

lecture twelve

rigid frames: compression & bending

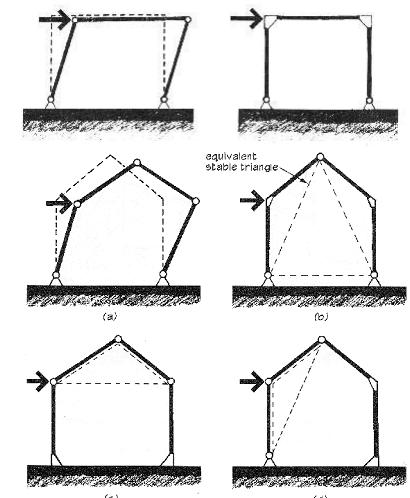
Rigid Frames 1
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Architectural Structures
ARCH 331 <http://nisee.berkeley.edu/godden> F2009abn

Rigid Frames

- rigid frames have no pins
- frame is all one body
- joints transfer moments and shear
- typically statically indeterminate
- types
 - portal
 - gable

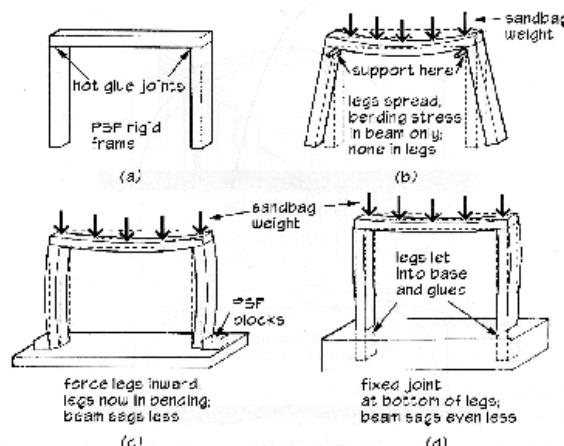


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Rigid Frames

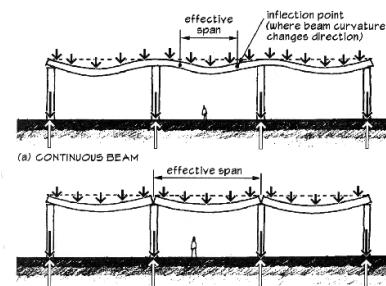
- moments get redistributed
- deflections are smaller
- effective column lengths are shorter
- very sensitive to settling



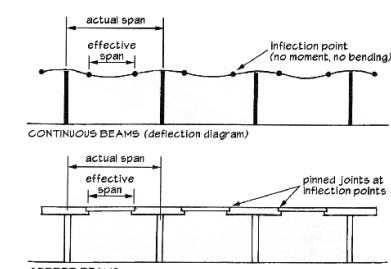
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(a) CONTINUOUS BEAM
(b) SIMPLE BEAM
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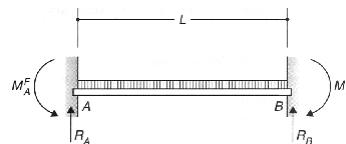


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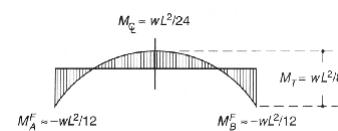
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Moment Redistribution

- continuous slabs & beams with uniform loading
 - joints similar to fixed ends, but can rotate
- change in moment to center = $\frac{wL^2}{8}$
 - M_{max} for simply supported beam



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Rigid Frames

- resists lateral loadings
- shape depends on stiffness of beams and columns
- 90° maintained

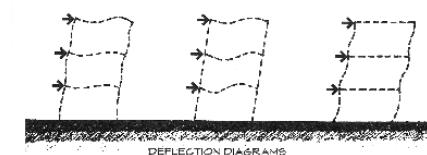
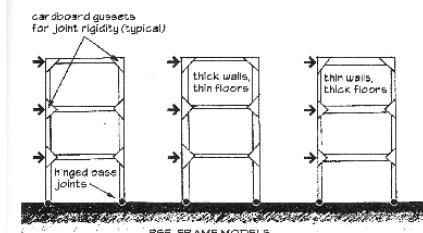
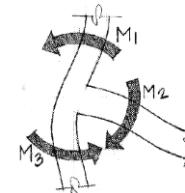


Figure 9.19: Model demonstration of the effects of varying the stiffness of beams and columns when a building frame is subjected to lateral loads.

