## ARCH 331: Practice Quiz 4

Note: No aids are allowed for part 1. One side of a letter sized paper with notes is allowed during part 2, along with a silent, non-programmable calculator. There are reference charts for part 2, shown on pages 2-6.

Clearly show your work and answer.
Part 1) Worth 5 points (conceptual questions)
Part 2) Worth 45 points
(NOTE: The loading type and sizes can and will be changed for the quiz with respect to the beam diagrams and formulas provided. The support condition, section, and bracing for the column can and will be changed.)
Sawn timber beams (like shown in Figure 4a) spaced 4 ft on center are needed to span 16 ft and support a roof having $30 \mathrm{lb} / \mathrm{ft}^{2}$ of dead load and two 2400 lb seven-day roof live loads at 3 feet from each end. The beam is simply supported and fully braced. Idaho White Pine will be used and has the following tabular design values for bending for single member uses and modulus of elasticity:

$$
\mathrm{F}_{\mathrm{b}}=1150 \mathrm{psi}, \mathrm{~F}_{\mathrm{v}}=65 \mathrm{psi}, \mathrm{E}=1.4 \times 10^{6} \mathrm{psi}
$$

a) Including a self weight of $10 \mathrm{lb} / \mathrm{ft}$, design the most economical member for strength (no consideration of serviceability).

A 6 m tall, $125 \mathrm{~mm} \times 200 \mathrm{~mm}$ (metric) glu-lam column (Figure 4b) is braced in the weak axis $(\mathrm{y}-\mathrm{y})$ at 3.2 m from the base. The ends can be considered to be pinned. The timber has the following tabular design values:

$$
\mathrm{F}_{\mathrm{c}}=13.8 \mathrm{MPa}, \mathrm{E}=12,400 \mathrm{MPa}:
$$

b) If the column is to support 180 kN , is it adequate for Allowable Stress Design assuming a two month snow load duration? $\left(\mathrm{A}=25.0 \times 10^{-3} \mathrm{~m}^{2}\right)$.


Figure 4b.
a) $\mathrm{S}_{\text {req'd }} \geq 94.83 \mathrm{in}^{3}, \mathrm{~A}_{\text {req'd }} \geq 63.5 \mathrm{in}^{2}$
b) $\mathrm{P}_{\text {allowable }}=136 \mathrm{kN} \therefore$ No Good $\quad\left(\mathrm{P}_{\text {weak }}=182.9 \mathrm{kN}\right.$ weak direction)
REFERENCE CHARTS FOR QUIZ 4

