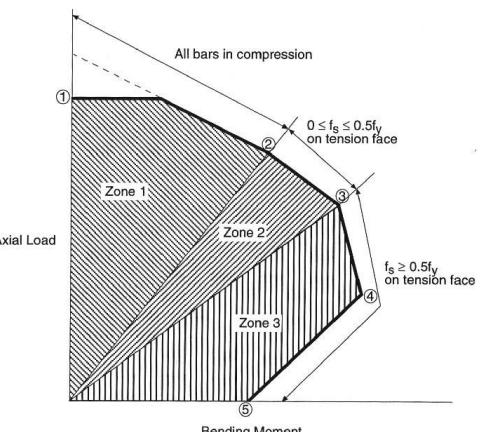


Figure 5-3 Transition Stages on Interaction Diagram

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## Design Considerations

- bending at both ends
  - $P-\Delta$  maximum
- biaxial bending
- walls
  - unit wide columns
  - “deep” beam shear
- detailing
  - shorter development lengths
  - dowels to footings

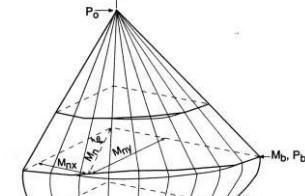
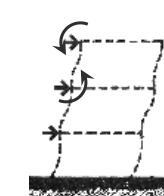
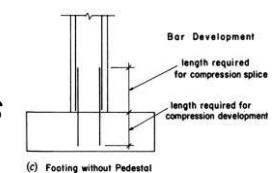


Figure 12-1 Biaxial Interaction Surface



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