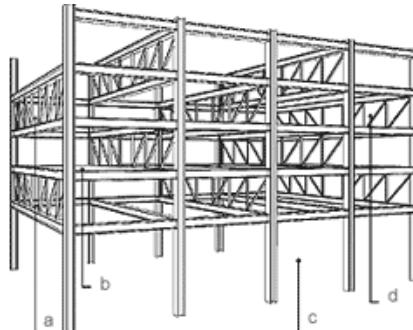
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Rigid Frames

- staggered truss
 - rigidity
 - clear stories



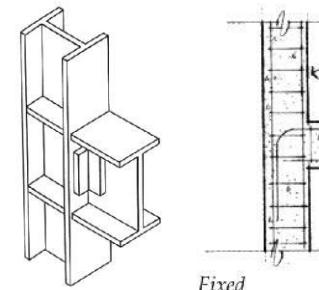
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Rigid Frames

- connections
 - steel
 - concrete



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Braced Frames

- pin connections
- bracing to prevent lateral movements



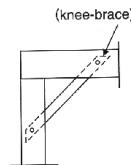
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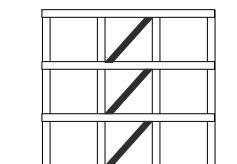
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Braced Frames

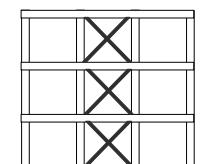
- types of bracing
 - knee-bracing
 - diagonal
 - X
 - K or chevron
 - shear walls



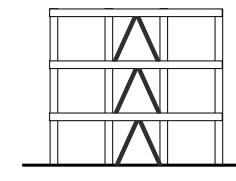
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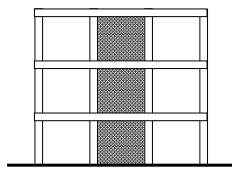
diagonal



X



K (chevron)

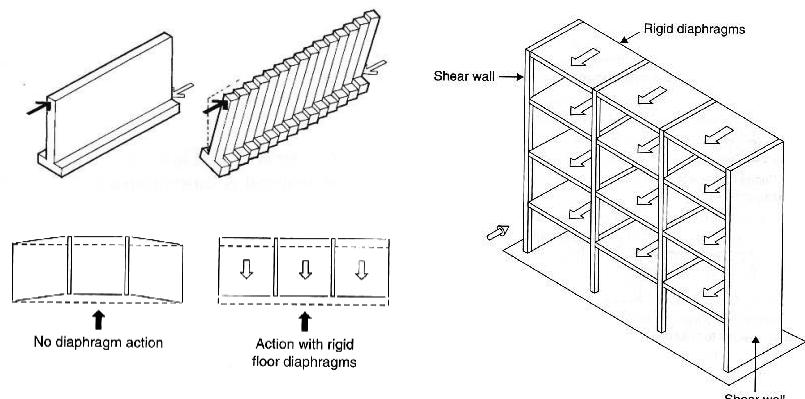


shear walls

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Shear Walls

- resist lateral load *in plane with wall*



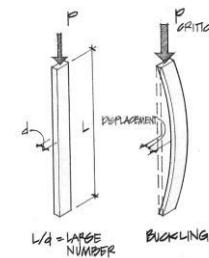
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Compression Members

- designed for strength & stresses
- designed for serviceability & deflection
- need to design for stability
 - ability to support a specified load without sudden or unacceptable deformations



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Column Buckling

- axially loaded columns
- long & slender
 - unstable equilibrium = buckling
 - sudden and not good