| 1. SIMPLE BEAM-UNIFORMLY DISTRIBUTED LOAD <br> Total Equiv. Uniform Load . . . = wl <br> $\mathrm{R}=\mathrm{v}$. . . . . . . . . $=\frac{w l}{2}$ <br> $\mathrm{v}_{\mathrm{x}}$. . . . . . . . $-w\left(\frac{l}{2}-\mathrm{x}\right)$ <br> $M_{\text {max. }}$ (at center ) . . . . $=\frac{w / 2}{8}$ <br> $m_{\mathrm{x}}$. . . . . . . . . . $=\frac{w \mathrm{x}}{2}(l-\mathrm{x})$ <br> $\Delta$ max. (at center) . . . $=\frac{5 \text { w/4 }}{384}$ <br> $\Delta \mathrm{x}$. . . . . . . . . . $\left.=\frac{w \mathrm{X}}{24 \mathrm{EI}}{ }^{(13}-21 \mathrm{x}^{2}+\mathrm{x}^{3}\right)$ | 4. SIMPLE BEAM-UNIFORM LOAD PARTIALLY DISTRIBUTED |
| :---: | :---: |
| 2. SIMPLE BEAM-LOAD INCREASING UNIFORMLY TO ONE END <br> Total Equiv. Uniform Load . . . $=\frac{16 \mathrm{~W}}{9 \sqrt{3}}=1.0264 \mathrm{~W}$ <br> $R_{1}=v_{1} \ldots . . . . . .=\frac{w}{3}$ <br> $R_{2}=v_{2}$ max. . . . . . . $=\frac{2 W}{3}$ <br> $\mathrm{v}_{\mathrm{x}}$. . . . . . . . . . $=\frac{\mathrm{w}}{3}-\frac{\mathrm{w}^{2}}{l^{2}}$ <br> $M_{\text {max. }}\left(\right.$ at $\left.\mathrm{x}=\frac{l}{\sqrt{3}}=.5774 l\right) . \quad=\frac{2 \mathrm{~W} l}{9 \sqrt{3}}=.1283 \mathrm{~W} l$ <br> $M_{x}$. . . . . . . . $=\frac{w_{x}}{3 l^{2}}\left(l^{2}-x^{2}\right)$ <br>  <br>  | 5. SIMPLE BEAM—UNIFORM LOAD PARTIALLY DISTRIBUTED AT ONE END <br> $\mathbf{R}_{\mathbf{1}}=\mathrm{V}_{\mathbf{1}}$ max. <br> $R_{2}=V_{2}$. <br> $=\frac{w \mathrm{a}}{2 l}(2 l-\mathrm{a})$ <br> $=\frac{w \mathrm{a}^{2}}{2 l}$ <br> $\mathrm{v}_{\mathrm{x}} \quad($ when $\mathrm{x}<\mathbf{a}) \cdots \cdots \mathrm{R}_{1}-w \mathrm{x}$ <br> $M_{\max .}\left(\right.$ at $\left.\mathrm{x}=\frac{\mathbf{R}_{\mathbf{1}}}{w}\right) \cdots \cdots \mathrm{R}_{1}{ }^{2}$ <br> ${ }_{\uparrow}^{k} v_{2} M_{x} \quad($ when $x<a) \cdots R_{1} \quad \cdots-\frac{w x^{2}}{2}$ <br> $M_{x} \quad($ when $x>a) \cdots \cdots R_{2}(l-x)$ <br>  <br> 6. SIMPLE BEAM-UNIFORM LOAD PARTIALLY DISTRIBUTED AT EACH END |
| 3. SIMPLE BEAM-LOAD INCREASING UNIFORMLY TO CENTER |  <br> $\mathrm{V}_{\mathrm{x}} \quad($ when $\mathrm{x}<\mathrm{a}) \quad . \quad . \quad . \quad . \quad=\mathbf{R}_{1}-w_{1} \mathrm{x}$ <br> $\mathbf{V}_{\mathrm{x}} \quad($ when $\mathrm{x}>\mathrm{a}$ and $<(\mathbf{a}+\mathrm{b})) \quad . \quad=\mathbf{R}_{1}-w_{1} \mathbf{a}$ <br> $\mathrm{V}_{\mathrm{x}} \quad($ when $\mathrm{x}>(\mathbf{a}+\mathrm{b})) . . \quad . \quad=\mathbf{R}_{\mathbf{2}}-w_{\mathbf{2}}(l-\mathrm{x})$ <br> $M$ max. $\left(\right.$ at $x=\frac{\mathbf{R}_{\mathbf{1}}}{w_{1}}$ when $\left.\mathbf{R}_{\mathbf{1}}<w_{1} \mathrm{a}\right) \quad . \quad=\frac{\mathbf{R}_{\mathbf{1}}{ }^{\mathbf{2}}}{2 w_{1}}$ <br> $M_{\text {max. }}\left(\right.$ at $\mathrm{x}=l-\frac{\mathbf{R}_{\mathbf{2}}}{w_{2}}$ when $\left.\mathbf{R}_{\mathbf{2}}<w_{\mathbf{2}} \mathrm{C}\right)=\frac{\mathbf{R}_{\mathbf{2}}{ }^{2}}{2 w_{\mathbf{2}}}$ <br> $M_{\mathrm{X}} \quad($ when $\mathrm{x}<\mathrm{a}) \quad$. . . . $=R_{1 \times} \mathrm{X}-\frac{\mathrm{w}_{1} \mathrm{x}^{2}}{2}$ <br> $M_{X} \quad($ when $x>a$ and $<(a+b)) \quad=R_{1} x-\frac{w_{1} a}{2}(2 x-a)$ <br> $M_{\mathrm{x}} \quad($ when $x>(a+b)) . \quad . \quad=R_{2}(l-x)-\frac{w_{2}(l-x)^{2}}{2}$ |