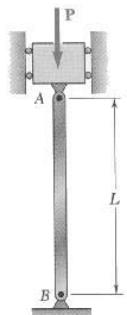


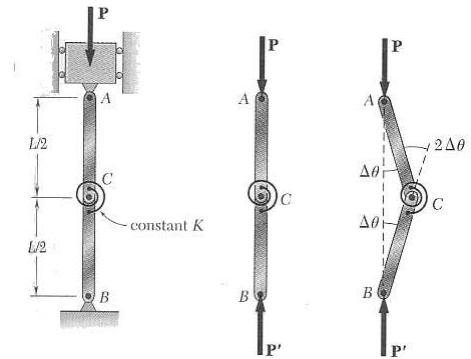
Fig. 10.1



Fig. 10.2

Modeling

- can be modeled with a spring at mid-height
- when moment from deflection exceeds the spring capacity ... “boing”
- critical load P



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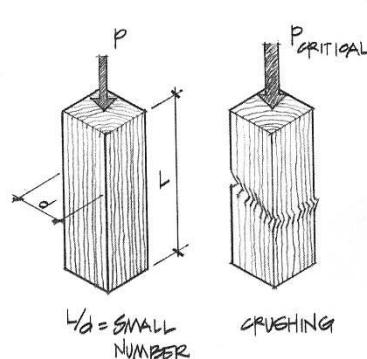
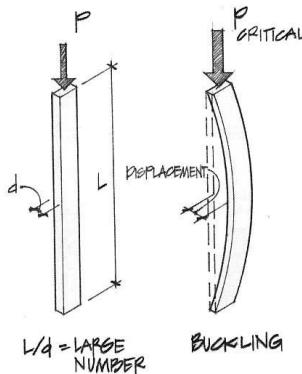
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Effect of Length

- long & slender
- short & stubby



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Buckling Load

- related to deflected shape ($P\Delta$)
- shape of sine wave
- Euler's Formula
- smallest I governs

$$P_{critical} = \frac{\pi^2 EI}{(L)^2}$$

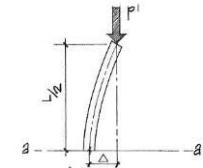


Figure 9.3 Leonhard Euler (1707–1783).

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Critical Stress

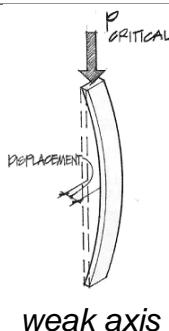
- short columns

$$f_{critical} = \frac{P_{actual}}{A} < F_a$$

- slenderness ratio = L_e/r (L/d)

- radius of gyration = $r = \sqrt{\frac{I}{A}}$

$$f_{critical} = \frac{P_{critical}}{A} = \frac{\pi^2 E A r^2}{A(L_e)^2} = \frac{\pi^2 E}{\left(\frac{L_e}{r}\right)^2}$$



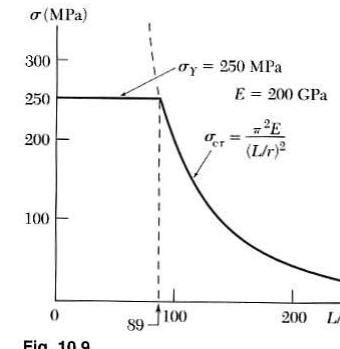
$$P_{critical} = \frac{\pi^2 E A}{\left(\frac{L_e}{r}\right)^2}$$

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Critical Stresses

- when a column gets stubby, F_y will limit the load
- real world has loads with eccentricity
- C_c for steel and allowable stress



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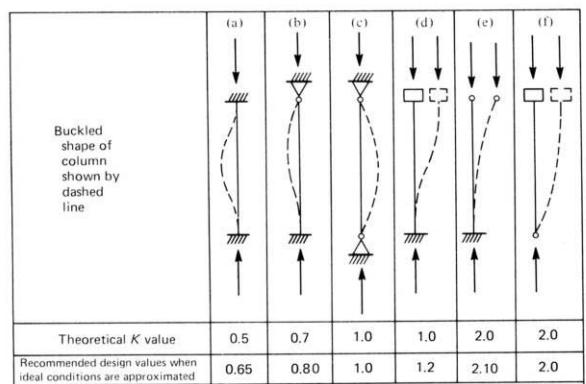
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Effective Length