REFERENCE CHARTS FOR OUIZ 4


## REFERENCE CHARTS FOR OUIZ 4

Section Properties of Dimension Western Lumber Sizes

| Nominal Size $(b \times h)$ (in.) | Surfaced <br> Dry Size (actual) (in.) | $\begin{gathered} \text { Nominal } \\ \text { Size } \\ (b \times h) \\ (\mathrm{mm}) \end{gathered}$ | Surfaced <br> Dry Size <br> (actual) (mm) | Area $\begin{gathered} A=(b) \times \\ (h) \\ \left(\text { in. }{ }^{2}\right) \end{gathered}$ | $\begin{gathered} \text { Area } \\ A=b h \\ \times 10^{3} \mathrm{~mm}^{2} \end{gathered}$ | Section Modulus $S=b h^{2} / 6$ $\text { (in. }{ }^{3} \text { ) }$ | Section <br> Modulus $S=b h^{2} / 6$ <br> $\times 10^{3} \mathrm{~mm}^{3}$ | Moment of Inertia $I=b h^{3} / 12$ (in. ${ }^{4}$ ) | Moment of Inertia $I=\vec{B}^{6} / 12$ $\times 10^{6} \mathrm{~mm}^{4}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $2 \times 2$ | $1.5 \times 1.5$ | $50 \times 50$ | $38 \times 38$ | 2.25 | 1.44 | 0.56 | 9.12 | 0.42 | 0.17 |
| $2 \times 3$ | $1.5 \times 2.5$ | $50 \times 75$ | $38 \times 64$ | 3.75 | 2.43 | 1.56 | 25.9 | 1.95 | 0.83 |
| $2 \times 4$ | $1.5 \times 3.5$ | $50 \times 100$ | $38 \times 89$ | 5.25 | 3.38 | 3.06 | 50.2 | 5.36 | 2.23 |
| $2 \times 6$ | $1.5 \times 5.5$ | $50 \times 150$ | $38 \times 140$ | 8.25 | 5.32 | 7.58 | 124 | 20.80 | 8.69 |
| $2 \times 8$ | $1.5 \times 7.25$ | $50 \times 200$ | $38 \times 184$ | 10.88 | 6.99 | 13.14 | 214 | 47.63 | 19.7 |
| $2 \times 10$ | $1.5 \times 9.25$ | $50 \times 250$ | $38 \times 235$ | 13.88 | 8.93 | 21.39 | 350 | 98.93 | 41.1 |
| $2 \times 12$ | $1.5 \times 11.25$ | $50 \times 300$ | $38 \times 286$ | 16.88 | 10.87 | 31.64 | 518 | 177.98 | 74.1 |
| $3 \times 3$ | $2.5 \times 2.5$ | $75 \times 75$ | $64 \times 64$ | 6.25 | 4.10 | 2.60 | 43.7 | 3.26 | 1.40 |
| $3 \times 4$ | $2.5 \times 3.5$ | $75 \times 100$ | $64 \times 89$ | 8.75 | 5.70 | 5.10 | 84.5 | 8.93 | 3.76 |
| $3 \times 6$ | $2.5 \times 5.5$ | $75 \times 150$ | $64 \times 140$ | 13.75 | 8.96 | 12.60 | 209 | 34.66 | 14.6 |
| $3 \times 8$ | $2.5 \times 7.25$ | $75 \times 200$ | $64 \times 184$ | 18.12 | 11.78 | 21.90 | 361 | 79.39 | 33.2 |
| $3 \times 10$ | $2.5 \times 9.25$ | $75 \times 250$ | $64 \times 235$ | 23.12 | 15.04 | 35.65 | 589 | 164.89 | 69.2 |
| $3 \times 12$ | $2.5 \times 11.25$ | $75 \times 300$ | $64 \times 286$ | 28.12 | 18.30 | 52.73 | 872 | 296.63 | 124.7 |
| $4 \times 4$ | $3.5 \times 3.5$ | $100 \times 100$ | $89 \times 89$ | 12.25 | 7.92 | 7.15 | 118 | 12.51 | 5.23 |
| $4 \times 6$ | $3.5 \times 5.5$ | $100 \times 150$ | $89 \times 140$ | 19.25 | 12.5 | 17.65 | 292 | 48.53 | 20.4 |
| $4 \times 8$ | $3.5 \times 7.25$ | $100 \times 200$ | $89 \times 184$ | 25.38 | 16.4 | 30.66 | 502 | 111.15 | 46.2 |
| $4 \times 10$ | $3.5 \times 9.25$ | $100 \times 250$ | $89 \times 235$ | 32.38 | 20.9 | 49.91 | 819 | 230.84 | 96.3 |
| $4 \times 12$ | $3.5 \times 11.25$ | $100 \times 300$ | $89 \times 286$ | 39.38 | 25.4 | 73.83 | 1213 | 415.28 | 174 |
| $4 \times 14$ | $3.5 \times 13.25$ | $100 \times 350$ | $89 \times 335$ | 46.38 | 29.8 | 102.41 | 1664 | 678.48 | 279 |
| $6 \times 6$ | $5.5 \times 5.5$ | $150 \times 150$ | $140 \times 140$ | 30.25 | 19.6 | 27.7 | 457 | 76.3 | 32.0 |
| $6 \times 8$ | $5.5 \times 7.5$ | $150 \times 200$ | $140 \times 191$ | 41.25 | 26.7 | 51.6 | 851 | 193.4 | 81.3 |
| $6 \times 10$ | $5.5 \times 9.5$ | $150 \times 250$ | $140 \times 241$ | 52.25 | 33.7 | 82.7 | 1355 | 393.0 | 163 |
| $6 \times 12$ | $5.5 \times 11.5$ | $150 \times 300$ | $140 \times 292$ | 63.25 | 40.9 | 121.2 | 1989 | 697.1 | 290 |
| $6 \times 14$ | $5.5 \times 13.5$ | $150 \times 350$ | $140 \times 343$ | 74.25 | 48.0 | 167.1 | 2745 | 1127.7 | 471 |
| $8 \times 8$ | $7.5 \times 7.5$ | $200 \times 200$ | $191 \times 191$ | 56.25 | 36.5 | 70.3 | 1161 | 263.7 | 111 |
| $8 \times 10$ | $7.5 \times 9.5$ | $200 \times 250$ | $191 \times 241$ | 71.25 | 46.0 | 112.8 | 1849 | 535.9 | 223 |
| $8 \times 12$ | $7.5 \times 11.5$ | $200 \times 300$ | $191 \times 292$ | 86.25 | 55.8 | 165.3 | 2714 | 950.6 | 396 |
| $8 \times 14$ | $7.5 \times 13.5$ | $200 \times 350$ | $191 \times 343$ | 101.25 | 65.5 | 227.8 | 3745 | 1537.7 | 642 |
| $8 \times 16$ | $7.5 \times 15.5$ | $200 \times 400$ | $191 \times 394$ | 116.25 | 75.2 | 300.3 | 4942 | 2327.4 | 974 |
| $10 \times 10$ | $9.5 \times 9.5$ | $250 \times 250$ | $241 \times 241$ | 90.25 | 58.1 | 142.9 | 2333 | 678.8 | 281 |
| $10 \times 12$ | $9.5 \times 11.5$ | $250 \times 300$ | $241 \times 292$ | 109.25 | 70.4 | 209.4 | 3425 | 1204.0 | 500 |
| $10 \times 14$ | $9.5 \times 13.5$ | $250 \times 350$ | $241 \times 343$ | 128.25 | 82.7 | 288.6 | 4726 | 1947.8 | 810 |
| $10 \times 16$ | $9.5 \times 15.5$ | $250 \times 400$ | $241 \times 394$ | 147.25 | 95.0 | 380.4 | 6235 | 2948.1 | 1228 |
| $12 \times 12$ | $11.5 \times 11.5$ | $300 \times 300$ | $292 \times 292$ | 132.25 | 85.3 | 253.5 | 4150 | 1457.5 | 606 |
| $12 \times 14$ | $11.5 \times 13.5$ | $300 \times 350$ | $292 \times 343$ | 155.25 | 100 | 349.3 | 5726 | 2357.9 | 982 |
| $12 \times 16$ | $11.5 \times 15.5$ | $300 \times 400$ | $292 \times 394$ | 178.25 | 115 | 460.5 | 7555 | 3568.7 | 1488 |
| $12 \times 18$ | $11.5 \times 17.5$ | $300 \times 450$ | $292 \times 445$ | 201.25 | 130 | 587.0 | 9637 | 5136.1 | 2144 |