- end conditions affect shape
- effective length factor, K

$$L_e = K \cdot L$$



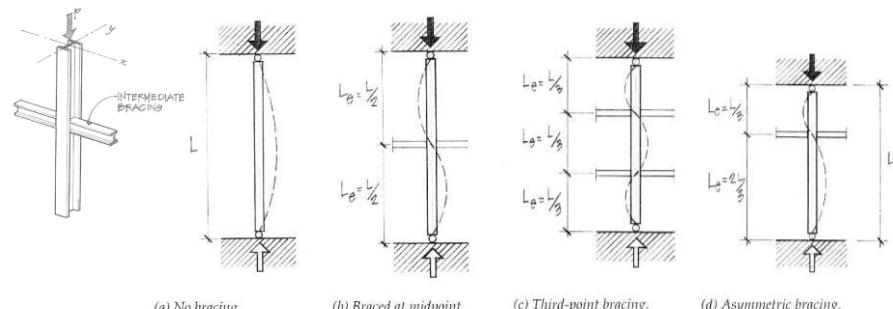
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Bracing

- bracing affects shape of buckle in one direction
- both should be checked!



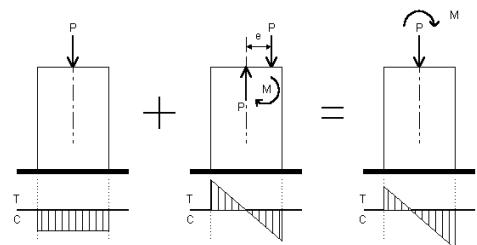
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Centric & Eccentric Loading

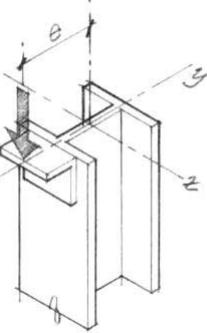
- *centric*
 - allowable stress from strength or buckling
- *eccentric*
 - combined stresses



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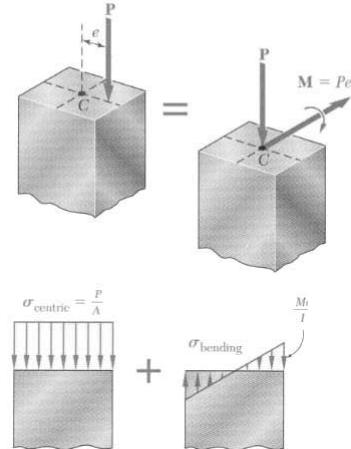
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Combined Stresses

- axial + bending

$$f_{\max} = \frac{P}{A} + \frac{Mc}{I}$$

$$M = P \cdot e$$



- design

$$f_{\max} \leq F_{cr} = \frac{f_{cr}}{F.S.}$$

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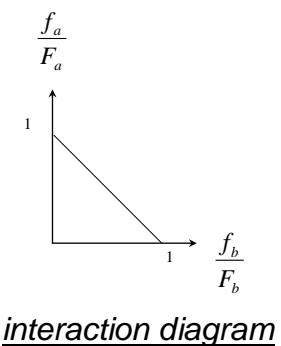
Stress Limit Conditions

- ASD interaction formula

$$\frac{f_a}{F_a} + \frac{f_b}{F_b} \leq 1.0$$

- with biaxial bending

$$\frac{f_a}{F_a} + \frac{f_{bx}}{F_{bx}} + \frac{f_{by}}{F_{by}} \leq 1.0$$



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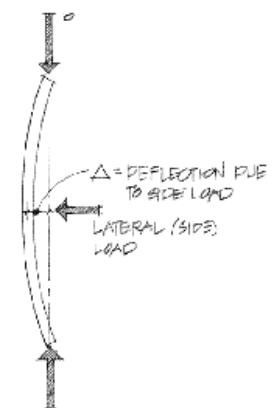
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Stress Limit Conditions

- in reality, as the column flexes, the moment increases

- P-Δ effect

$$\frac{f_a}{F_a} + \frac{f_b \times (\text{Magnification factor})}{F_{bx}} \leq 1.0$$



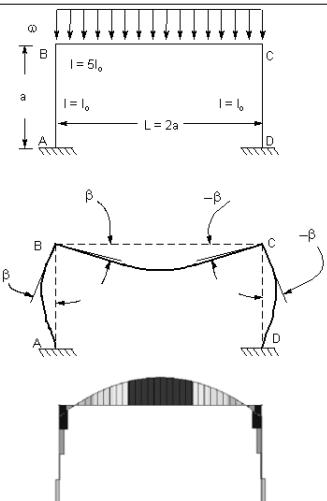
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Rigid Frame Analysis

- members see
 - shear
 - axial force
 - bending
- V & M diagrams
 - plot on “outside”



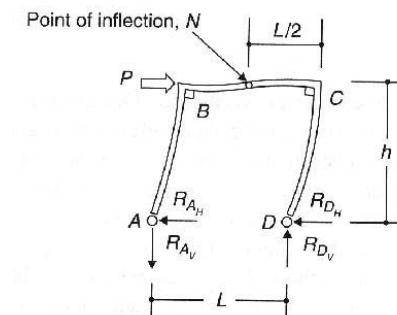
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Rigid Frame Analysis

- need support reactions
- free body diagram each member
- end reactions are equal and opposite on next member
- “turn” member like beam
- draw V & M



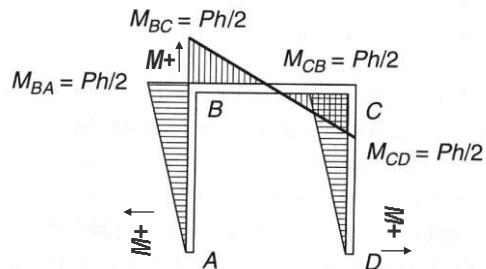
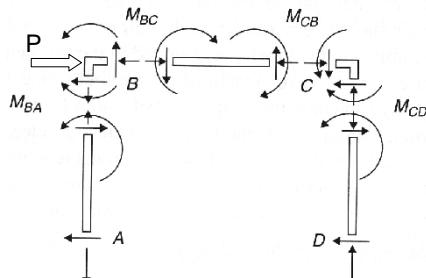
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Rigid Frame Analysis

- FBD & M
- opposite end reactions at joints



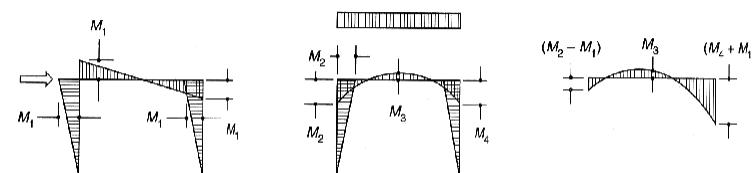
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Rigid Frame Design

- loads and combinations
- usually uniformly distributed gravity loads
- worst case for largest moments...
- wind direction can increase moments



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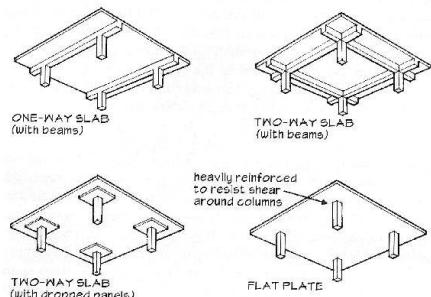
Rigid Frame Design

- frames & floors

- rigid frame can have slab floors or slab with connecting beams

- other

- slabs or plates on columns



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Rigid Frame Design

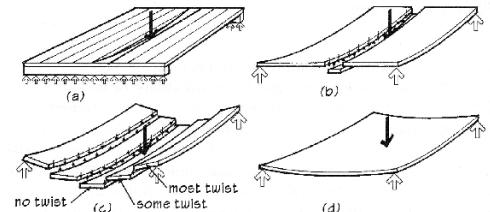
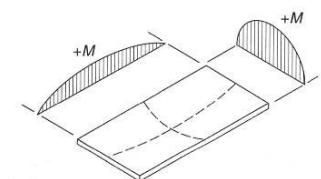
- floors – plates & slabs