## REFERENCE CHARTS FOR OUIZ 4

Table 14 Column Stability Factor C $_{\mathrm{p}}$.

(continued)

## REFERENCE CHARTS FOR QUIZ 4

Table 14 Column Stability Factor $\mathrm{C}_{\mathrm{p}}$. (Continued)

|  |  |  | " $C_{p}$ " | $F_{c}^{\prime}=C_{p} \cdot F_{c}^{*} \quad F_{C E}=\frac{.30 E}{(l / d)^{2}}$ |  |  |  |  | $\frac{.418 E}{(l / d)^{2}}$ fo | for glu-lam posts |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\frac{F_{C E}}{F_{C}}$ | Sawed $C_{p}$ | Glu-Lam $C_{p}$ | $\frac{F_{C E}}{F_{C}^{*}}$ | Sawed $C_{p}$ | Glu-Lam $C_{p}$ | $\frac{F_{C E}}{F_{C}}{ }^{*}$ | Sawed $C_{p}$ | Glu-Lam $C_{p}$ | $\frac{F_{C E}}{F_{C}^{*}} \mathrm{Sa}$ | Sawed $C_{p}$ | $\begin{aligned} & \text { lu-Lam } \\ & C_{p} \end{aligned}$ |
| 2.00 | 0.867 | 0.921 | 2.40 | 0.894 | 0.940 | 3.40 | 0.930 | 0.962 | 4.40 | 0.948 | 0.972 |
| 2.02 | 0.869 | 0.922 | 2.45 | 0.897 | 0.941 | 3.45 | 0.931 | 0.963 | 4.45 | 0.949 | 0.973 |
| 2.04 | 0.870 | 0.924 | 2.50 | 0.899 | 0.943 | 3.50 | 0.932 | 0.963 | 4.50 | 0.949 | 0.973 |
| 2.06 | 0.872 | 0.925 | 2.55 | 0.901 | 0.944 | 3.55 | 0.933 | 0.964 | 4.55 | 0.950 | 0.974 |
| 2.08 | 0.874 | 0.926 | 2.60 | 0.904 | 0.946 | 3.60 | 0.934 | 0.965 | 4.60 | 0.950 | 0.974 |
| 2.10 | 0.875 | 0.927 | 2.65 | 0.906 | 0.947 | 3.65 | 0.936 | 0.965 | 4.65 | 0.951 | 0.974 |
| 2.12 | 0.876 | 0.928 | 2.70 | 0.908 | 0.949 | 3.70 | 0.937 | 0.966 | 4.70 | 0.952 | 0.975 |
| 2.14 | 0.878 | 0.929 | 2.75 | 0.910 | 0.950 | 3.75 | 0.938 | 0.966 | 4.75 | 0.952 | 0.975 |
| 2.16 | 0.879 | 0.930 | 2.80 | 0.912 | 0.951 | 3.80 | 0.938 | 0.967 | 4.80 | 0.953 | 0.975 |
| 2.18 | 0.881 | 0.931 | 2.85 | 0.914 | 0.952 | 3.85 | 0.939 | 0.968 | 4.85 | 0.953 | 0.975 |
| 2.20 | 0.882 | 0.932 | 2.90 | 0.916 | 0.953 | 3.90 | 0.940 | 0.968 | 4.90 | 0.954 | 0.976 |
| 2.22 | 0.883 | 0.932 | 2.95 | 0.917 | 0.954 | 3.95 | 0.941 | 0.969 | 5.00 | 0.955 | 0.976 |
| 2.24 | 0.885 | 0.933 | 3.00 | 0.919 | 0.955 | 4.00 | 0.942 | 0.969 | 6.00 | 0.963 | 0.981 |
| 2.26 | 0.886 | 0.934 | 3.05 | 0.920 | 0.956 | 4.05 | 0.943 | 0.969 | 8.00 | 0.973 | 0.986 |
| 2.28 | 0.887 | 0.935 | 3.10 | 0.922 | 0.957 | 4.10 | 0.944 | 0.970 | 10.0 | 0.979 | 0.989 |
| 2.30 | 0.888 | 0.936 | 3.15 | 0.923 | 0.958 | 4.15 | 0.944 | 0.970 | 20.0 | 0.990 | 0.995 |
| 2.32 | 0.889 | 0.937 | 3.20 | 0.925 | 0.959 | 4.20 | 0.945 | 0.971 | 40.0 | 0.995 | 0.997 |
| 2.34 | 0.891 | 0.937 | 3.25 | 0.926 | 0.960 | 4.25 | 0.946 | 0.971 | 60.0 | 0.997 | 0.998 |
| 2.36 | 0.892 | 0.938 | 3.30 | 0.927 | 0.961 | 4.30 | 0.947 | 0.972 | 100.0 | 0.998 | 0.999 |
| 2.38 | 0.893 | 0.939 | 3.35 | 0.929 | 0.961 | 4.35 | 0.947 | 0.972 | 200.0 | 0.999 | 0.999 |

Table developed and permission for use granted by Professor Ed Lebert, Dept. of Architecture, University of Washington.

Table 10.3 Load duration factors.

| $C_{D}$-Load Duration Adjustment |  |
| :--- | :---: |
| Load Duration | Factor |
| Permanent | 0.9 |
| Ten years (normal load) | 1.0 |
| Two months (snow load) | 1.15 |
| Seven days (construction load) | 1.25 |
| One day , , Wind or EQ) | 1.33 |
| Ten minutes | 1.6 |
| Impact | 2.0 |