- one-way behavior

- side ratio > 1.5
- “strip” beam

- two-way behavior

- more complex



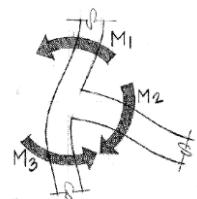
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Rigid Frame Design

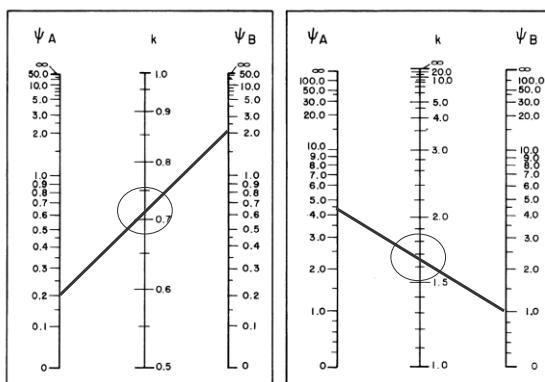
- column effective length, k



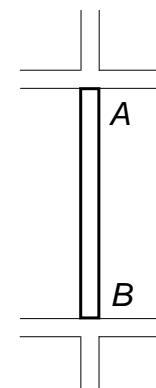
$$G = \Psi = \frac{\sum EI}{l_c}$$

- for the joint

- l_c is the column length of each column
- l_b is the beam length of each beam
- measured center to center



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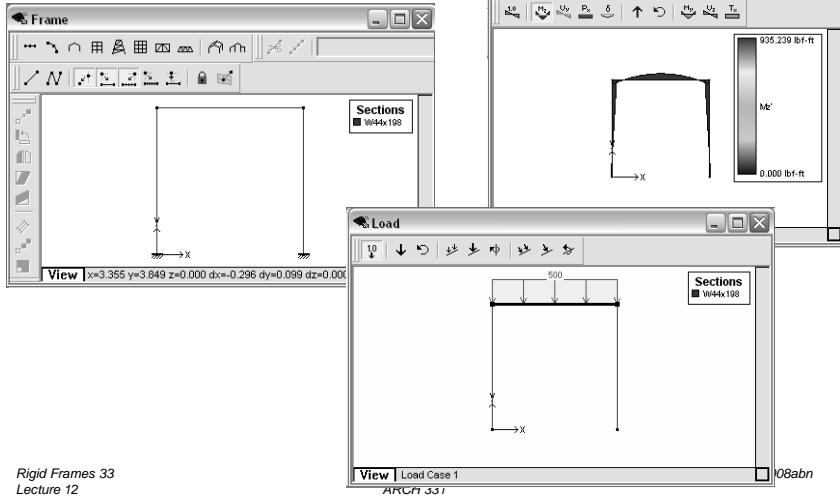
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Tools – Multiframe

- in computer lab



Tools – Multiframe

- frame window

– define frame members

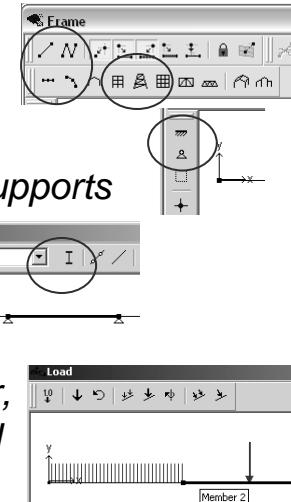
- or pre-defined frame

– select points, assign supports

– select members,
assign section

– load window

– select point or member,
add point or distributed
loads



Tools – Multiframe

- to run analysis choose

- Analyze menu
 - Linear

- plot

- choose options

- results

- choose
options

